

Realization of the 5-Axis Machine Tool Digital Twin **Using Direct Servo Control from CAM**

Roby Lynn¹, Mukul Sati², Tommy Tucker³, Jarek
Rossignac², Christopher Saldana¹, Thomas Kurfess¹

¹George W. Woodruff School of Mechanical Engineering, Georgia Tech

²School of Interactive Computing, Georgia Tech

³Tucker Innovations, Inc.

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Introduction

- ❖ Machine tools are *difficult to operate*
 - Significant experience required for effective use

- ❖ Control

- Decades old G-Code
- Geometric primitives
- Unidirectional data transfer

- ❖ Feedback

- MTConnect
- OPC UA



```
G0 G17 G20 G40 G49 G64 G80 G90 G98 G54
G54.4 P0
G53 G90 G0 Z0.
G53 G90 G0 B80. C90.
G65 P9544 H1
G54.1 P300
G54.4 P1
S4800 M3
G43 H#3020 X-3.2923 Y-7.6496 Z8. B80. C90.
Z4.2575
G05 P2
G61.1 P3
G1 Z3.2575 F.02
G41 D#3020 Y-7.5079 F.006
G3 X-3.7647 Y-7.0354 I-.4724
G2 X-4.6077 Y-6.1924 J.843
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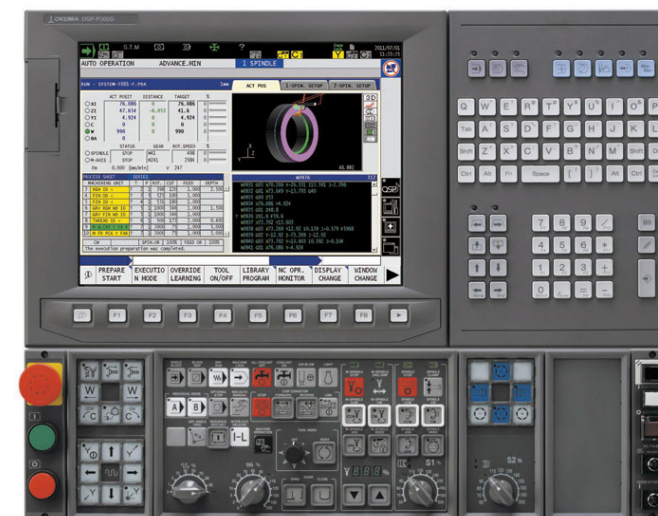
- ❖ *How can we use the digital twin concept to enable CNC machine tools to be operated as easily as 3D printers?*

Current Industrial Practice: CAM to G-Code to CNC

- ❖ CAM systems create G-Code using post processors
 - Machine specific instructions

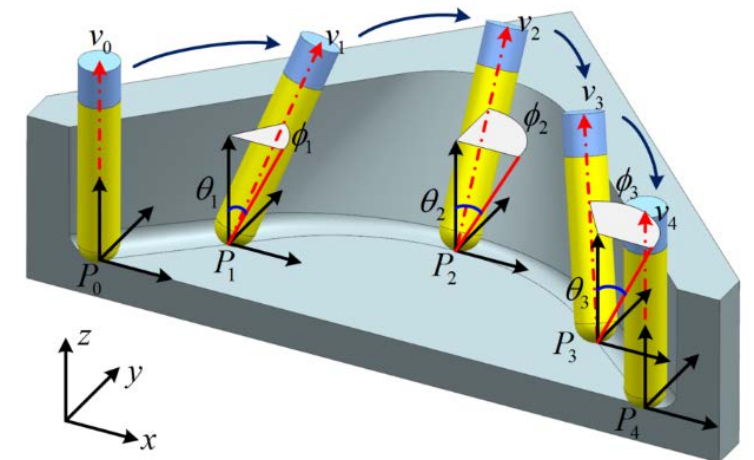
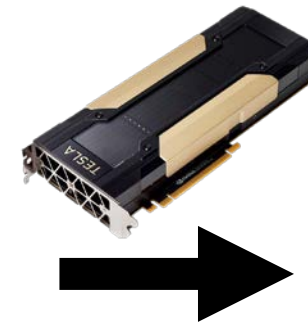
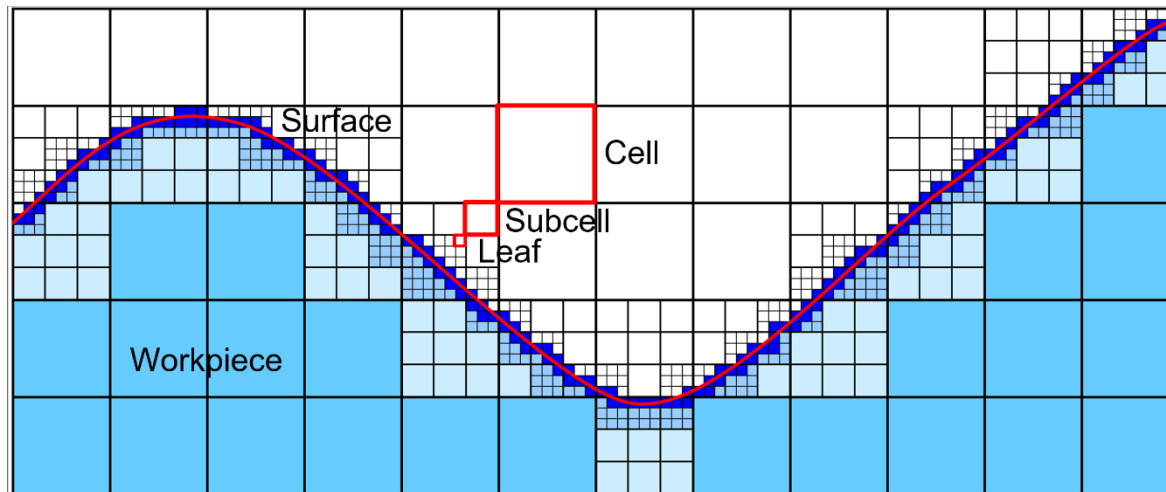
- ❖ G-Code: text-based NC programming language, originally standardized in 1960s, still dominant today
 - Serial execution
 - Lines, arcs, and splines (primitives)
 - Maximum traversal velocity

- ❖ Industrial CNC systems
 - Proprietary architecture
 - Lack of interoperability
 - Options available – at a cost



Digital Volumetric Processing (DVP) Using High-Performance Computing

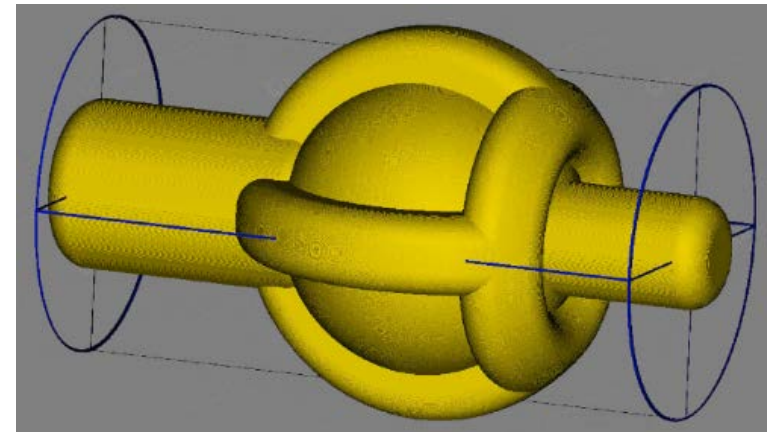
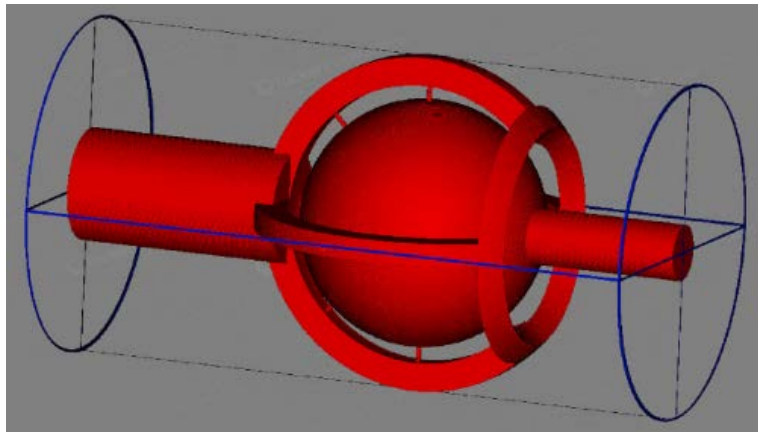
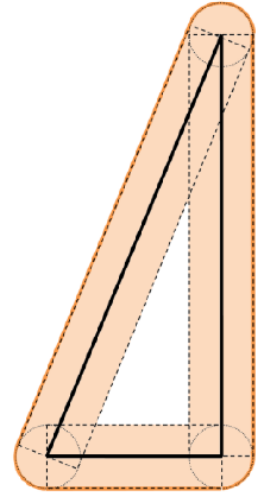
- ❖ Reformulation of the traditional toolpath planning problem
- ❖ Discrete Geometry
 - Part surface comprised of many small cubes called **voxels**
 - Voxel size s determines resolution of part surface
 - STLs, scans, point clouds
- ❖ High Performance Computing (HPC) using graphics processing units (GPUs)



5-Axis Voxel-Based Path Planning: Contact Volume Generation

- ❖ Constraints on tool center position
 - Axial cutting depth
 - Final part geometry

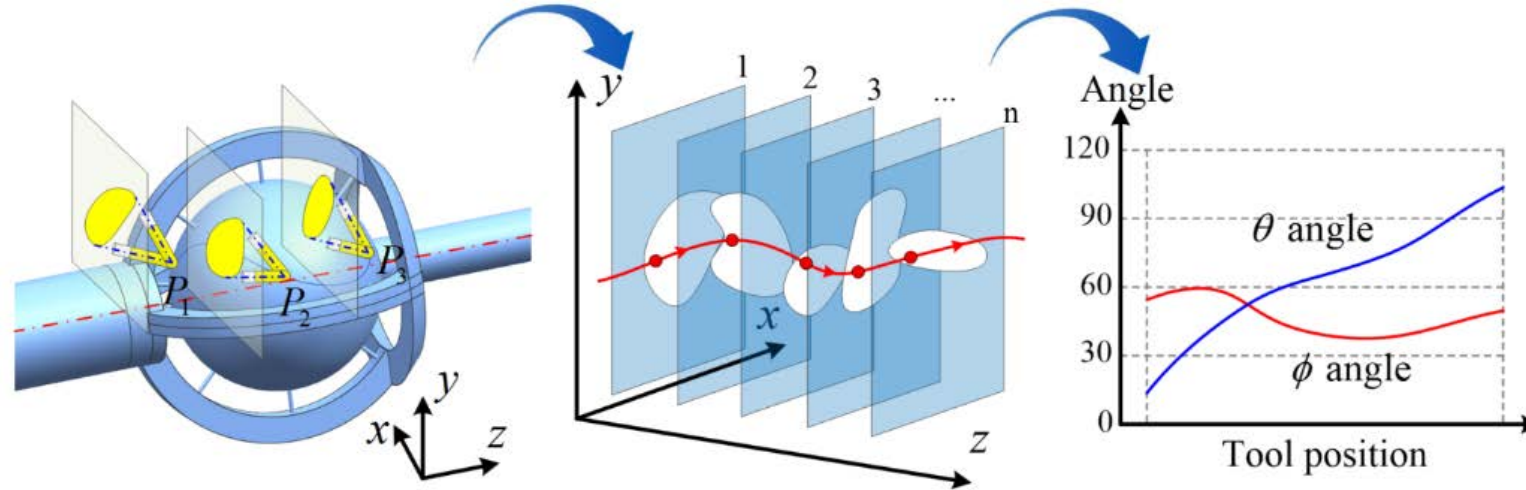
- ❖ A sequence of volumetric offsets
 - Positive offset (expansion) of model by tool radius and cutting allowance
 - Negative offset (shrinkage) of stock volume by DoC
 - Union



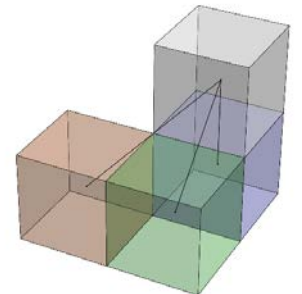
[2] R. Lynn, D. Contis, M. Hossain, N. Huang, T. Tucker, T. Kurfess. *Voxel Model Surface Offsetting for Computer-Aided Manufacturing Using Virtualized High-Performance Computing*. SME Journal of Manufacturing Systems, 2016.

[3] M. Hossain. *Voxel-Based Offsetting at High Resolution with Tunable Speed and Precision Using Hybrid Dynamic Trees*. Georgia Institute of Technology, 2016.

5-Axis Voxel-Based Path Planning: Accessibility Analysis



- ❖ Constraints on tool axis orientation
 - Collisions, travel constraints, surface normals
- ❖ Stack of binary bitmaps of unique orientations which are checked for collisions with workpiece and fixture
 - Access path through white regions on maps
- ❖ Result: toolpath consisting of *small, discrete, 5-axis movements* between voxels

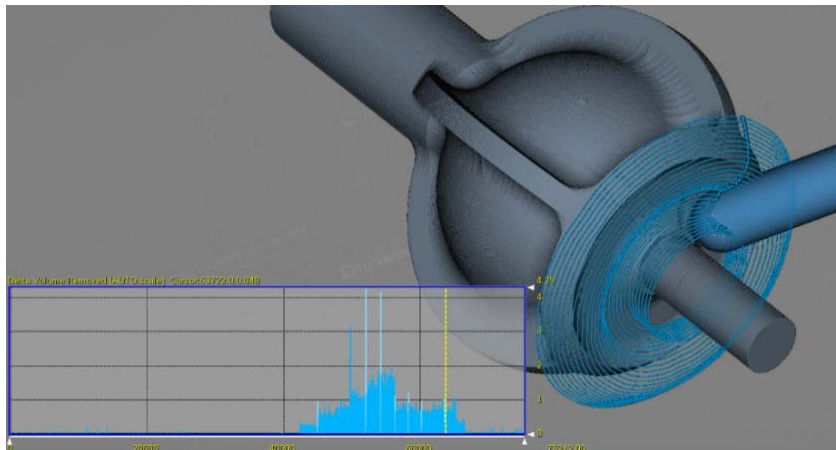


Process Intelligence: Material Removal Rate Analysis and Control Using Voxel-Based CAM

- ❖ Volume removed V_i is the sum of voxels of side length s swept by cutter envelope C over a step i

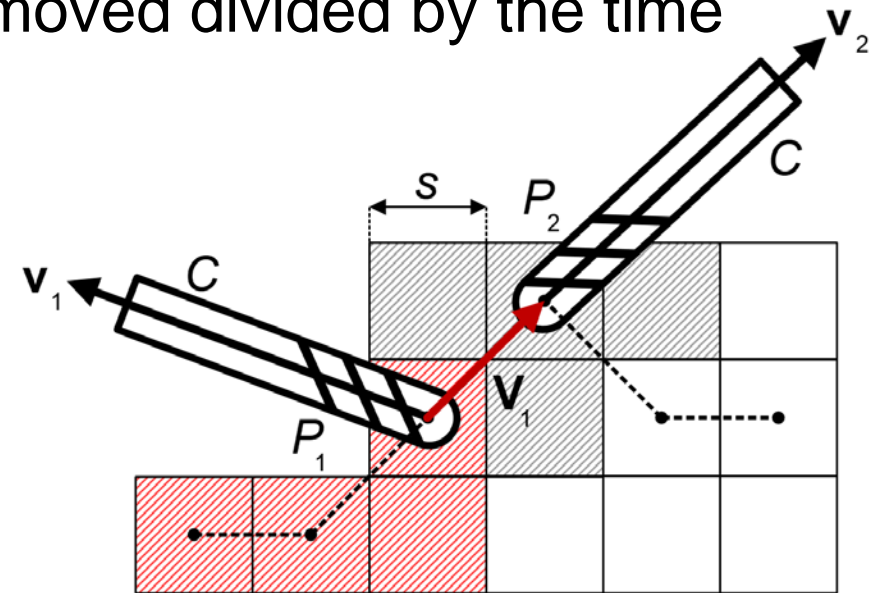
$$V_i = \sum_i dv \times s^3 \mid dv \in C_i$$

- ❖ Average MRR for the step i is the volume removed divided by the time taken to complete the step, Δt



$$MRR_i = \frac{V_i}{\Delta t_i}$$

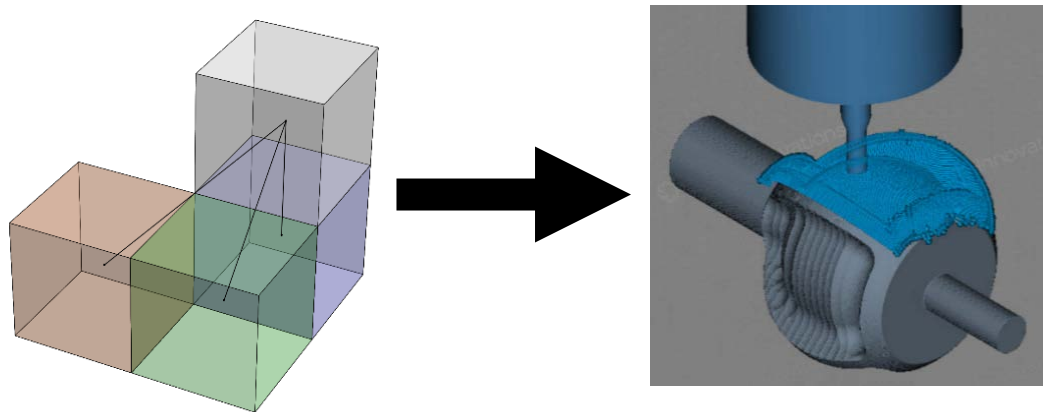
$$\Delta t_{i \rightarrow i+1} \geq \frac{\sum_i dv \times s^3}{MRR_{Limit}}$$



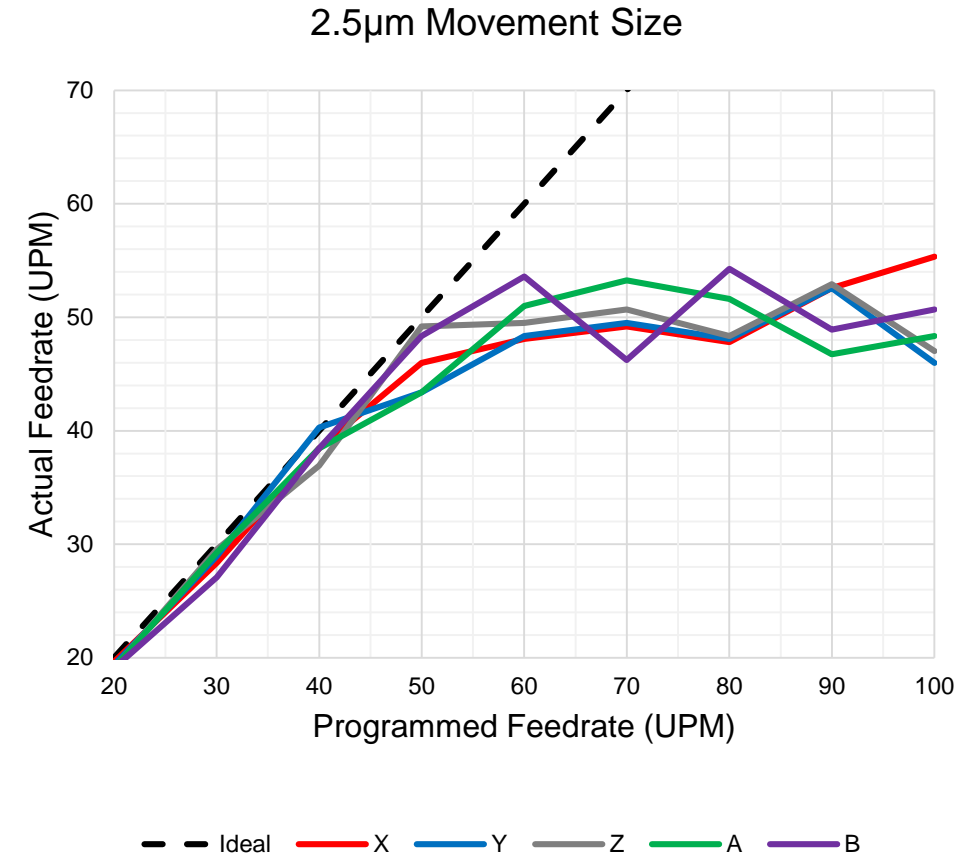
Traditional Method: DVP to G-Code

- ❖ Typical 5-axis block: G1XxYyZzAaBbFf
 - x, y, z, a, and b are endpoints
 - f is *maximum* speed
 - Velocity constrained so all axes arrive at the same time

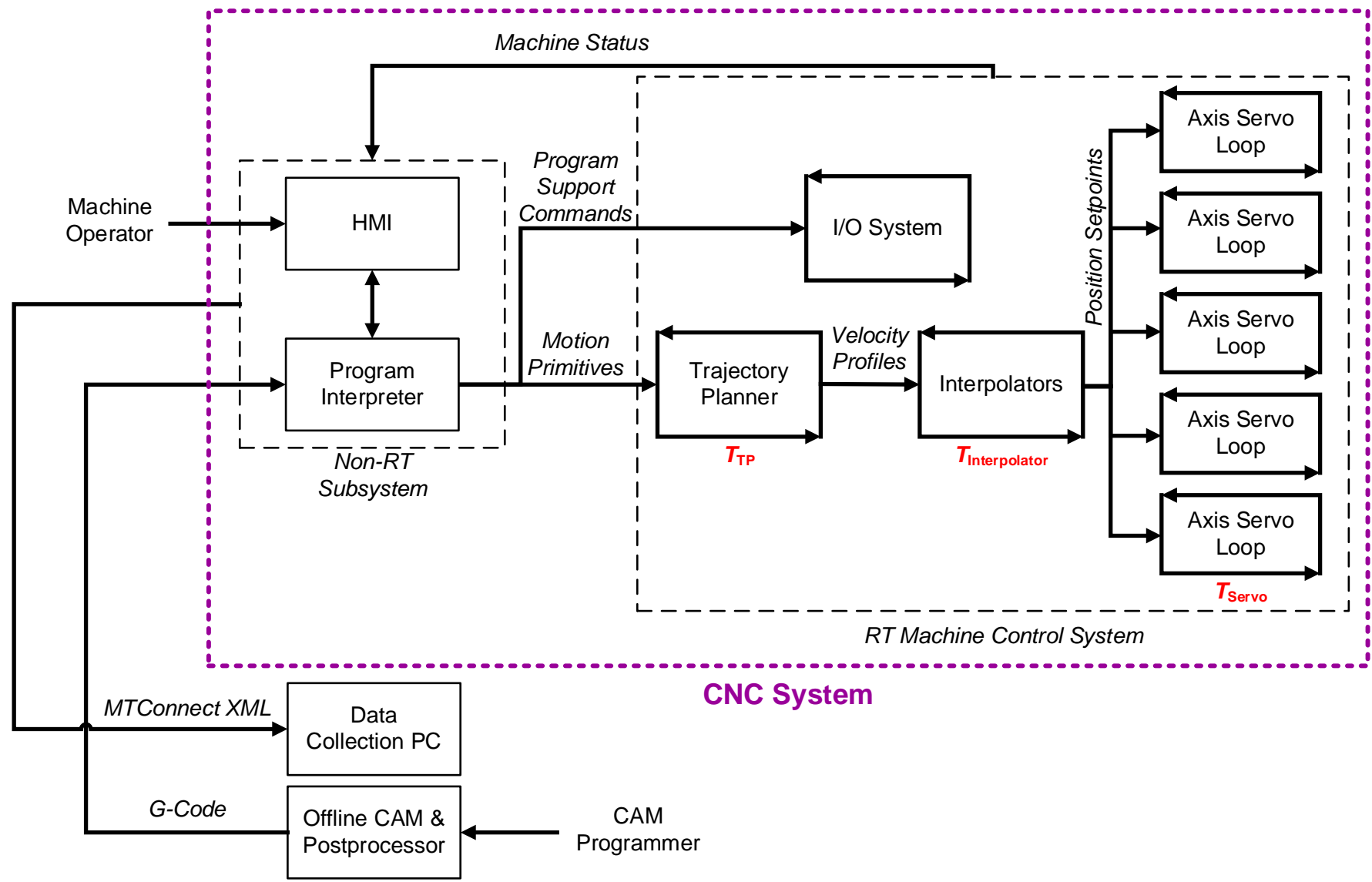
- ❖ For sufficiently small voxel sizes, a toolpath can consist of millions of linear movements (G1s) between voxel centers



$$L_{\text{Shared Face}} = s, \quad L_{\text{Shared Edge}} = \sqrt{2}s, \quad L_{\text{Shared Vertex}} = \sqrt{3}s$$

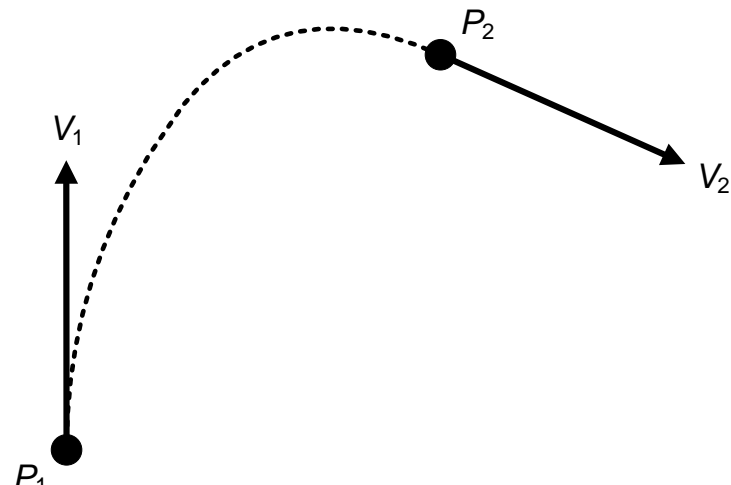


Traditional Method: Obfuscated Trajectory Planning



Direct Control Method: DVP to Servo Commands

- ❖ High speed communication of servo setpoints instead of geometric primitives

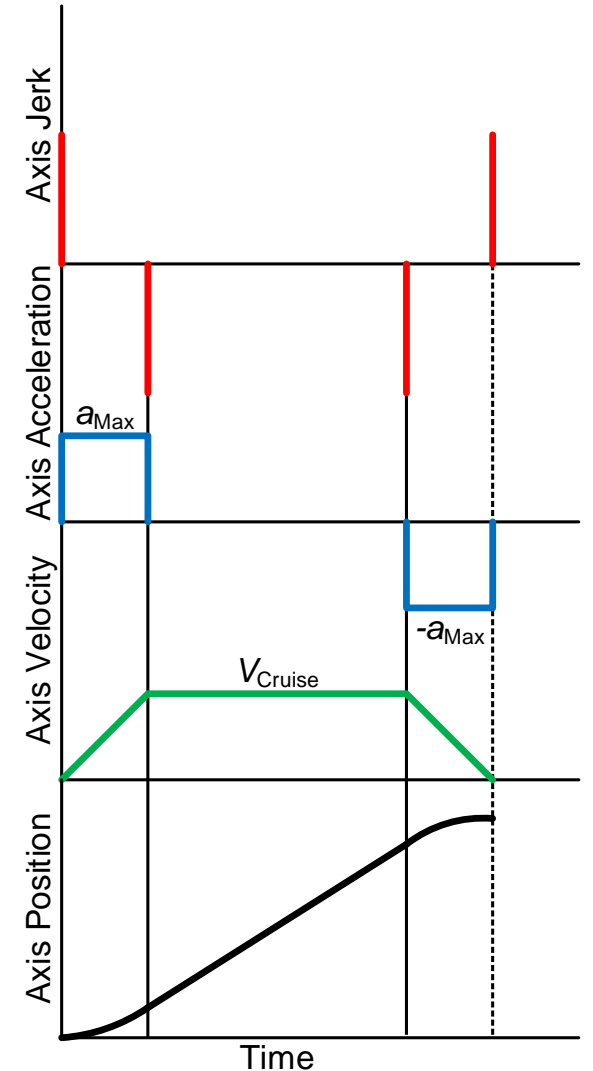


$$\Delta t_{i \rightarrow i+1} > 0 \quad \frac{\Delta^2 P}{\Delta t_{i \rightarrow i+1}^2} \leq A_{\text{Max}}$$

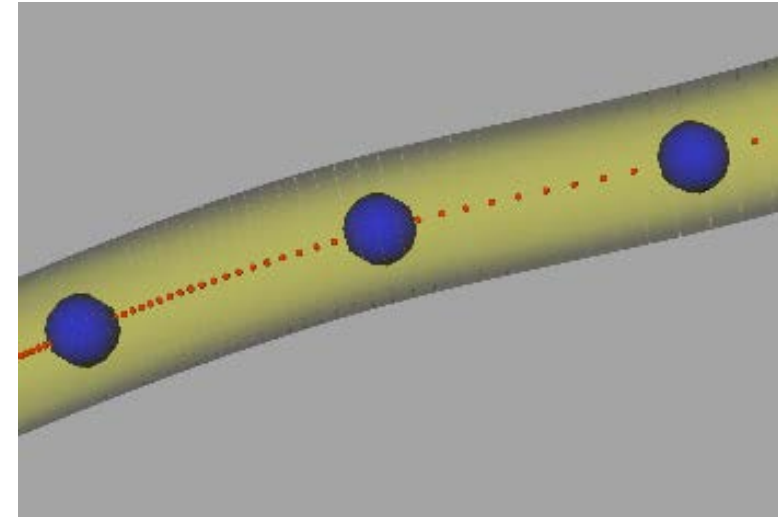
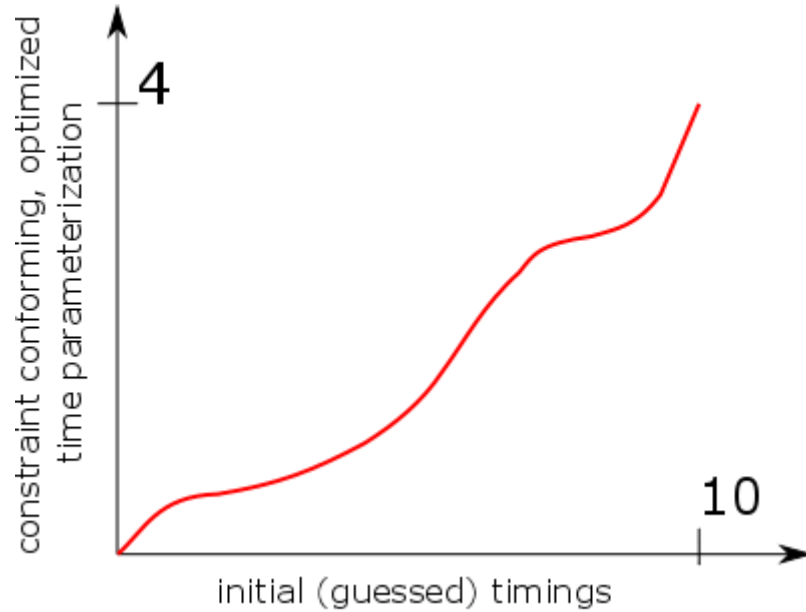
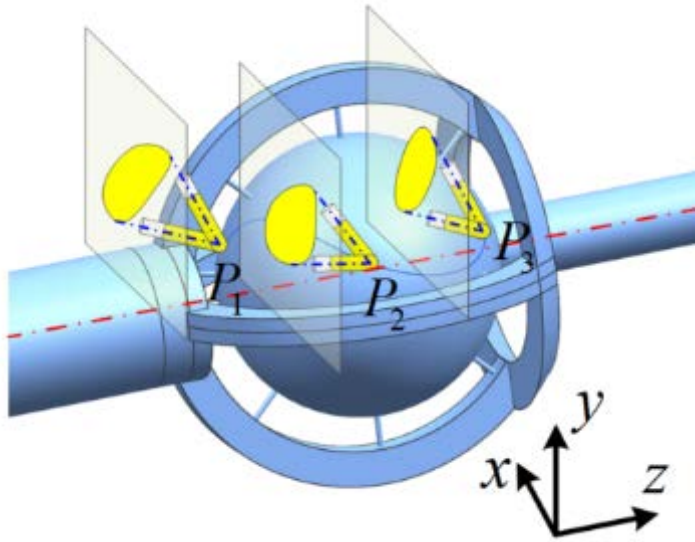
$$\frac{\Delta P}{\Delta t_{i \rightarrow i+1}} \leq V_{\text{Max}} \quad \frac{\Delta^3 P}{\Delta t_{i \rightarrow i+1}^3} \leq J_{\text{Max}}$$

- ❖ Time-optimal path planning

- Position constraints from CAM
- Machine kinematic constraints
- Spline fit to axis position commands
- Multiple solutions of robotic path planning strategy



DVP to Servo Commands: Mathematical Formulation



$$P_{T,i} = \begin{bmatrix} X_{T,i} \\ Y_{T,i} \\ Z_{T,i} \\ \theta_i \\ \phi_i \end{bmatrix} \quad P_{J,i} = \begin{bmatrix} X_{J,i} \\ Y_{J,i} \\ Z_{J,i} \\ A_i \\ B_i \end{bmatrix}$$

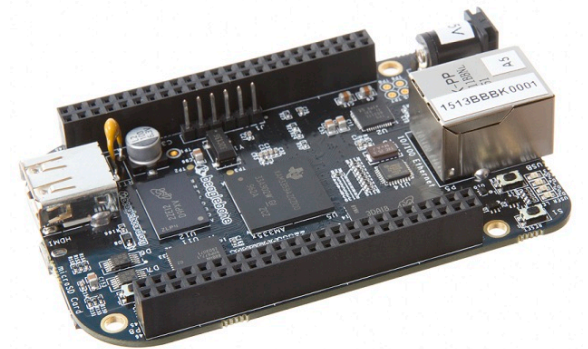
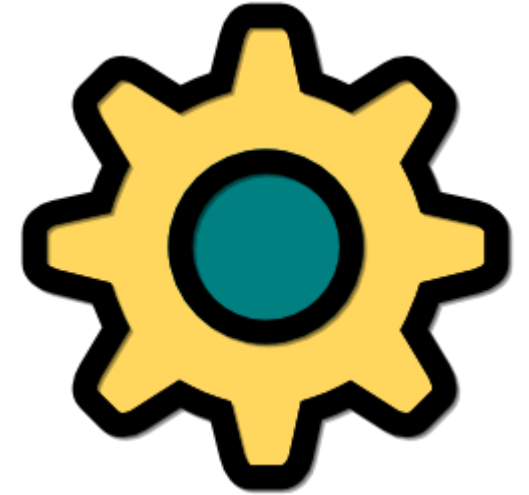
$$r^* = \operatorname{argmin}_R \left\{ \int_0^1 \left(\frac{dr}{dt} \right)^{-1} du \quad \left. \begin{array}{l} \frac{dJ}{dt} \leq V_{\text{Max}} \\ \frac{d^2J}{dt^2} \leq A_{\text{Max}} \\ \frac{dV}{dt} \leq \text{MRR}_{\text{Max}} \end{array} \right\}$$

$$P'_{J,i} = \begin{bmatrix} X'_{J,i} \\ Y'_{J,i} \\ Z'_{J,i} \\ A'_i \\ B'_i \end{bmatrix}$$

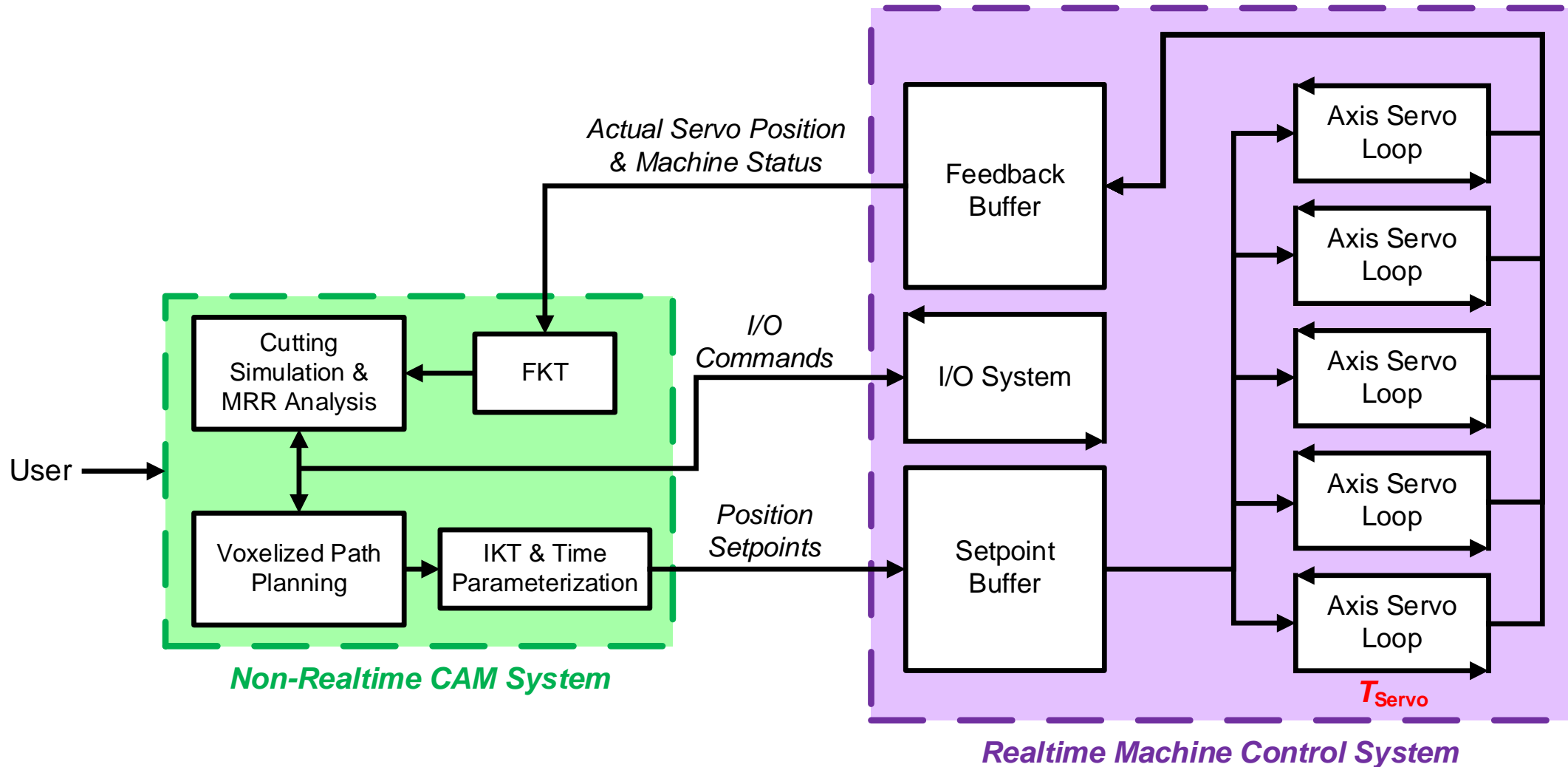
Direct Servo Control Method: Requirements and Capabilities

- ❖ Generalizable methodology for complete control of motion profiles directly from a CAM system
 - Pre-interpolated data with already-planned, optimized trajectories
 - Creation of joint space profiles at the servo rate with inverse kinematic transformation (IKT)
 - Use of open-source tools

- ❖ Dense feedback to CAM system to enable toolpath analysis and optimization
 - As-executed motion profile using forward kinematic transformation (FKT)
 - Positional derivatives along toolpath



Direct Servo Control from Voxel-Based CAM: Concept



Direct Servo Control from Voxel-Based CAM: Hardware Implementation

- ❖ Current Platform: PocketNC
 - \$4000 5-axis desktop machine tool
 - Beaglebone Black, Machinekit
 - Desktop-sized open CNC research platform

- ❖ WIP: Mori Seiki Retrofit

- ❖ Additional Capabilities
 - Enhanced control of tool trajectory and MRR
 - Richer feedback information
 - Improved usability for complex machines, similar to AM



Direct Servo Control from Voxel-Based CAM: The Machine Tool Digital Twin



Screenshot of the SculptPrint software interface (Version 4.0 - Pass7Mapped_pass7.scpr). The interface displays a 3D model of a machine tool and a graph showing the X-axis position (XPos) over time (X Axis 0,000 XPos:0,0 (AUTO scale)). The graph shows a step function with some noise, indicating the machine's response to a digital twin simulation.

Properties

X Axis	-0.398702264
Z Axis	-0.7416779
Spindle Axis	-90
Y Axis	-5.59411128E-05
A Axis	89.960434
B Axis	0
Vise Axis	-1
Stationary Screw Axis	1
Number of Axes	8
Name	PocketNC

Monitor Machine

Select axes to plot:

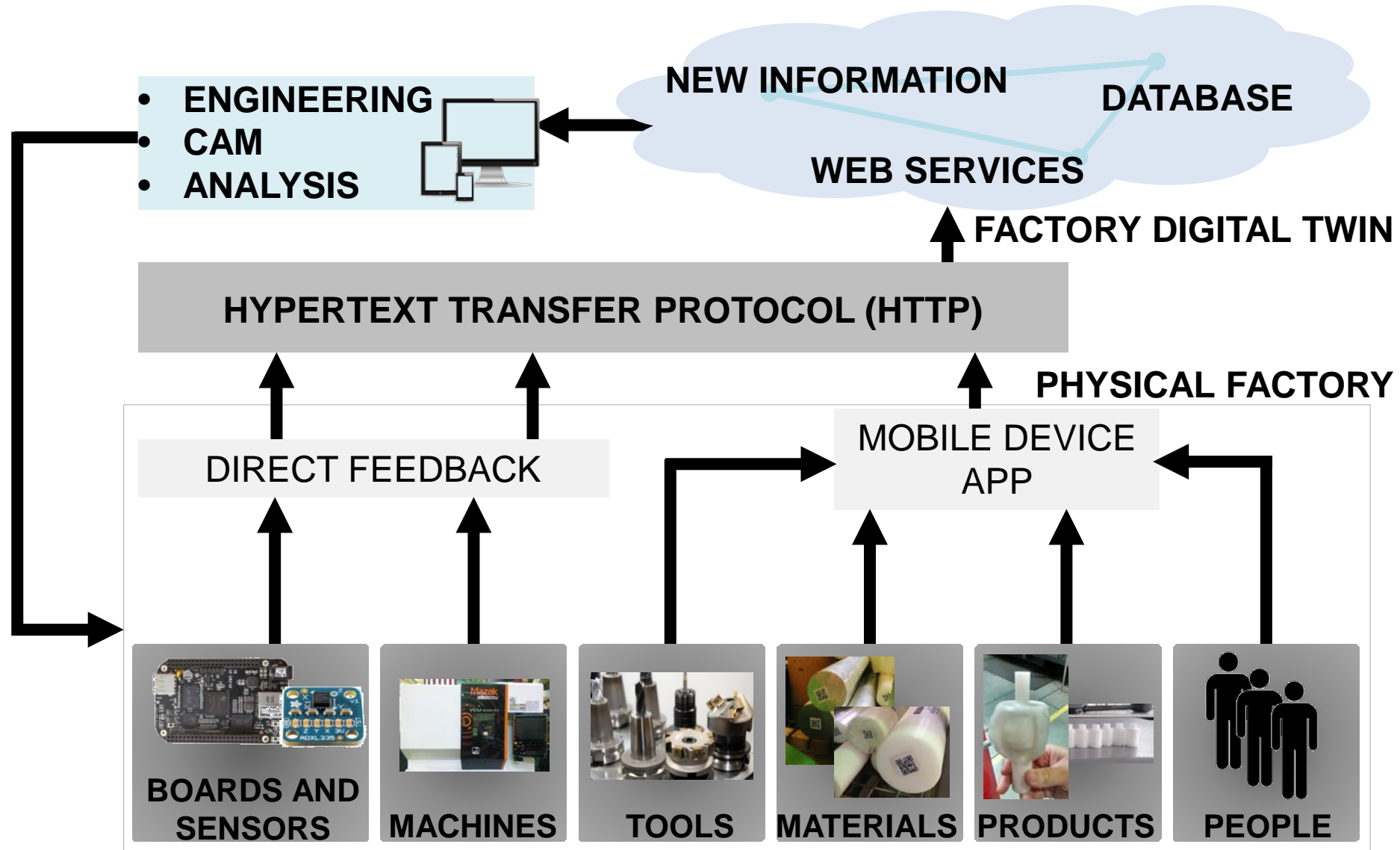
Axis Name	Label	Value
X Axis	X	0.03984902
Z Axis	Z	-0.5839313
Spindle Axis	S	-90
Y Axis	Y	0.1456011
A Axis	A	76.02734
B Axis	B	121.5384

Buttons: Disconnect, Start, OK, Cancel

Ready

[Click here for information: Guide](#)

Integration into Complete Shop Floor Digital Twin



Implications & Conclusions

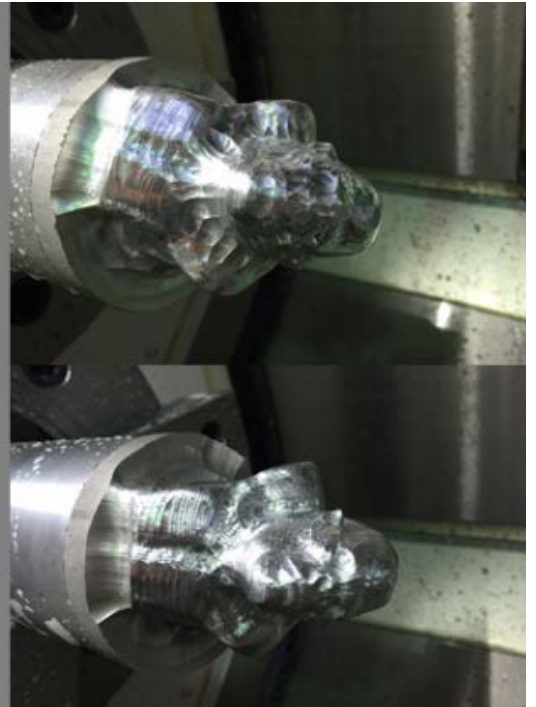
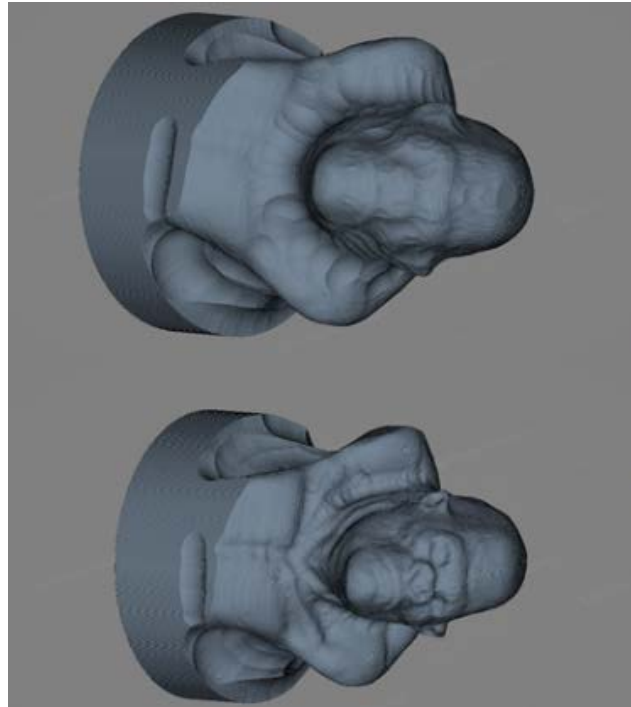
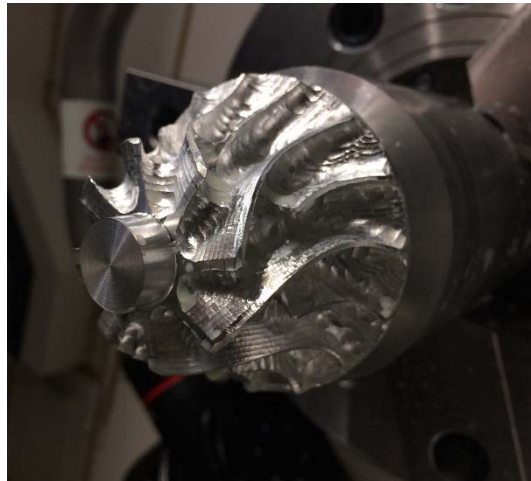
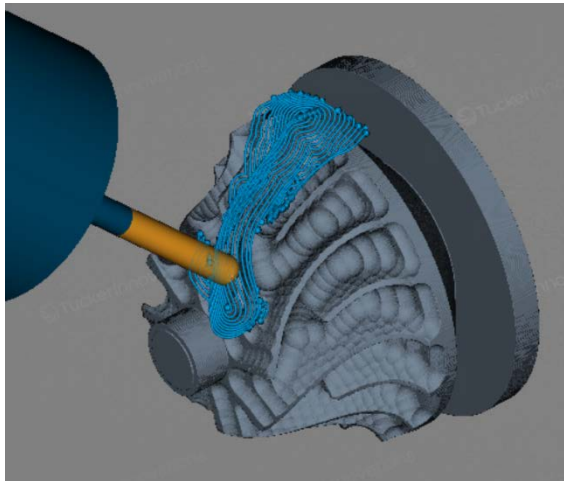
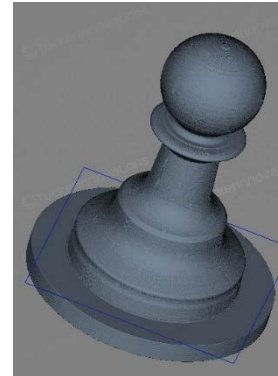
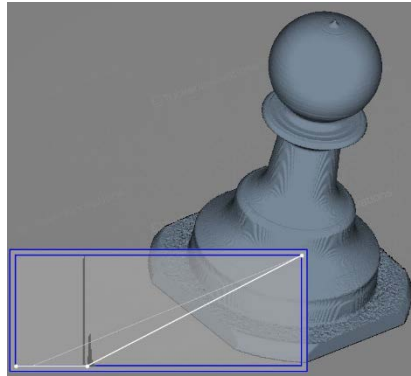
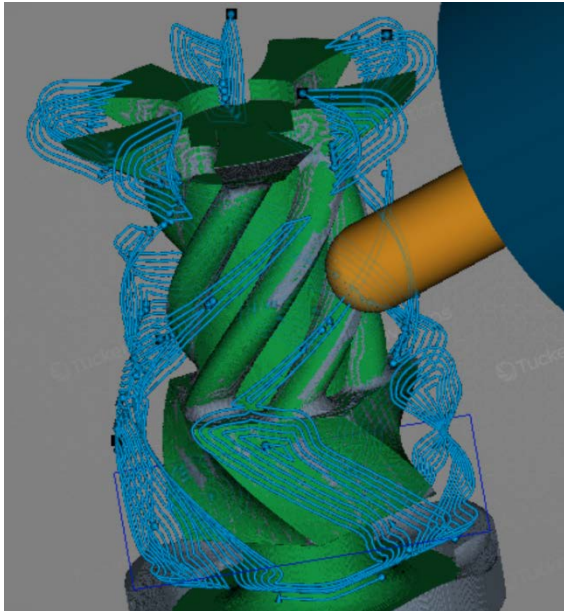
- ❖ Voxel-based CAM system
 - Intricate simulation, MRR analysis
- ❖ Time parameterization of 5-axis toolpaths using position samples from voxel models
 - Minimum time path planning, kinematic and MRR limits
- ❖ New strategy for control and monitoring of a 5-axis machine tool directly from CAM
 - Enables usability similar to typical 3D printers
 - Allow for tighter integration into shop floor digital twin

Questions?

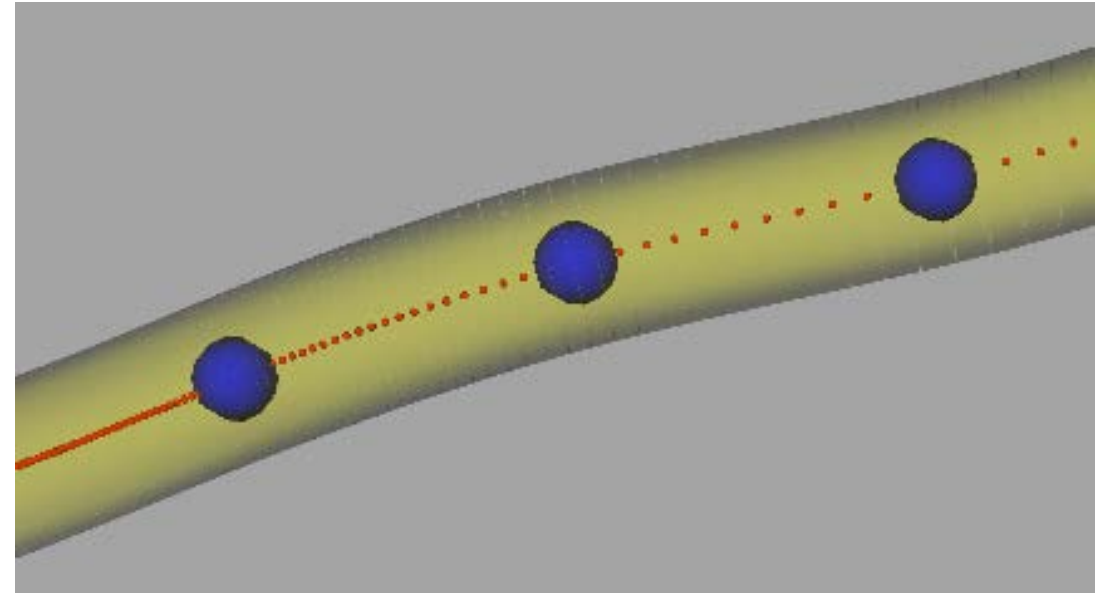
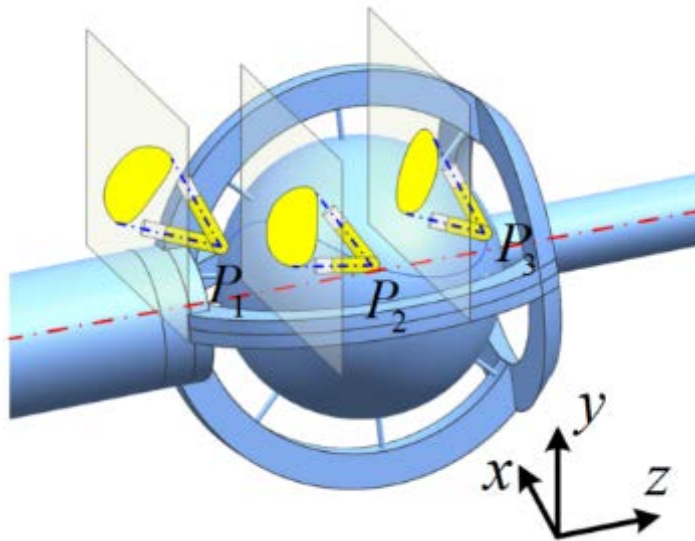
❖ Acknowledgements

- NSF Grants CMMI-1329742, CMMI-1547093, and IIP-1631083
- NSF GRFP DGE-1650044

DVP to Final Part



DVP to Servo Commands: Mathematical Formulation



$$P_{T,i} = \begin{bmatrix} X_{T,i} \\ Y_{T,i} \\ Z_{T,i} \\ \theta_i \\ \phi_i \end{bmatrix}$$

$$r^* = \operatorname{argmin}_R \left\{ \int_0^1 \left(\frac{dr}{dt} \right)^{-1} du \quad \left. \begin{array}{l} \frac{dJ}{dt} \leq V_{\text{Max}} \\ \frac{d^2J}{dt^2} \leq A_{\text{Max}} \\ \frac{dV}{dt} \leq \text{MRR}_{\text{Max}} \end{array} \right\}$$

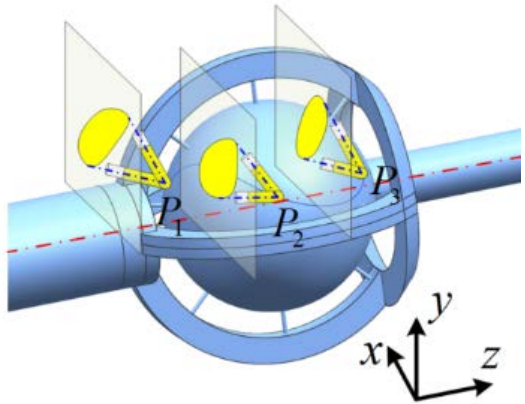
$$P_{J,i} = \begin{bmatrix} X_{J,i} \\ Y_{J,i} \\ Z_{J,i} \\ A_i \\ B_i \end{bmatrix}$$

DVP to Servo Commands: Mathematical Formulation

$$P_{T,i} = \begin{bmatrix} X_{T,i} \\ Y_{T,i} \\ Z_{T,i} \\ \theta_i \\ \phi_i \end{bmatrix} \quad M^{-1}(P_{T,i}) = \begin{bmatrix} \sin \theta_i & -\sin \phi_i \cos \theta_i & \cos \phi_i \cos \theta_i \\ \cos \theta_i & \sin \phi_i \sin \theta_i & -\sin \phi_i \cos \theta_i \\ 0 & \cos \phi_i & \sin \phi_i \end{bmatrix}^{-1} \begin{bmatrix} -X_{T,i} - c_1 \cos \phi \cos \theta + c_2 \\ -Y_{T,i} + c_1 \sin \theta \cos \phi \\ -Z_{T,i} - c_1 \sin \phi - c_3 \end{bmatrix} \quad P_{J,i} = \begin{bmatrix} X_{J,i} \\ Y_{J,i} \\ Z_{J,i} \\ A_i \\ B_i \end{bmatrix}$$

$u \in [0,1] \quad r : t \rightarrow u, r^{-1} : u \rightarrow t \quad R = \{r \mid r \in C^1[\square \rightarrow \square]\}$

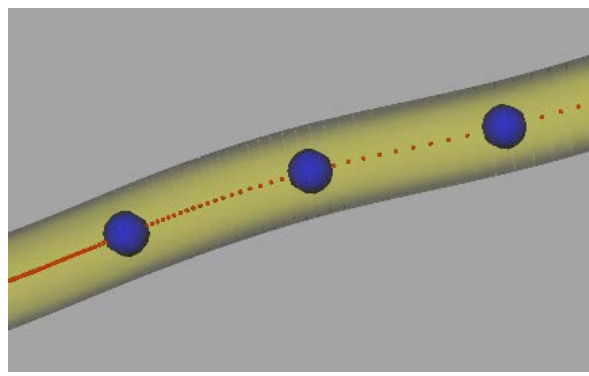
$$J : \begin{pmatrix} \square \rightarrow \square^5 \\ u \rightarrow J(u) \in P_J \end{pmatrix}$$



$$r^* = \operatorname{argmin}_R \left\{ \int_0^1 \left(\frac{dr}{dt} \right)^{-1} du \quad \left. \begin{array}{l} \frac{dJ}{dt} \leq V_{\text{Max}} \\ \frac{d^2J}{dt^2} \leq A_{\text{Max}} \\ \frac{dV}{dt} \leq \text{MRR}_{\text{Max}} \end{array} \right\}$$

$$\frac{dJ}{dt} = \frac{dJ}{dr} \frac{dr}{dt} \quad \frac{d^2J}{dt^2} = \frac{dJ}{dr} \frac{d^2r}{dt^2} + \frac{d^2J}{dr} \left(\frac{dr}{dt} \right)^2 \quad \frac{dV}{dt} = \frac{dV}{dr} \frac{dr}{dt}$$

$$T : \begin{pmatrix} \square \rightarrow \square^5 \\ u \rightarrow M(J(u)) \in P_T \end{pmatrix}$$



$$T' : \begin{pmatrix} \square \rightarrow \square^5 \\ u \rightarrow M(J(u)) + [0 \ 0 \ 0 \ \alpha(u) \ \beta(u)]^u \end{pmatrix}$$

Direct Servo Control from Voxel-Based CAM: Software

