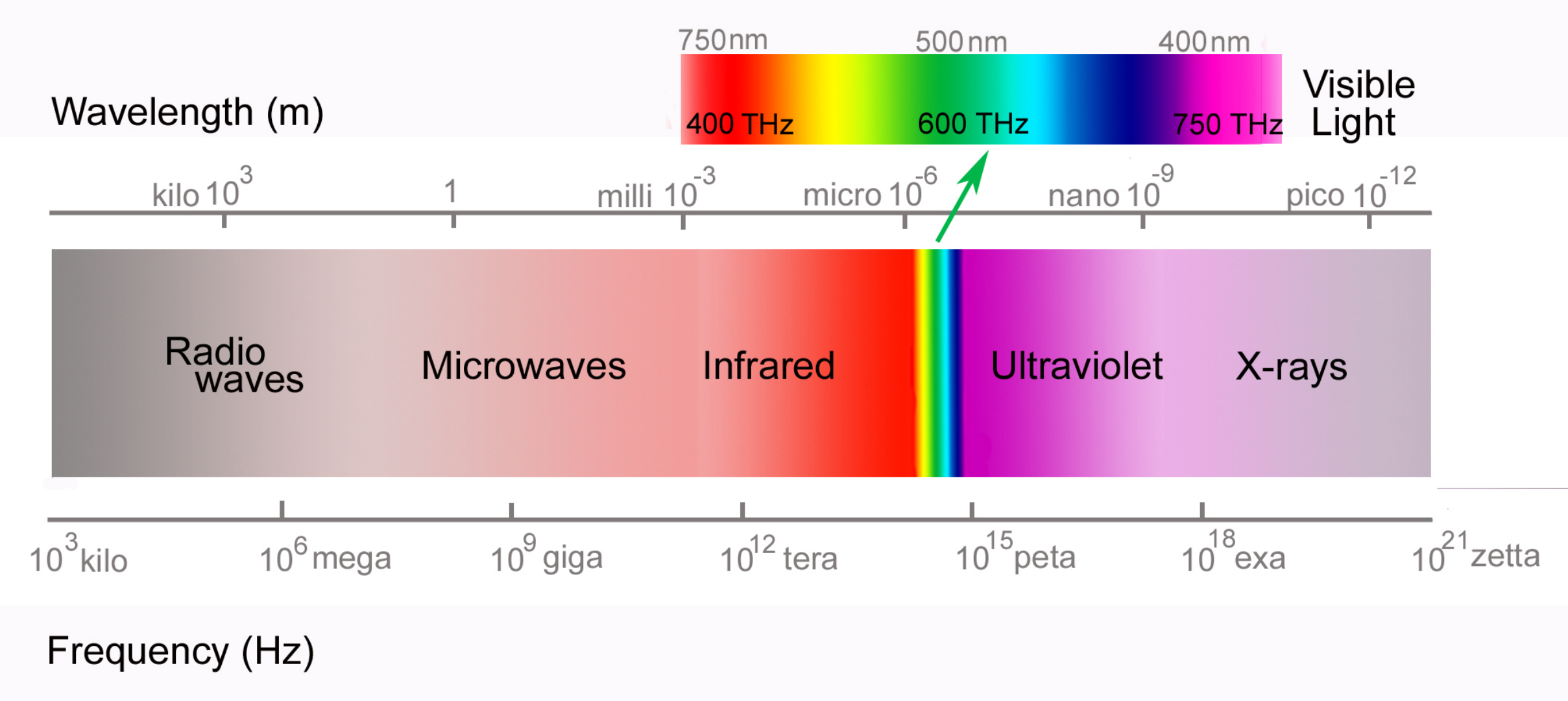


# The Electromagnetic Spectrum

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# The Electromagnetic Spectrum



# Measurement Scale – SI Units

## May 20, 2019 – Redefinition of the SI Units



Credit: ©BIPM

Hyperfine structure transition frequency cesium-133

Speed of light

Planck constant

Elementary charge

Boltzmann constant

Avogadro constant

Luminous efficacy of monochromatic radiation (540 THz)

$$\Delta\nu_{\text{Cs}} = 9192631770 \text{ s}^{-1}$$

$$c = 299792458 \text{ m}\cdot\text{s}^{-1}$$

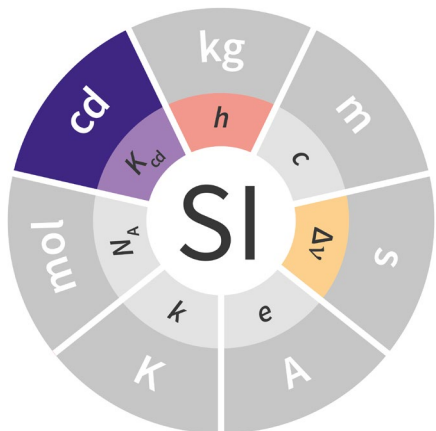
$$h = 6.62607015 \times 10^{-34} \text{ kg}\cdot\text{m}^2\cdot\text{s}^{-1}$$

$$e = 1.602176634 \times 10^{-19} \text{ A}\cdot\text{s}$$

$$k = 1.380649 \times 10^{-23} \text{ kg}\cdot\text{m}^2\cdot\text{K}^{-1}\cdot\text{s}^{-2}$$

$$N_{\text{A}} = 6.02214076 \times 10^{23} \text{ mol}^{-1}$$

$$K_{\text{cd}} = 683 \text{ cd}\cdot\text{sr}\cdot\text{s}^3\cdot\text{kg}^{-1}\cdot\text{m}^{-2}$$



Credit: ©BIPM

The candela, symbol cd, is the SI unit of luminous intensity in a given direction. It is defined by taking the fixed numerical value of the luminous efficacy of monochromatic radiation of frequency  $540 \times 10^{12}$  Hz,  $K_{\text{cd}}$ , to be 683 when expressed in the unit  $\text{lm}\cdot\text{W}^{-1}$ , which is equal to  $\text{cd}\cdot\text{sr}\cdot\text{W}^{-1}$ , or  $\text{cd}\cdot\text{sr}\cdot\text{kg}^{-1}\cdot\text{m}^{-2}\cdot\text{s}^3$ , where the kilogram, meter and second are defined in terms of  $h$ ,  $c$  and  $\Delta\nu_{\text{Cs}}$ .



Credit: Hans Michel/Courtesy BIPM

# Primary Source - Blackbody

## Plank's Law

$$L_b(\lambda) = \frac{2hc^2}{n^2\lambda^5} \frac{1}{\exp(hc/(n\lambda k_B T)) - 1}$$

$h$  = Planck's constant

$c$  = speed of light

$n(\lambda)$  = index of refraction of medium

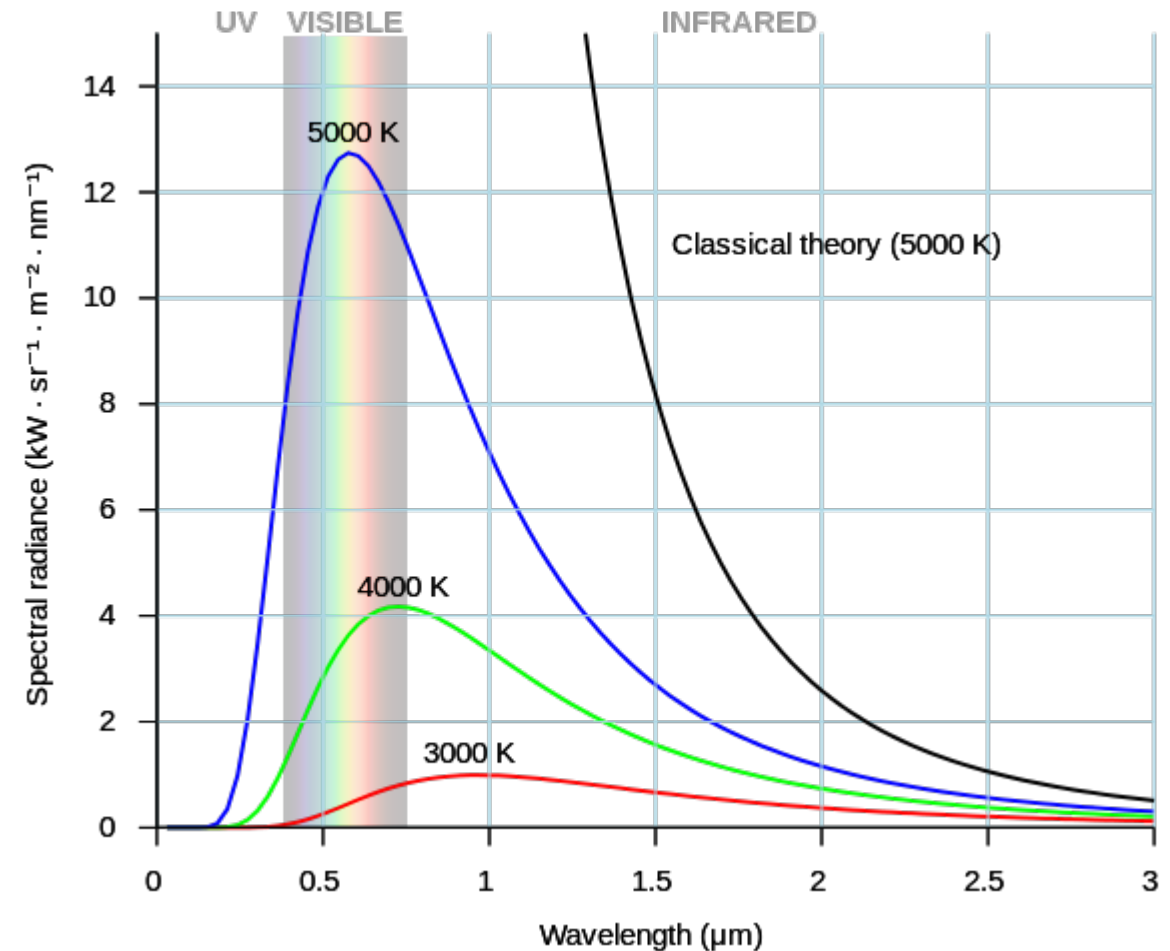
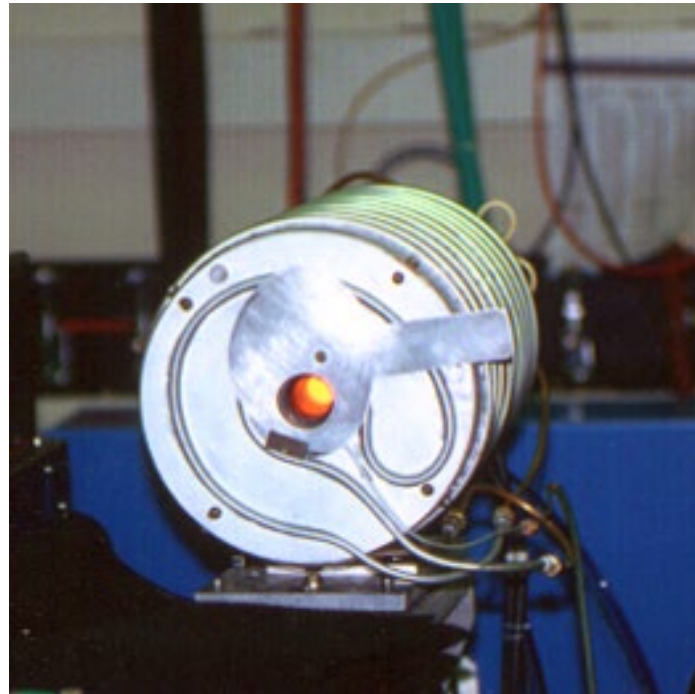
$k_B$  = Boltzmann's constant

$\lambda$  = wavelength of light

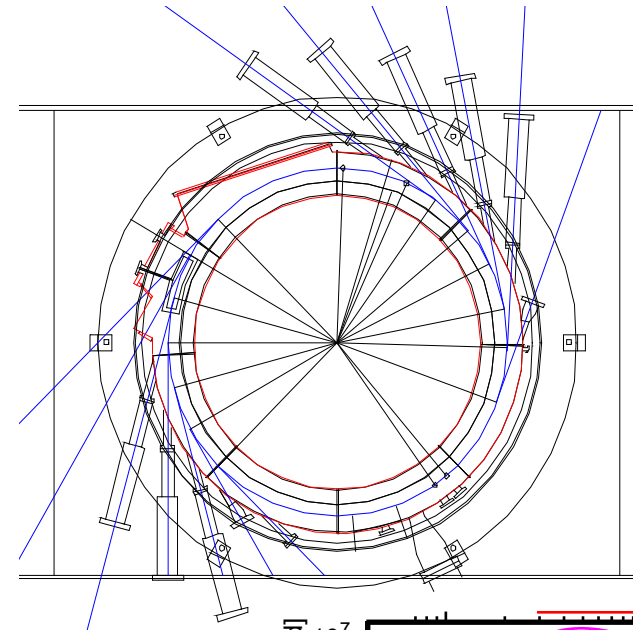
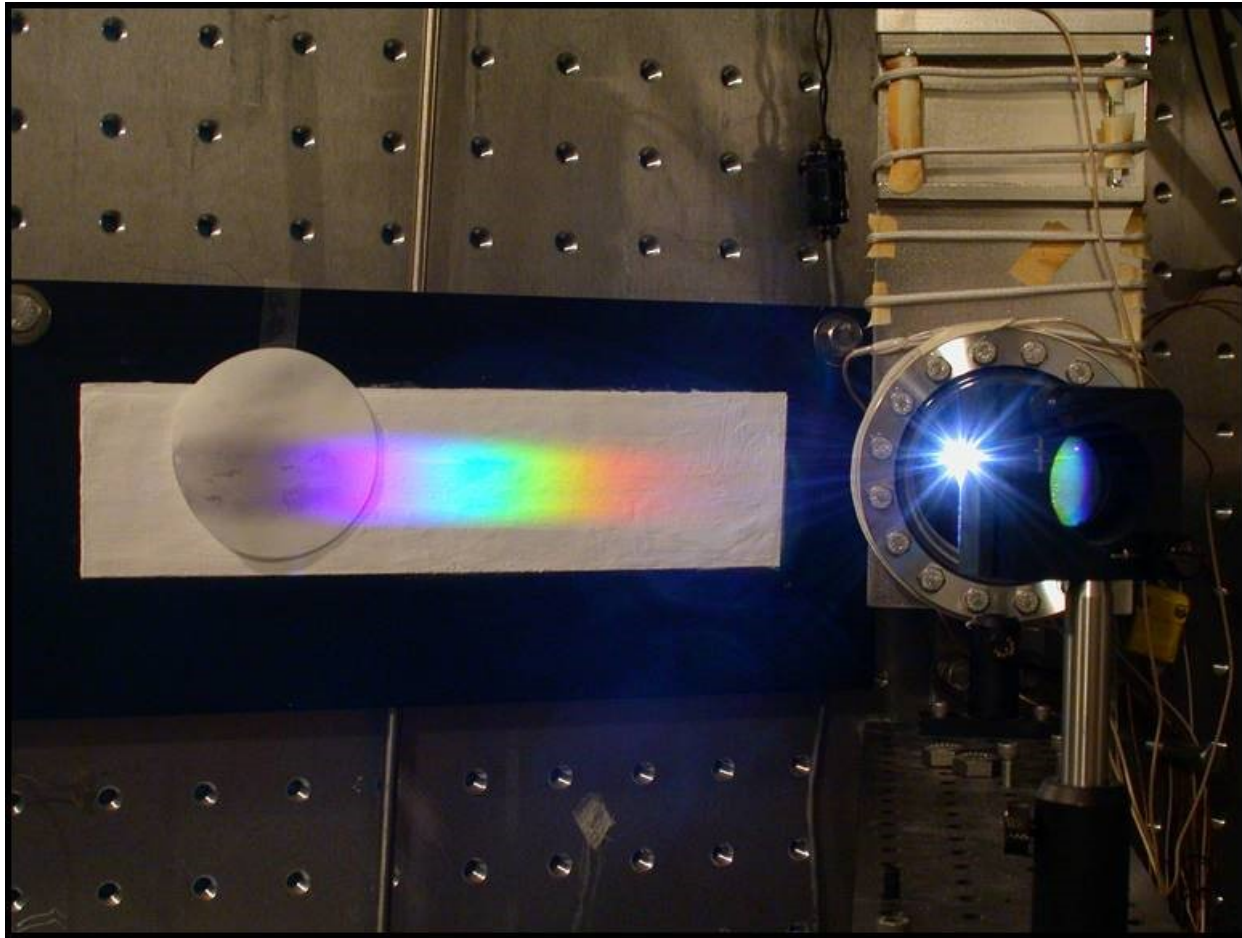
$T$  = temperature

Gold-point  
Blackbody

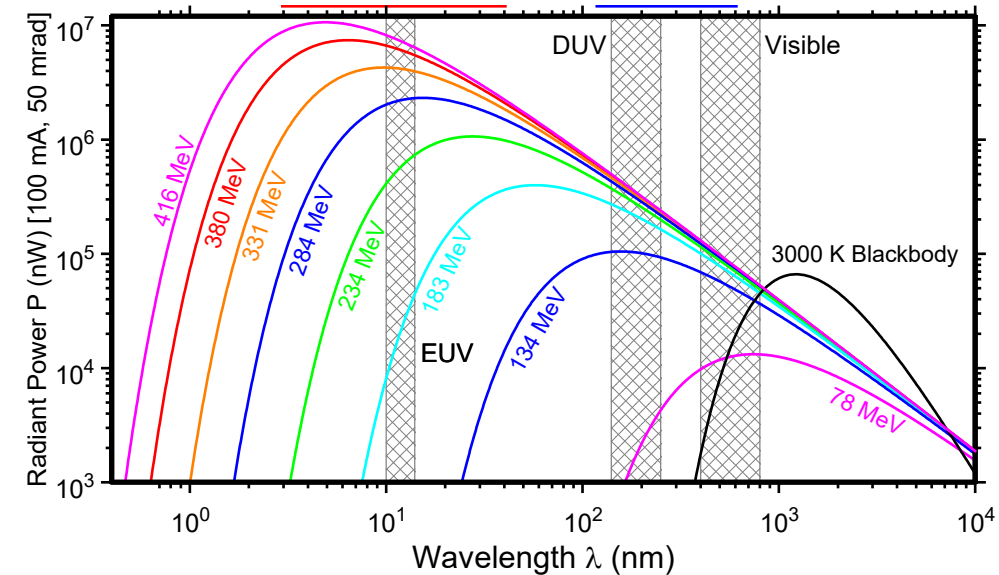
1337.33 K



# Primary Source - Synchrotron



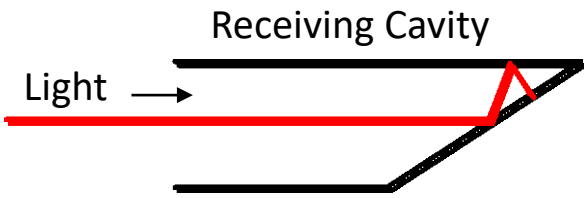
Source spectral radiance calculated - Schwinger equation  
Depends on Plank's & Boltzmann constants and speed of light



# Primary Detector – Cryogenic Radiometer

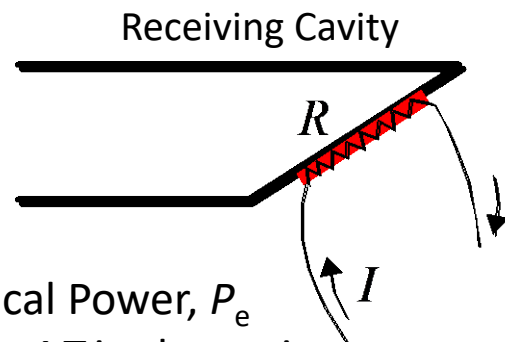
## Electrical Substitution Radiometer

Optical Heating



Optical Power,  $P_0$   
creates  $\Delta T$  in the cavity

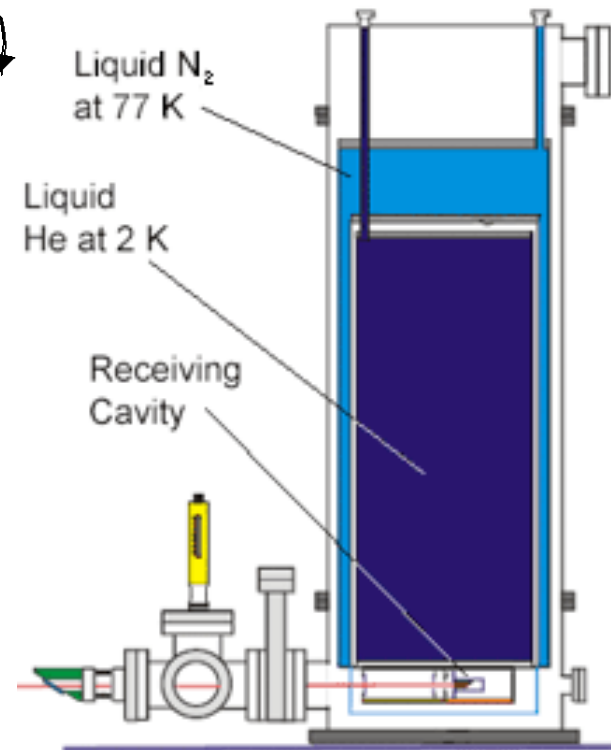
Electrical Heating



Electrical Power,  $P_e$   
creates  $\Delta T$  in the cavity

The same  $\Delta T$ . Thus,  $P_0 = P_e = I^2 R$

Optical Watt is measured based on the Electrical Watt.

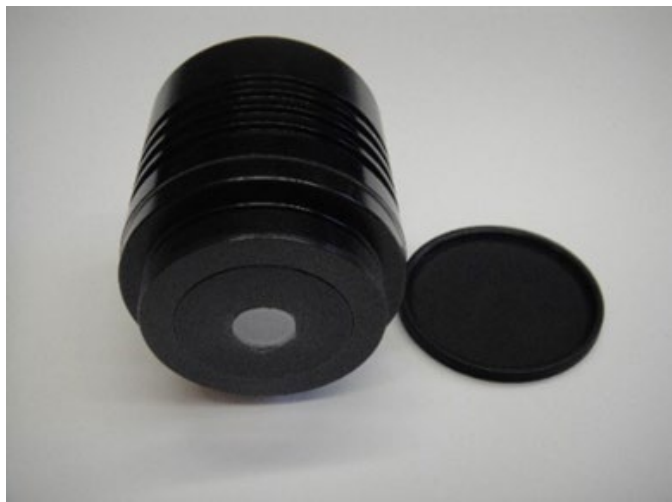


# Measurement Scale – Summary



Wavelength (nm)	Expanded Uncertainty (k=2) %
200	1.07
250	0.95
300	0.97
350	0.99
400	1.04

Wavelength (nm)	Expanded Uncertainty (k=2) %
250	1.74
350	1.27
450	0.91
555	0.77
900	0.57



Wavelength (nm)	Expanded Uncertainty (k=2) %
200	4.7
250	1.8
300	1.0
350	0.82
400	0.60

?

