



Automatically aligning crystal lattices to neutron diffraction instruments using reinforcement learning

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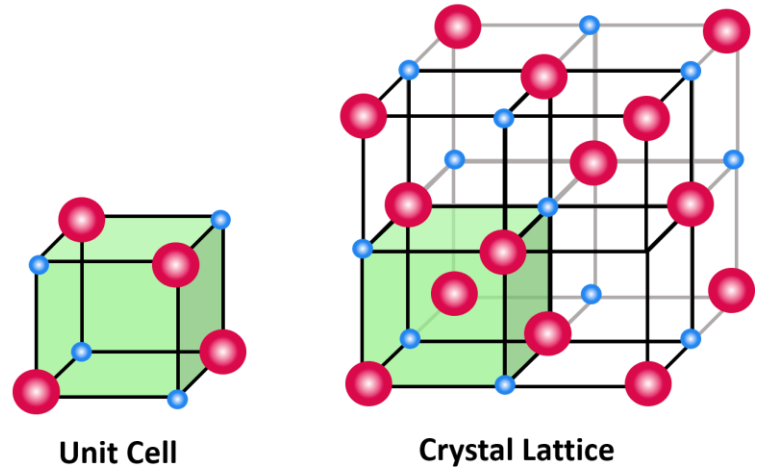
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Crystals

- A type of solid material composed of atoms or groups of atoms that are arranged in a three-dimensional pattern that is very ordered
- Lattice determines the different diffraction patterns

Crystal Lattice and Unit Cell



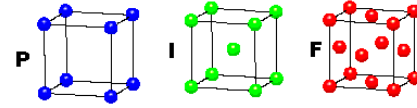
Bravais Lattice

- Symmetrical three-dimensional structural arrangements
- One of the 14 different types of unit cells that a crystal structure can be made up of
- Determines the different diffraction patterns

CUBIC

$$a = b = c$$

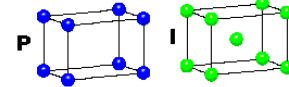
$$\alpha = \beta = \gamma = 90^\circ$$



TETRAGONAL

$$a = b \neq c$$

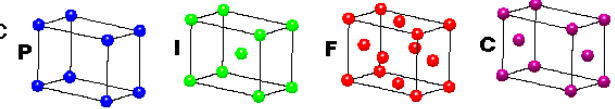
$$\alpha = \beta = \gamma = 90^\circ$$



ORTHORHOMBIC

$$a \neq b \neq c$$

$$\alpha = \beta = \gamma = 90^\circ$$

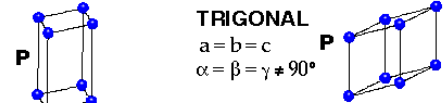


HEXAGONAL

$$a = b \neq c$$

$$\alpha = \beta = 90^\circ$$

$$\gamma = 120^\circ$$



TRIGONAL

$$a = b = c$$

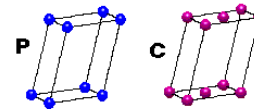
$$\alpha = \beta = \gamma \neq 90^\circ$$

MONOCLINIC

$$a \neq b \neq c$$

$$\alpha = \gamma = 90^\circ$$

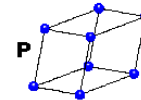
$$\beta \neq 120^\circ$$



TRICLINIC

$$a \neq b \neq c$$

$$\alpha \neq \beta \neq \gamma \neq 90^\circ$$

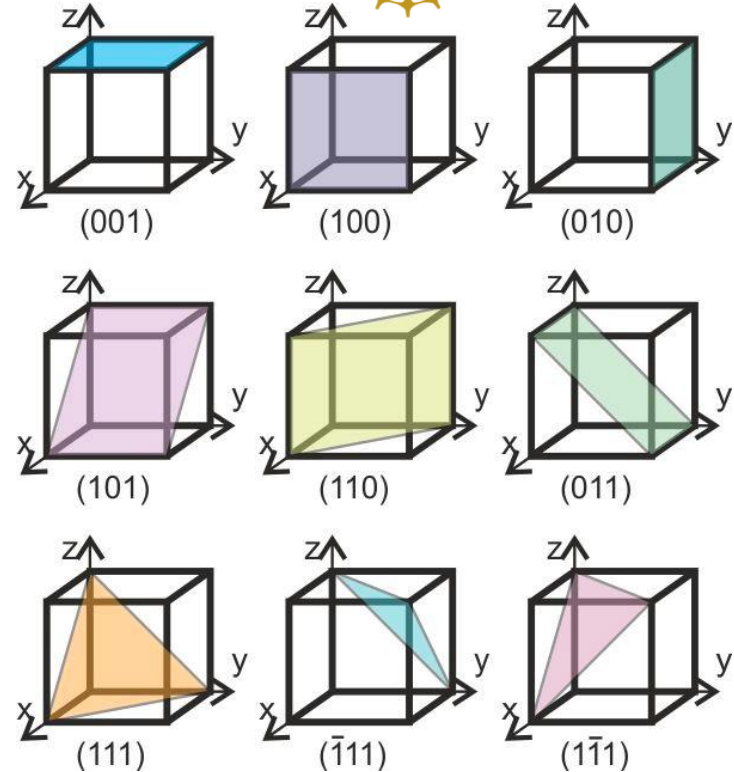


4 Types of Unit Cell
 P = Primitive
 I = Body-Centred
 F = Face-Centred
 C = Side-Centred
 +
7 Crystal Classes
 → **14 Bravais Lattices**

Crystallographic Planes

Miller Indices (HKL)

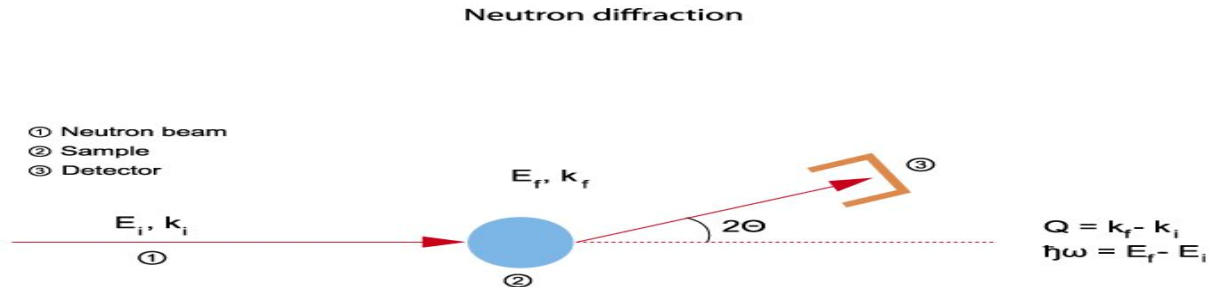
- Represent the orientation of crystallographic planes within the crystal lattice



https://www.researchgate.net/figure/Miller-indices-indicating-the-plane-perpendicular-to-the-vector-given-for-the-cubic_fig7_302838100

Neutron Diffraction

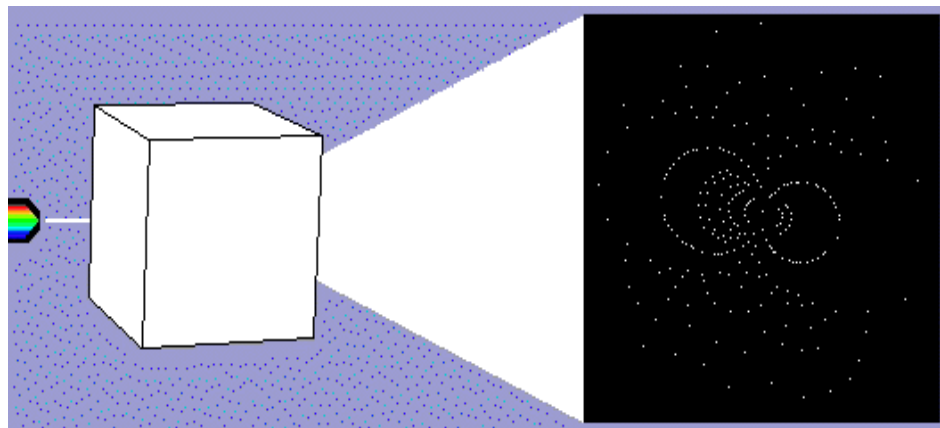
- Neutron Diffraction is the application of neutron scattering to determine the atomic and magnetic structure of a material
- A sample is placed in a beam of neutrons to obtain a diffraction pattern that provides information about the structure of the sample



<https://nmi3.eu/neutron-research/techniques-for-structural-research.html>

Objective

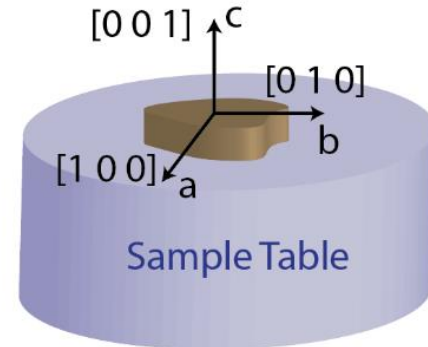
- Automatically align crystal structures to instruments
- Assist in fully automating the crystal diffraction process



<https://www.ill.eu/users/instruments/instruments-list/orientexpress/how-it-works/principle-of-neutron-laue-diffraction>

Alignment

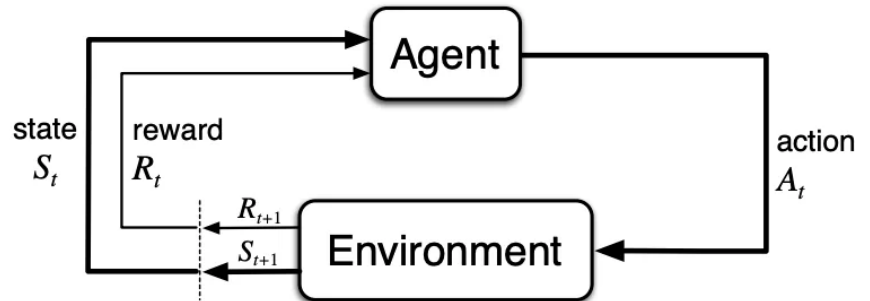
1. Choose a particular plane
2. Choose two projection vectors corresponding to the plane
3. Rotate table
4. Take alignment scans
5. Analyze scans
6. Repeat 3, 4, and 5 until aligned



Reinforcement Learning - Key Elements

Area of machine learning where agents take actions in an environment in order to maximize the notion of cumulative reward

- Agent
- Environment
- State
- Action
- Reward



<https://towardsdatascience.com/reinforcement-learning-101-e24b50e1d292>

A horizontal bar with a teal segment on the left and an orange segment on the right.

Reinforcement Learning - advantages

- Can be used to solve very complex problems
- Can outperform humans in many tasks
- It is similar to the learning of human beings and can correct errors during the training process
- It doesn't require large labeled datasets

A horizontal bar with a teal segment on the left and an orange segment on the right.

Reinforcement Learning - examples

- DeepMind
- AlphaFold
- AlphaGo



<https://venturebeat.com/ai/deepminds-big-losses-and-the-questions-around-running-an-ai-lab/>

Q-Learning

- Model-free reinforcement learning algorithm
- Q-table that stores the expected rewards for state-action pairs
- Q-values updated over multiple episodes
- Agent selects the action with the highest Q-value
- Effective for small state spaces
- Different from Value function

$$\text{New } Q(s, a) = Q(s, a) + \alpha [R(s, a) + \gamma \max_{a'} Q'(s', a') - Q(s, a)]$$

Learning Rate Discount Rate

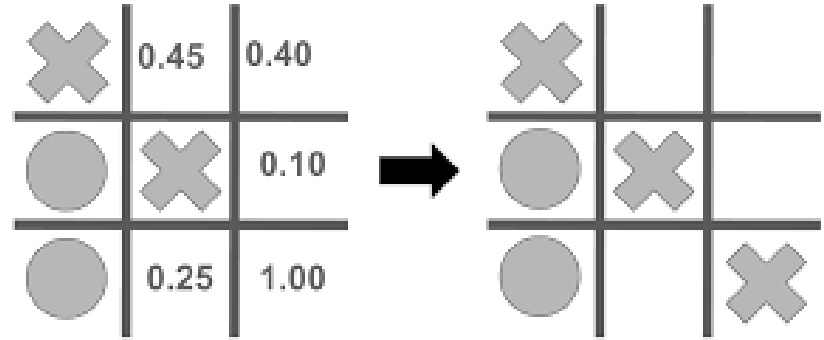
New Q value for the state and action Current Q values Reward for taking an action in a state Maximum expected future reward Current Q values

<https://towardsdatascience.com/a-beginners-guide-to-q-learning-c3e2a30a653c>

Q-learning with tic tac toe



```
# only when game ends
def giveReward(self):
    result = self.winner()
    # backpropagate reward
    if result == 1:
        self.p1.feedReward(1)
        self.p2.feedReward(0)
    elif result == -1:
        self.p1.feedReward(0)
        self.p2.feedReward(1)
    else:
        self.p1.feedReward(0.1)
        self.p2.feedReward(0.5)
```



<https://towardsdatascience.com/how-to-play-tic-tac-toe-using-reinforcement-learning-9604130e56f6>

```
value_max = -999
for p in positions:
    next_board = current_board.copy()
    next_board[p] = symbol
    next_boardHash = self.getHash(next_board)
    value = 0 if self.states_value.get(next_boardHash) is None else self.states_value.get(next_boardHash)
    # print("value", value)
    if value >= value_max:
        value_max = value
        action = p
# print("{} takes action {}".format(self.name, action))
return action
```

A horizontal bar with a teal segment on the left and an orange segment on the right.

Implementation

- Training:
 - Reward
 - Punished for each rotation
 - Awarded for finding peak
- Decides how much to rotate
- Rotates automatically until finds diffraction peak

Hyperparameters

- Values that control the learning process
- Learning rate, discount factor, episodes

Parameter	Value
Discount factor γ	0.9
Critic net learning rate α_{critic}	0.001
Actor net learning rate α_{actor}	0.001
Batch size N	64
Soft update rate τ	0.01
Standard deviation of Gaussian noise	0.3
Maximum number of training episodes e_{max}	1000
Control time step dt	0.01 s
Maximum time step in an episode t_{max}	5 s
Reward function parameter a_1	1.0
Reward function parameter δ_1	0.01
Reward function parameter ρ_1	π
Reward function parameter a_2	0.1
Reward function parameter δ_2	0.1
Reward function parameter ρ_2	2π

4.2.3. CMA-ES Training Detail in the Simulation Environment

<https://www.researchgate.net/publication/343594992/figure/fig/AS:932830192341025@1599415457664/Reinforcement-learning-RL-training-hyper-parameters.png>



Why/How

Why

- automate some of the crystallography process
- significant because correct alignment is necessary

How

1. Build the q learning algorithm
2. Train the algorithm using simulated data
3. Evaluate/test the algorithm
4. Tune hyperparameters if needed
5. Evaluate again

Results

```
Episode 1: Number of Rotations = 114
Episode 2: Number of Rotations = 138
Episode 3: Number of Rotations = 87
Episode 4: Number of Rotations = 61
Episode 5: Number of Rotations = 12
Episode 6: Number of Rotations = 39
Episode 7: Number of Rotations = 28
Episode 8: Number of Rotations = 31
Episode 9: Number of Rotations = 39
Episode 10: Number of Rotations = 14
Episode 11: Number of Rotations = 83
Episode 12: Number of Rotations = 1
Episode 13: Number of Rotations = 8
Episode 14: Number of Rotations = 38
Episode 15: Number of Rotations = 54
Episode 16: Number of Rotations = 29
Episode 17: Number of Rotations = 6
Episode 18: Number of Rotations = 4
Episode 19: Number of Rotations = 69
Episode 20: Number of Rotations = 10
Episode 21: Number of Rotations = 2
Episode 22: Number of Rotations = 13
Episode 23: Number of Rotations = 35
Episode 24: Number of Rotations = 3
Episode 25: Number of Rotations = 36
Episode 26: Number of Rotations = 16
Episode 27: Number of Rotations = 4
Episode 28: Number of Rotations = 33
Episode 29: Number of Rotations = 145
Episode 30: Number of Rotations = 24
Episode 31: Number of Rotations = 7
Episode 32: Number of Rotations = 3
Episode 33: Number of Rotations = 1
Episode 34: Number of Rotations = 1
Episode 35: Number of Rotations = 1
Episode 36: Number of Rotations = 17
Episode 37: Number of Rotations = 18
Episode 38: Number of Rotations = 12
```

```
Episode 964: Number of Rotations = 9
Episode 965: Number of Rotations = 3
Episode 966: Number of Rotations = 1
Episode 967: Number of Rotations = 5
Episode 968: Number of Rotations = 5
Episode 969: Number of Rotations = 6
Episode 970: Number of Rotations = 2
Episode 971: Number of Rotations = 4
Episode 972: Number of Rotations = 4
Episode 973: Number of Rotations = 2
Episode 974: Number of Rotations = 1
Episode 975: Number of Rotations = 4
Episode 976: Number of Rotations = 2
Episode 977: Number of Rotations = 4
Episode 978: Number of Rotations = 6
Episode 979: Number of Rotations = 1
Episode 980: Number of Rotations = 3
Episode 981: Number of Rotations = 1
Episode 982: Number of Rotations = 2
Episode 983: Number of Rotations = 7
Episode 984: Number of Rotations = 6
Episode 985: Number of Rotations = 6
Episode 986: Number of Rotations = 6
Episode 987: Number of Rotations = 3
Episode 988: Number of Rotations = 4
Episode 989: Number of Rotations = 8
Episode 990: Number of Rotations = 2
Episode 991: Number of Rotations = 1
Episode 992: Number of Rotations = 6
Episode 993: Number of Rotations = 2
Episode 994: Number of Rotations = 4
Episode 995: Number of Rotations = 1
Episode 996: Number of Rotations = 4
Episode 997: Number of Rotations = 3
Episode 998: Number of Rotations = 3
Episode 999: Number of Rotations = 1
Episode 1000: Number of Rotations = 2
```



What's Next

- Mcstas needs to be implemented
- Implement into different types of instruments such as triple-axis spectrometer



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Acknowledgements

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