

# Molecular Dynamics Study of the Conformational Properties of Polymers in an Explicit Solvent and the Identification of the $\theta$ -Temperature

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**NIST**  
National Institute of  
Standards and Technology  
U.S. Department of Commerce



**MATERIAL  
MEASUREMENT  
LABORATORY**

# POLYMERS

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Large molecule/macromolecule composed of repeating subunits called monomers



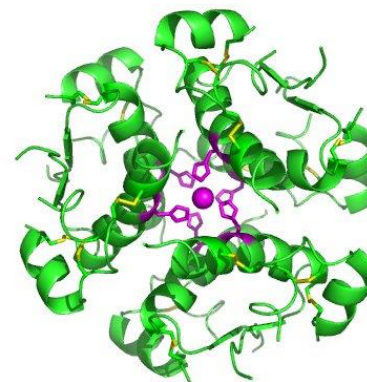
Polystyrene(Styrofoam)

Image from:  
<https://www.theodysseyonline.com/new-year-no-more-styrofoam>



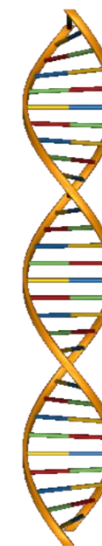
Polyisoprene(rubber)

Image from:  
<https://www.tirerack.com/content/tirerack/desktop/en/homepage.html>



Insulin Hexamer

Image from:  
<https://en.wikipedia.org/wiki/Insulin>

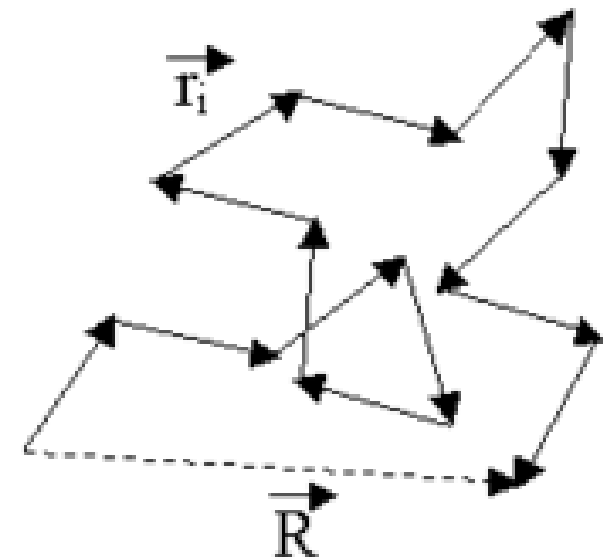


DNA

Image from:  
<http://exchange.smarttech.com/search.html?q=%22DNA%20structure%22>

# POLYMER MODELS

- Ideal Chain:
  - Modeled after a random walk model (no attractions, no repulsions)
- “Real Chain”:
  - Incorporates interactions between all segments
  - Includes a repulsive excluded volume interaction and an attractive component that allows us to account for the quality of the solvent



A typical ideal chain

[https://en.wikipedia.org/wiki/Ideal\\_chain](https://en.wikipedia.org/wiki/Ideal_chain)

# FLORY THEORY/SCALING LAW

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$$R_g \sim N^\nu$$

$$R_g^2 = \frac{1}{N} \sum_{k=1}^n (r_k - r_{mean})^2$$

$R_g$  is the radius of gyration of the polymer

$N$  is the degree of polymerization (# of segments)

$\nu$  is the Flory exponent

For a good solvent,  $\nu \approx 3/5$

For the  $\theta$ -solvent,  $\nu \approx 1/2$

For a poor solvent,  $\nu \approx 1/3$

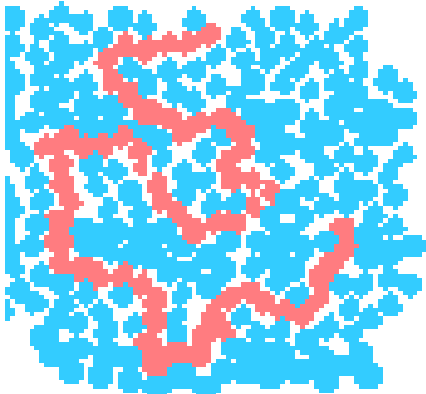
**Solvent quality depends on chemistry and temperature**

# SOLVENT QUALITY

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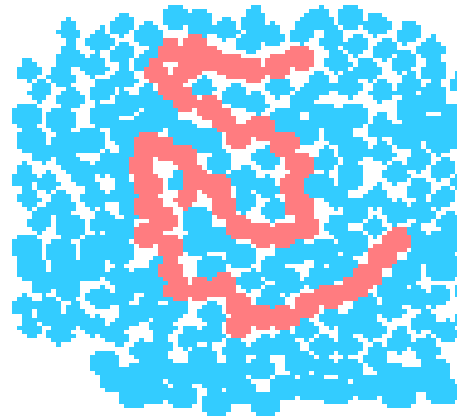
- **“Good solvent”:**

- Monomers prefer to interact with the solvent particles rather than with other monomers
- Repulsive interactions dominate
- Polymer swells



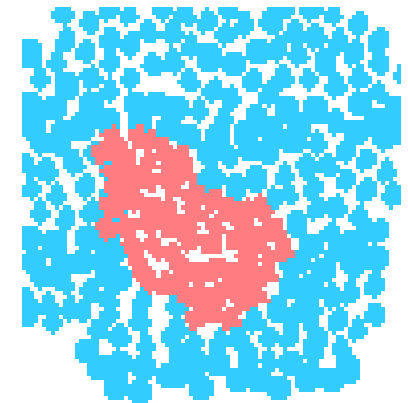
- **“ $\theta$ -solvent”:**

- Attractive and repulsive interactions are equal
- Polymer behaves as if it's an ideal chain



- **“Poor solvent”**

- Monomers prefer to interact with other monomers rather than with solvent particles
- Attractive forces dominate
- Polymer contracts and behaves more as a hard sphere



Images from: <http://rkt.chem.ox.ac.uk/lectures/pol.html>

# OBJECTIVES

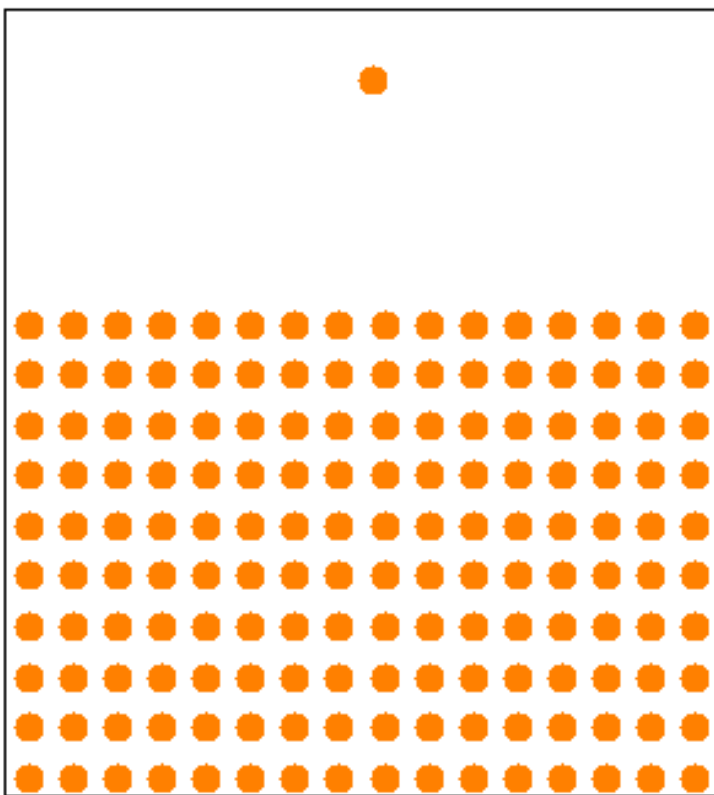
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- Develop a model that can identify the  $\theta$ -temperature of a polymer solution
- Use molecular dynamics to simulate polymers of varying chemistries and molecular architectures in an explicit solvent

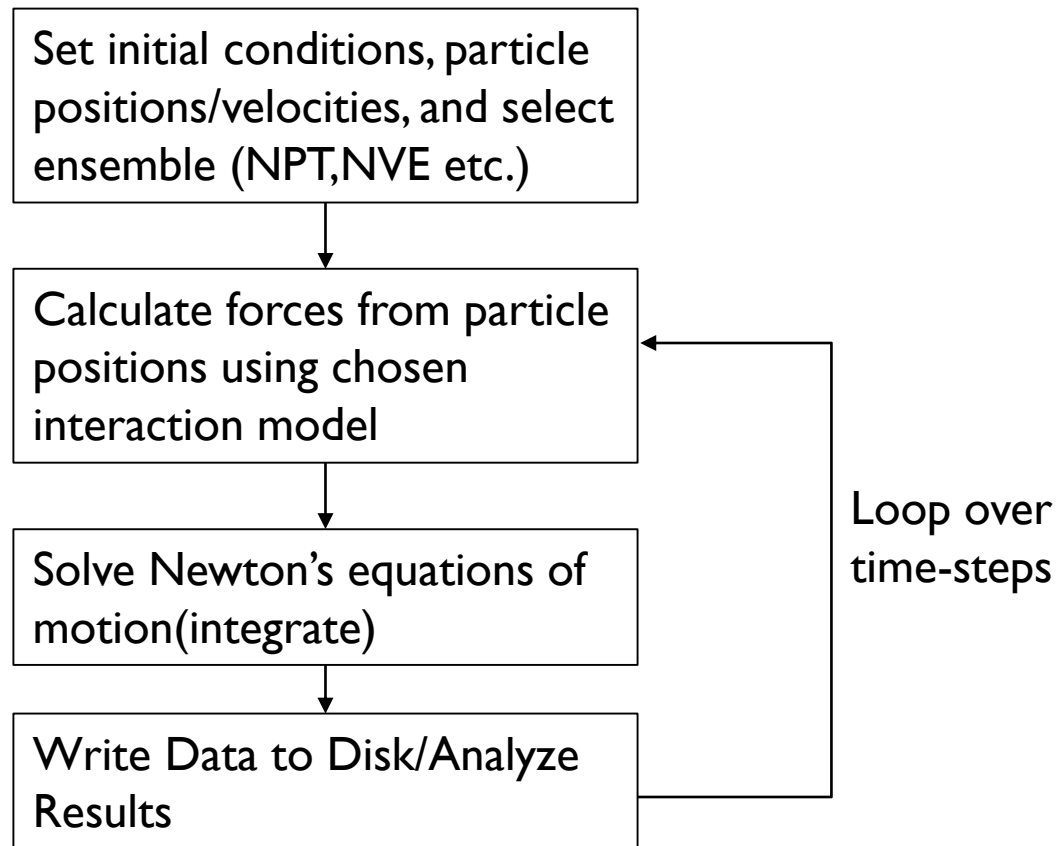


# MOLECULAR DYNAMICS SIMULATIONS

time 0.0041 ps



Animation from  
[https://en.wikipedia.org/wiki/Molecular\\_dynamics](https://en.wikipedia.org/wiki/Molecular_dynamics)



# IMPLICIT SOLVATION WORK

- Implicit solvation work on this topic has been done by Steinhauser M.O. In J. Chem. Phys. 122(2005) on flexible linear polymer chains of varying molecular masses
- Used a coarse grained bead-spring model that introduced a dimensionless parameter  $\lambda$  which determines the depth of the intermolecular potential
- Larger  $\lambda$ =greater attractive forces between segments
- The overall intermolecular potential has the form

$$V_{inter}(r) = \begin{cases} V_{WCA}(r) - \lambda\epsilon, & 0 < r < 2^{1/6}\sigma \\ \lambda V_{cos}(r), & 2^{1/6} \leq r < r_{cut} \\ 0 & else \end{cases}$$

$$V_{WCA}(r) = 4\epsilon \left\{ \left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^6 \right\} + \epsilon$$

$$V_{cos}(r) = \left[ \frac{1}{2} \cos(\alpha r^2 + \beta) + 0.5 \right] \epsilon$$

Where  $\alpha$  and  $\beta$  are parameters that fit the cosine curve to smoothly approach 0 at the cutoff

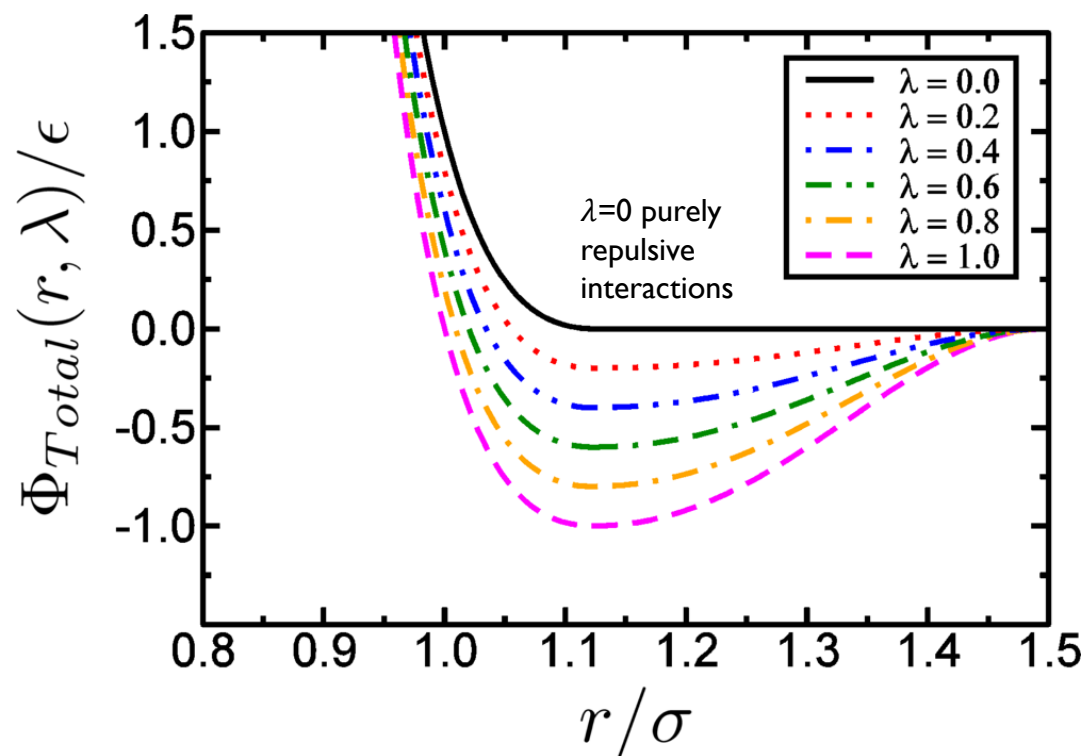


Image from:  
Steinhauser M.O.  
*Int. J. Mol. Sci.* 2009, 10(12)

Steinhauser M.O.J.  
*Chem. Phys*  
122(2005)



# IMPLICIT SOLVATION WORK

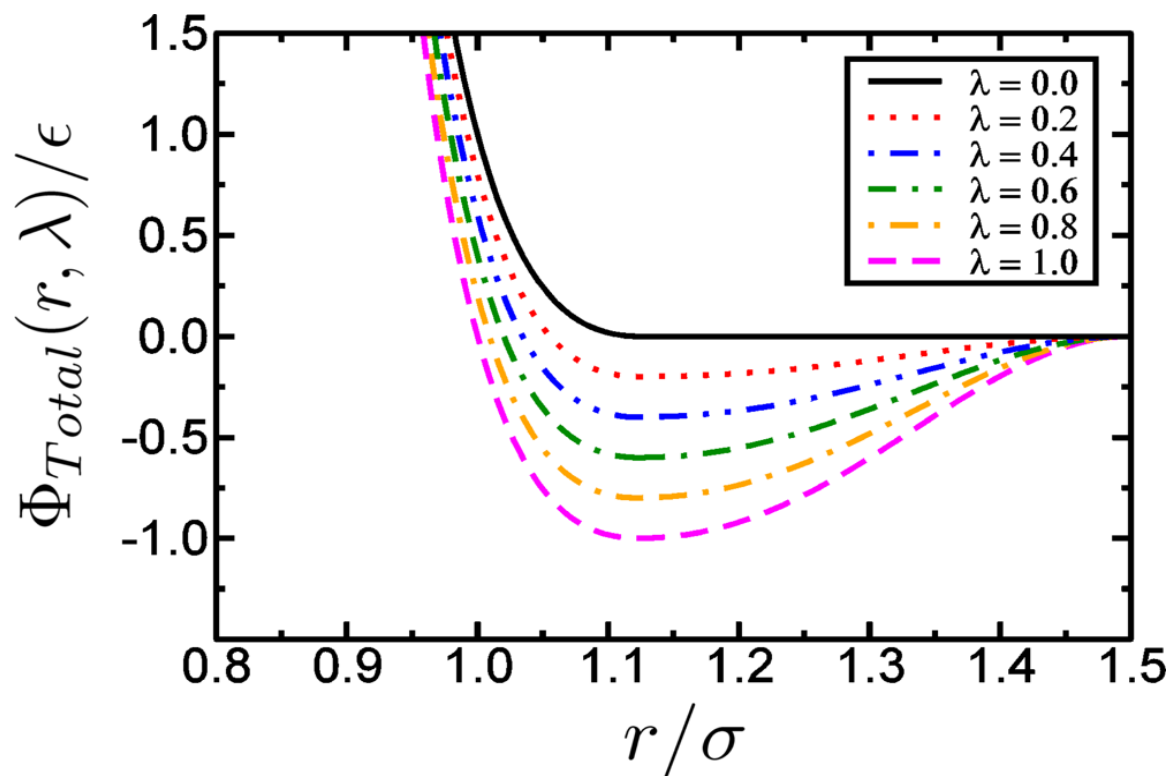
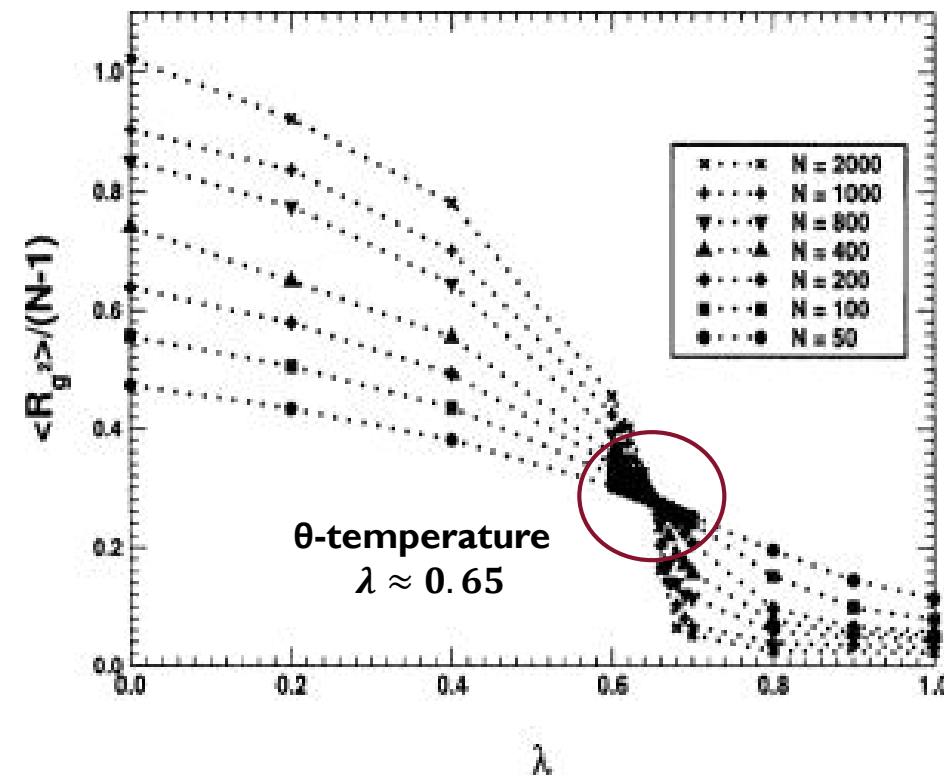


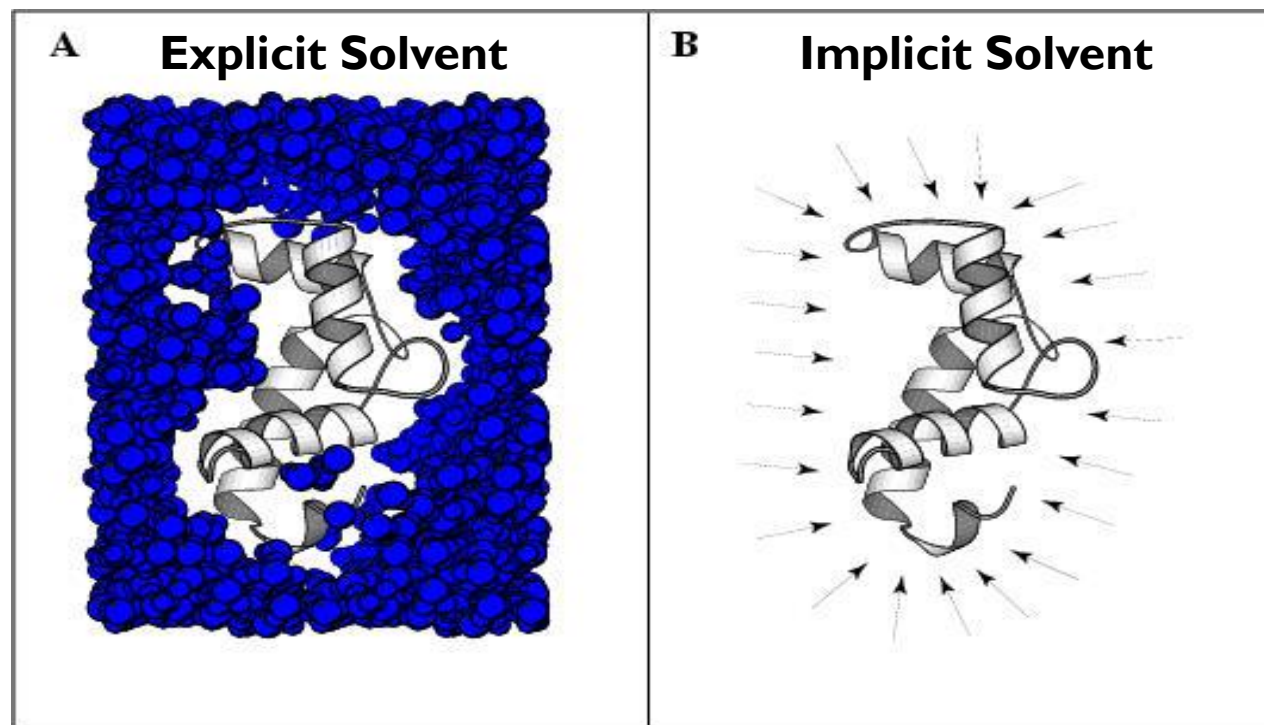
Image from: Steinhauser M.O. *Int. J. Mol. Sci.* 2009, 10(12)



Steinhauser M.O. *J. Chem. Phys.* 122(2005)

# WHY USE AN EXPLICIT SOLVENT?

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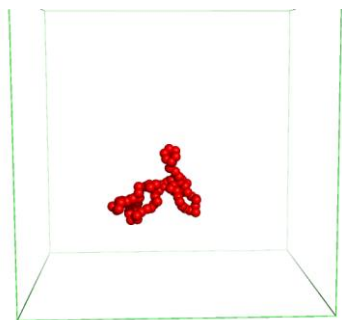


- Provides a more realistic and detailed full-atom description of the system
- Essential to reproduce certain properties of solute molecules
  - Reaction kinetics
  - Dynamics
- Computationally expensive... but worth it

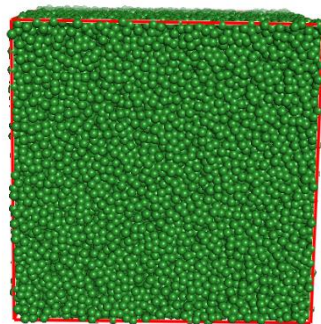
Image from: <http://csb.stanford.edu/~koehl/ProShape/born.php>

# SIMULATION DETAILS

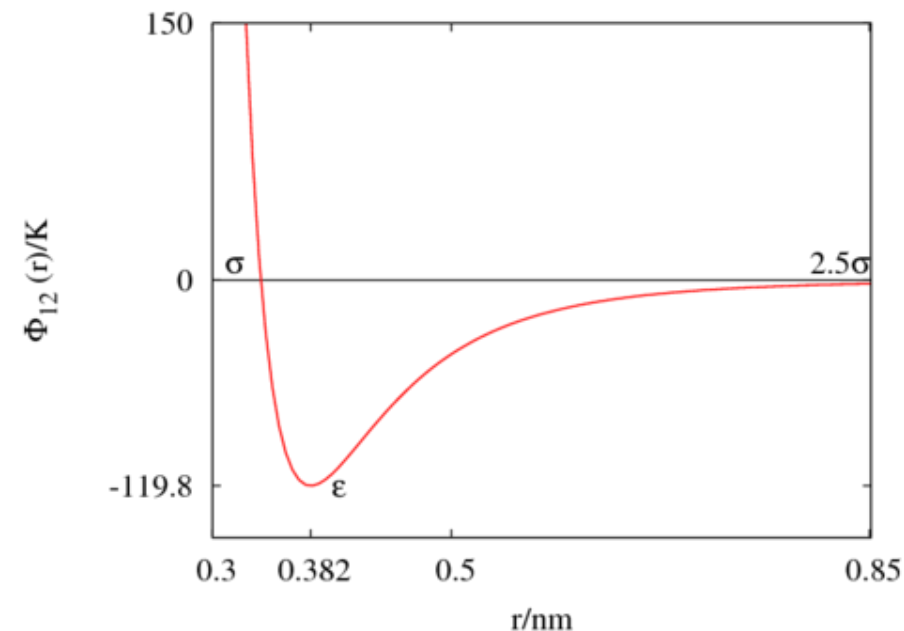
- Used a coarse grained bead model with an explicit solvent to try and determine the  $\theta$ -temperature of various polymers of different molecular architectures and chemistries
- NPT Ensemble
- The Lennard Jones Potential was used with a cutoff of  $2.5\sigma$
- Used ZENO numerical path integration software to obtain conformational properties of the generated polymer chains (radius of gyration, hydrodynamic radius, etc)



Polymer chain with 41 monomers



72000 solvent particles + polymer



$$V_{LJ}(r) = 4\epsilon \left\{ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6 \right\}$$

Image from: [http://www.sklogwiki.org/SklogWiki/index.php/Lennard-Jones\\_model](http://www.sklogwiki.org/SklogWiki/index.php/Lennard-Jones_model)

# SYSTEMS STUDIED

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Molecular Mass: 41,81,161,321

Temperature=0.5,0.7,0.9

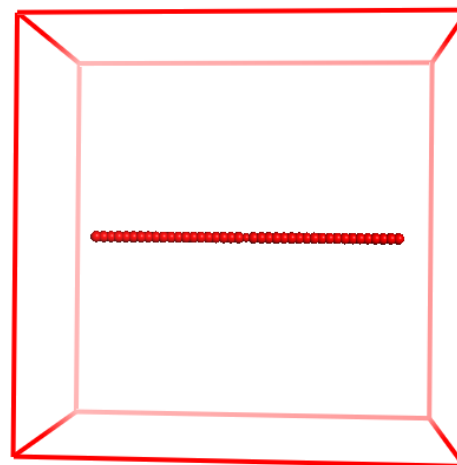
$\epsilon_{pp}$  for polymer-polymer interactions: 1.0

$\epsilon_{ss}$  for solvent-solvent interactions: 1.0

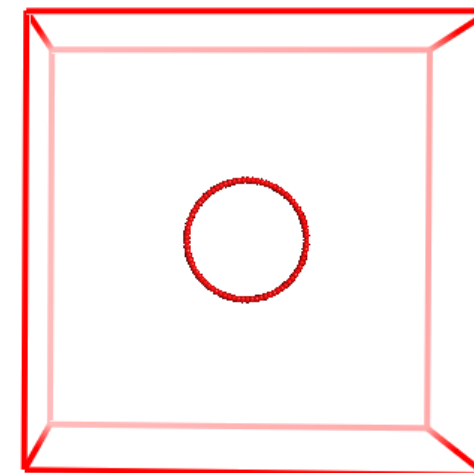
$\epsilon_{sp}$  cross interactions: Modified Lorentz Berthelot mixing rule

$$\epsilon_{sp} = \sqrt{\epsilon_{pp} * \epsilon_{ss}} (1 - \alpha)$$

$\alpha=.0, \alpha=.02, \alpha=.04, \alpha=.06, \alpha=.08, \alpha=.1, \alpha=.12, \alpha=.14, \alpha=.16,$



Linear Chain



Ring Polymer

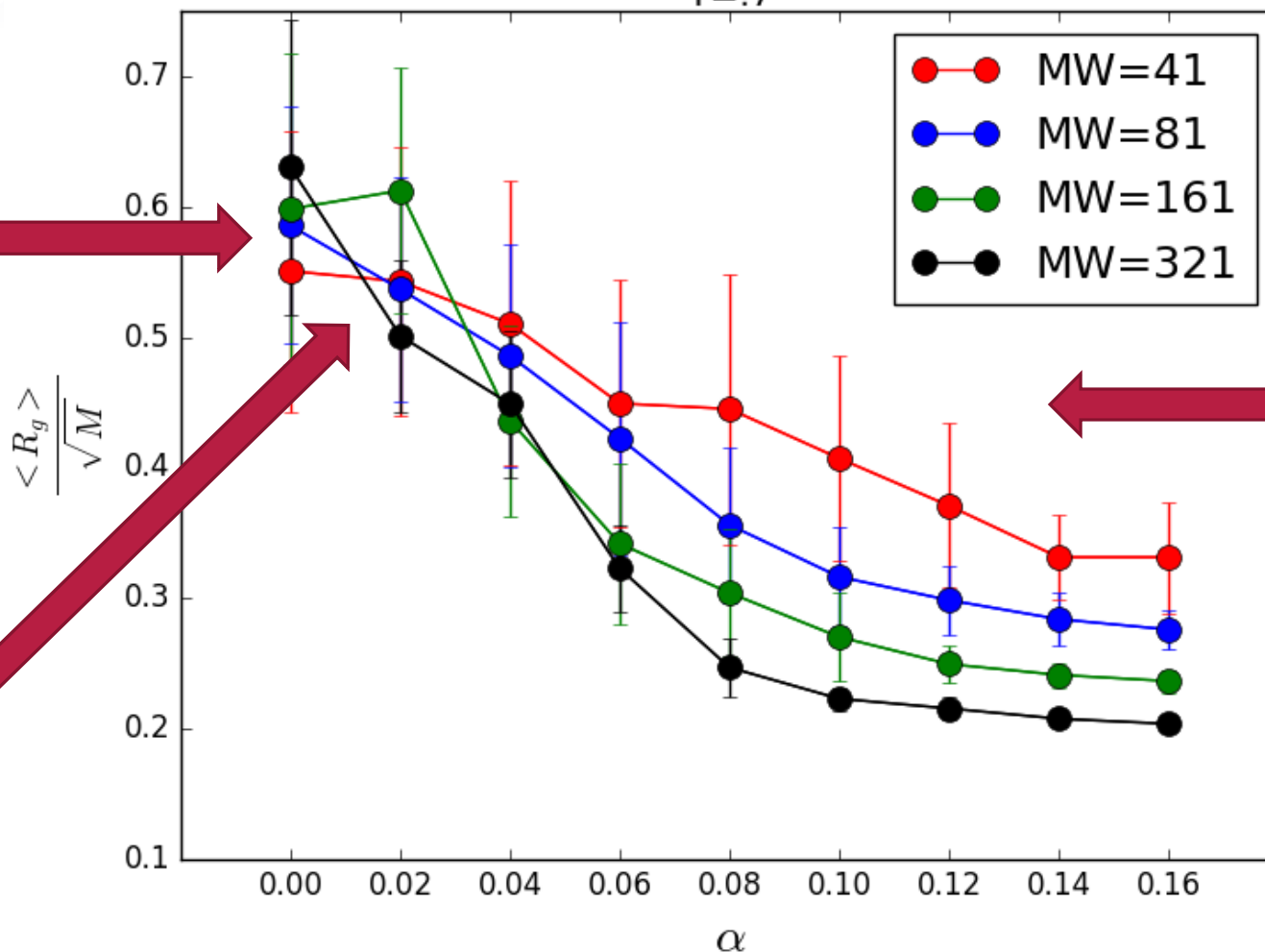
# WHAT SHOULD OUR MIXING RULE BE?

Mixing Rule Dependence of  $\langle R_g \rangle$  for Linear Chains

$T=.7$

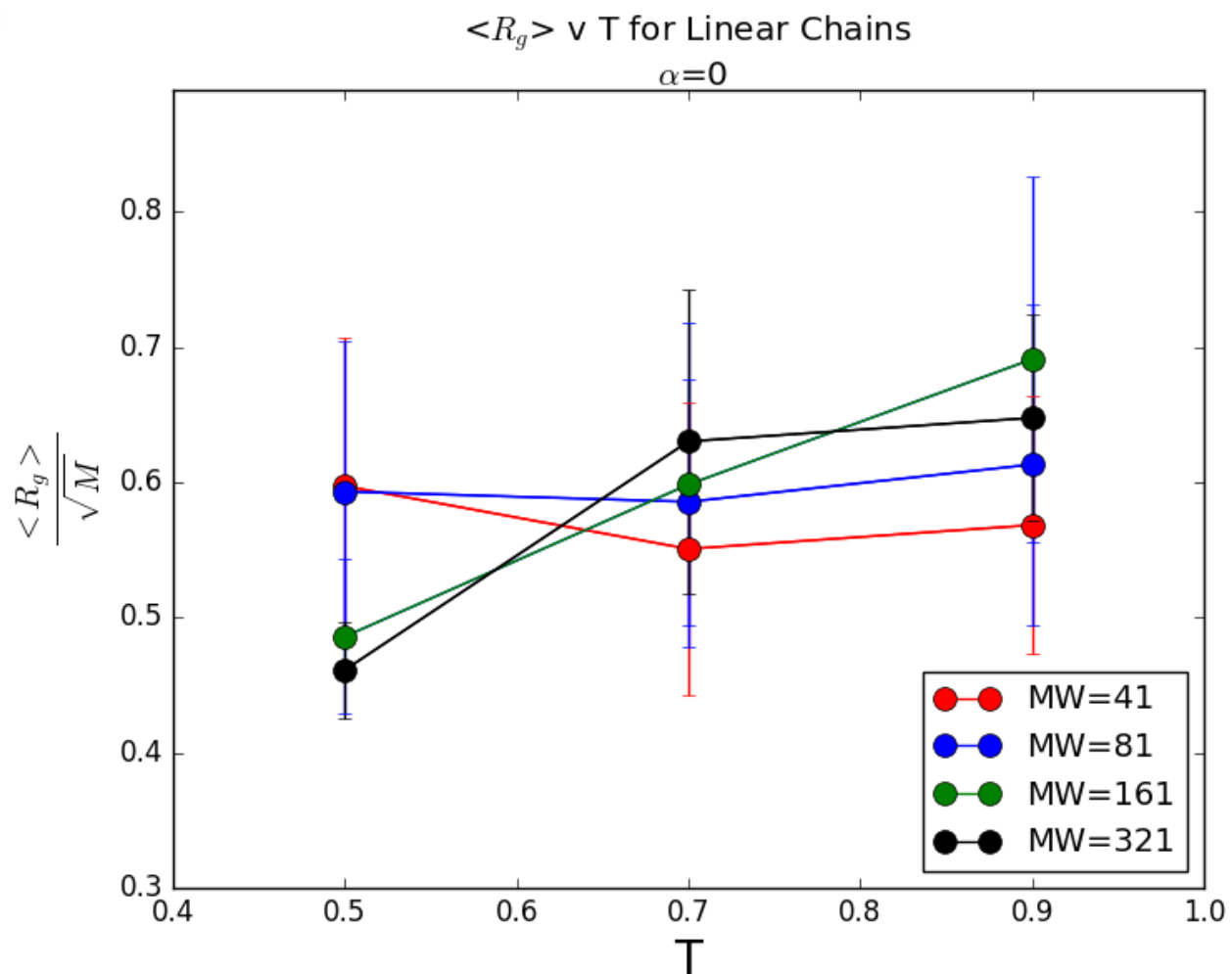
$\alpha=0$   
Swollen Region  
Good solvent  
conditions

$0.02 < \alpha < 0.04$   
Intermediate Region  
 $R_g$  is sensitive to  
changes in temperature

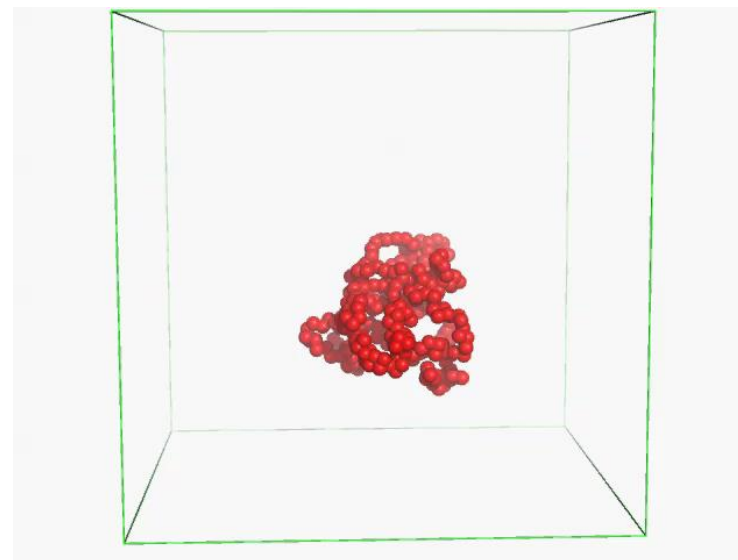


$\alpha \geq 0.06$   
Collapsed Region  
Always poor solvent  
conditions

# SWOLLEN REGION-LINEAR



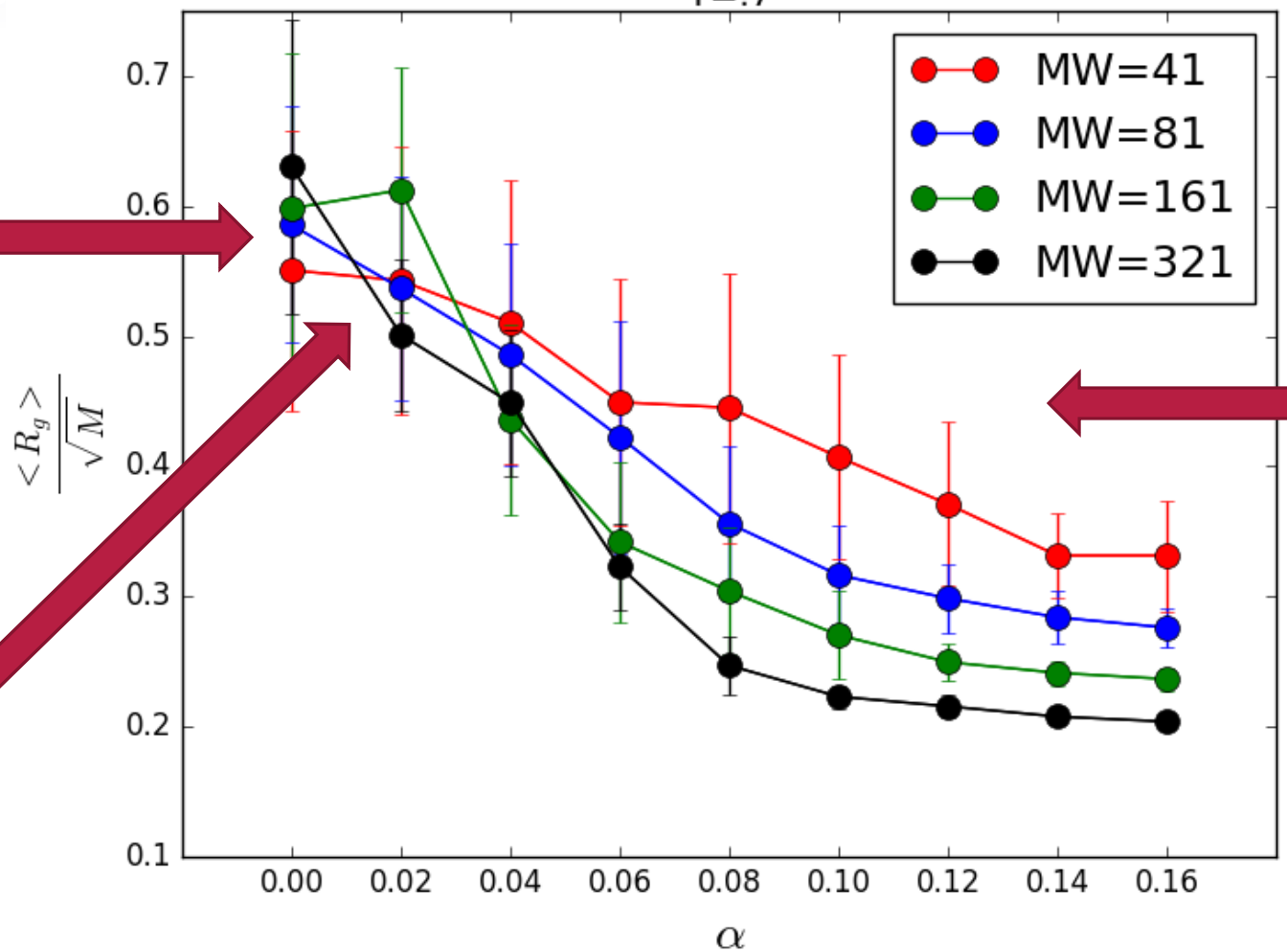
- $\alpha=0$
- No clear trend between  $\langle R_g \rangle$  and temperature, difficult to identify  $\theta$ -temperature
- Chains are more swollen, cross interactions too attractive (good solvent conditions)
- Cannot naively choose mixing rule





### Mixing Rule Dependence of $\langle R_g \rangle$ for Linear Chains

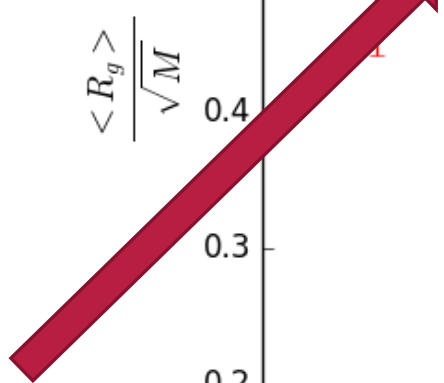
$T=.7$



$\alpha=0$   
Swollen Region  
Good solvent  
conditions



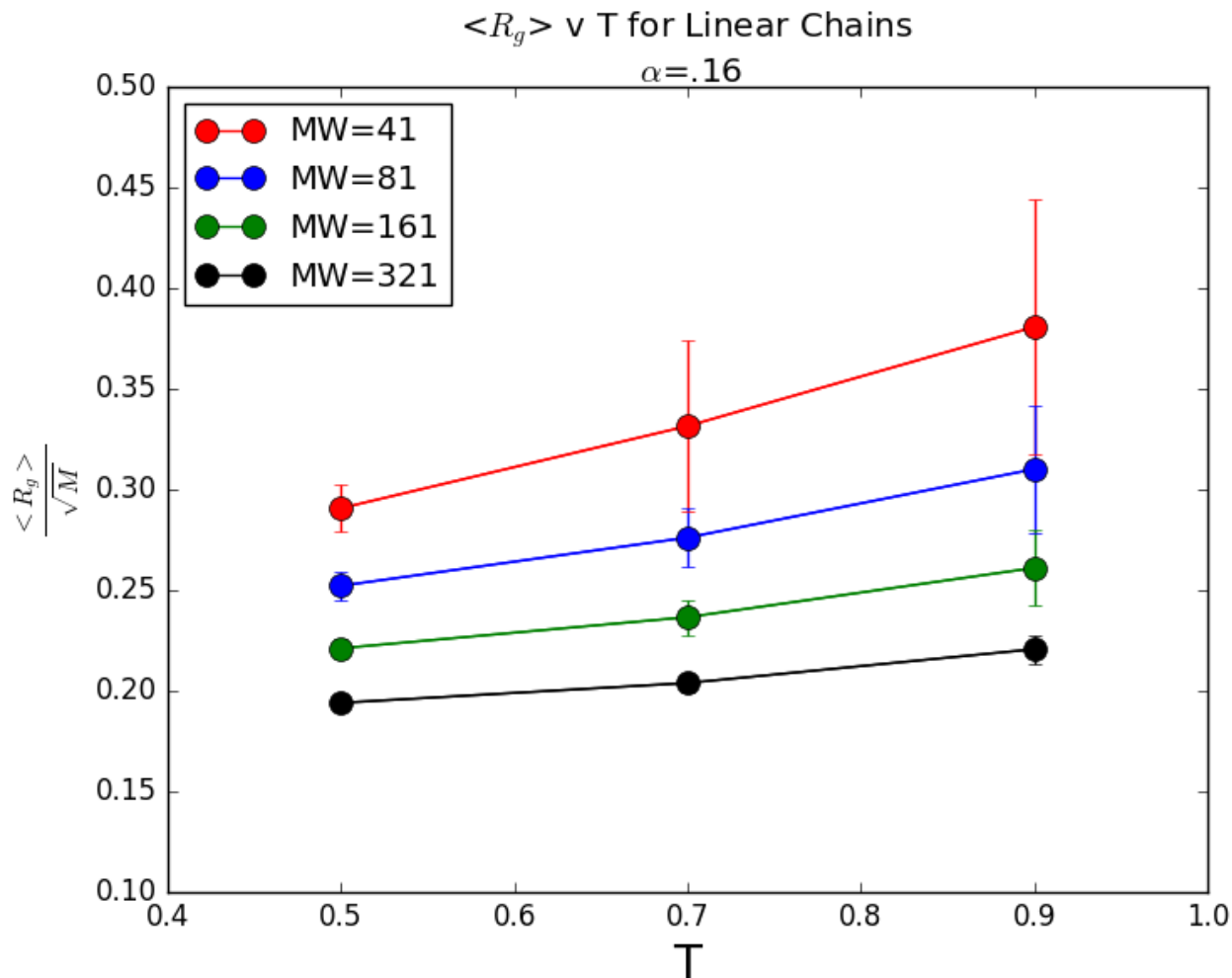
$0.02 < \alpha < 0.04$   
Intermediate Region  
 $\langle R_g \rangle$  is sensitive to  
changes in temperature



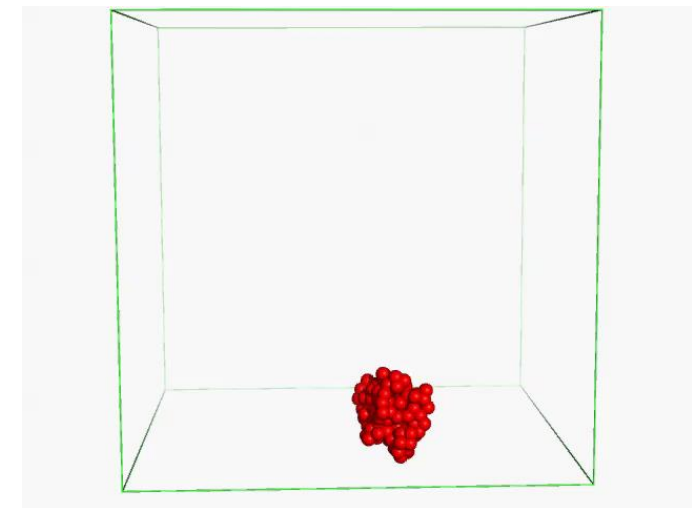
$\alpha \geq 0.06$   
Collapsed Region  
Always poor solvent  
conditions



# COLLAPSED REGION-LINEAR



- $\alpha \geq 0.06$
- Chain is always collapsed, cross interactions too repulsive (bad solvent conditions)
- Desired behavior was not achieved for these simulations, no crossover occurs



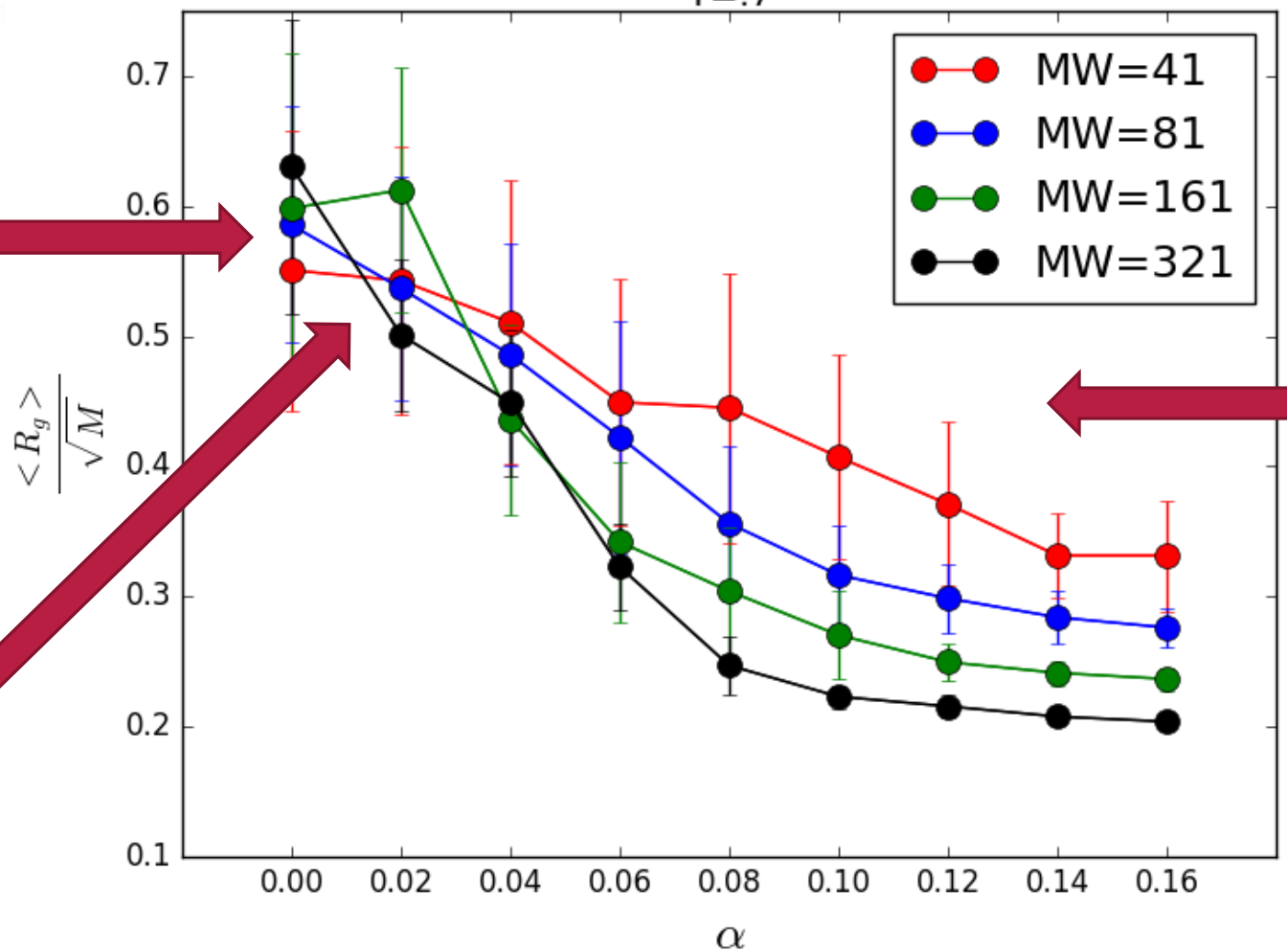
### Mixing Rule Dependence of $\langle R_g \rangle$ for Linear Chains

$T=.7$

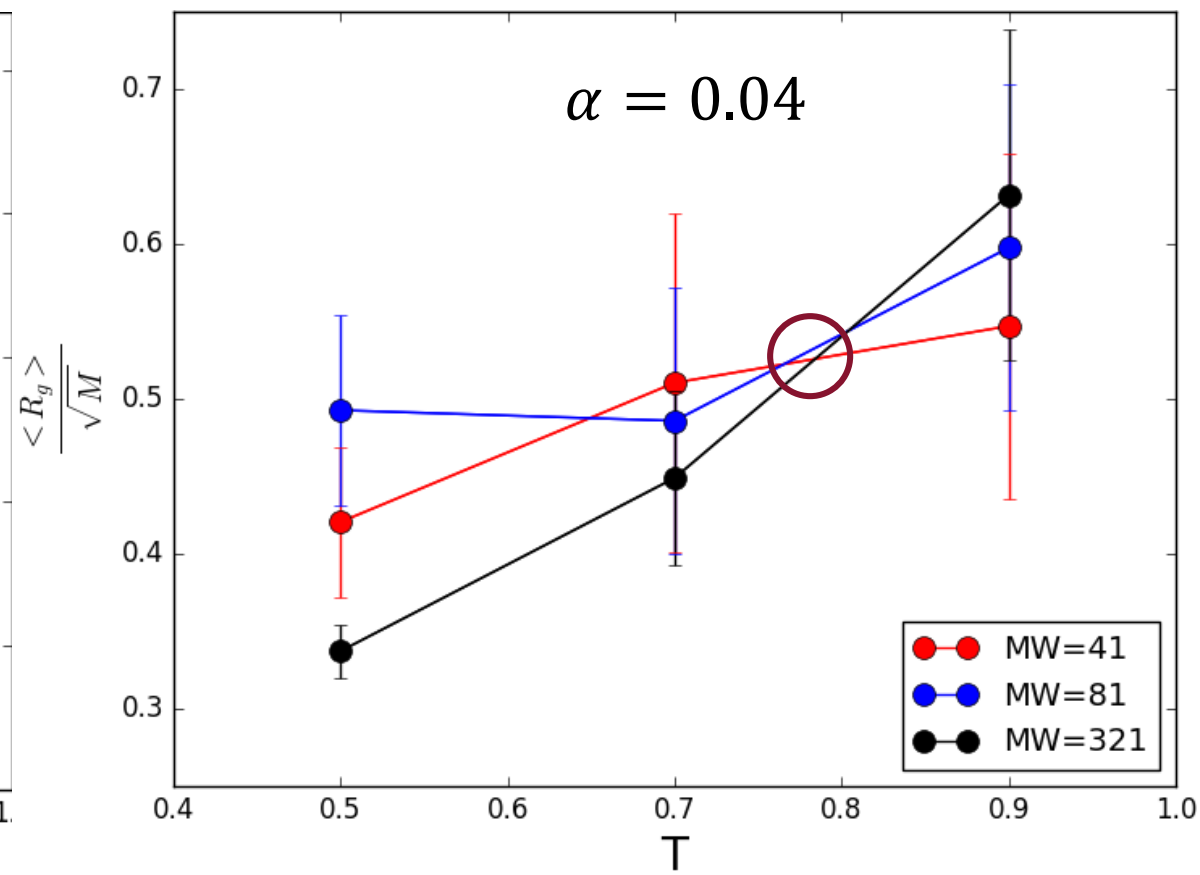
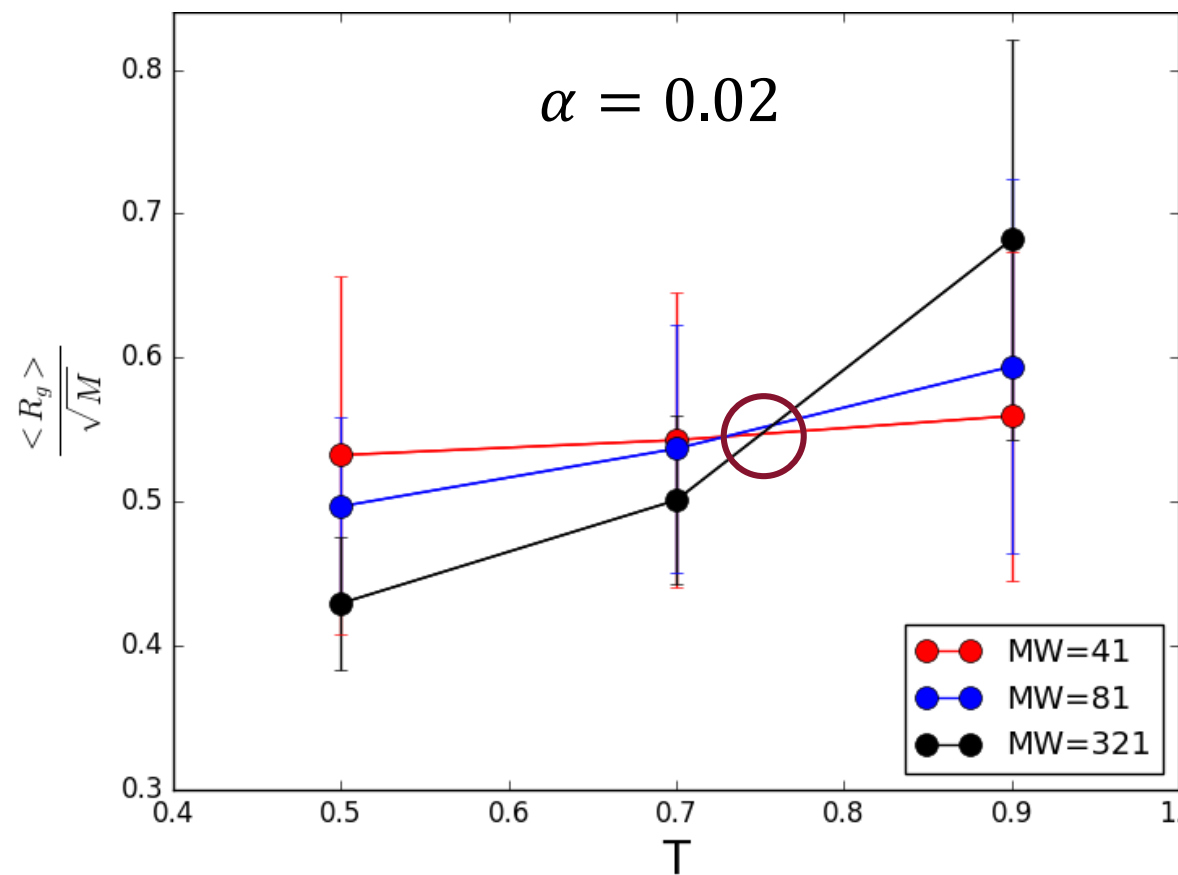
$\alpha=0$   
Swollen Region  
Good solvent  
conditions

$0.02 < \alpha < 0.04$   
Intermediate Region  
 $R_g$  is sensitive to  
changes in temperature

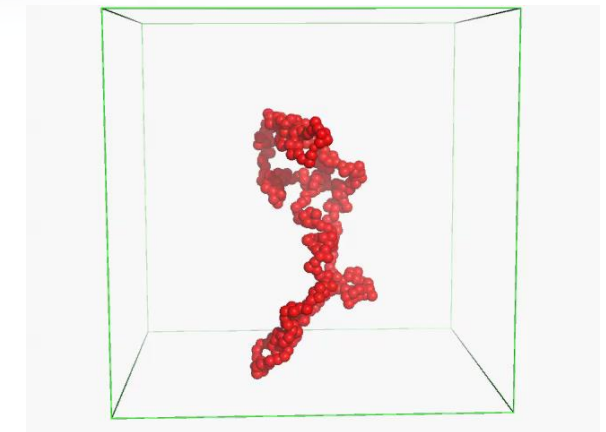
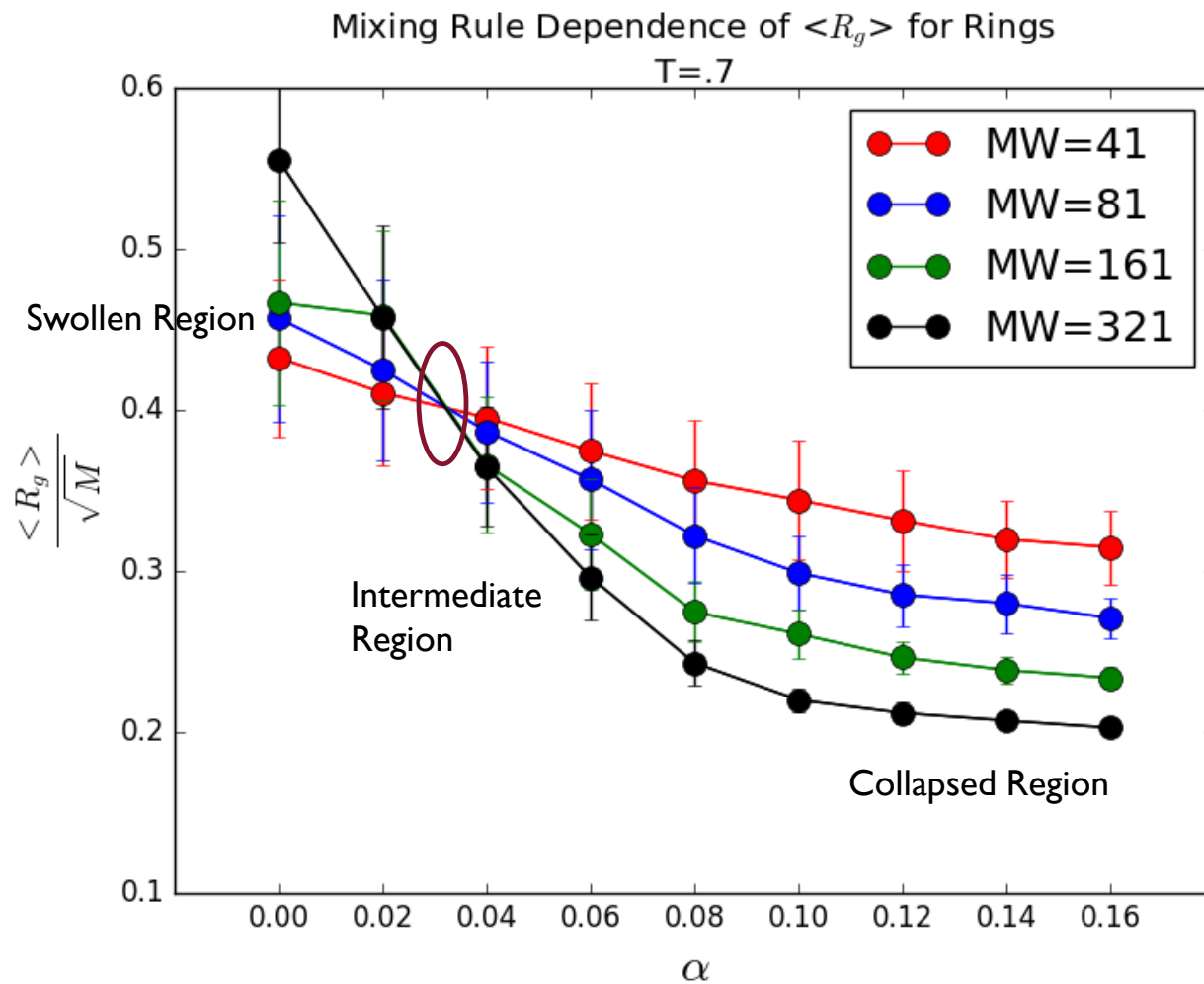
$\alpha \geq 0.06$   
Collapsed Region  
Always poor solvent  
conditions



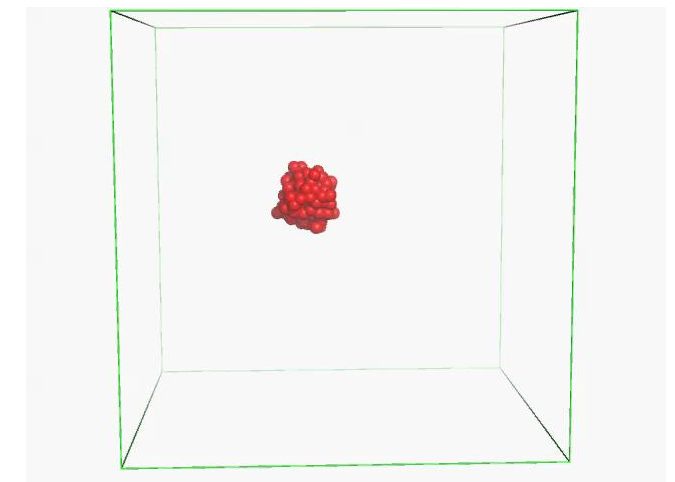
# INTERMEDIATE REGION-LINEAR



# RING POLYMERS

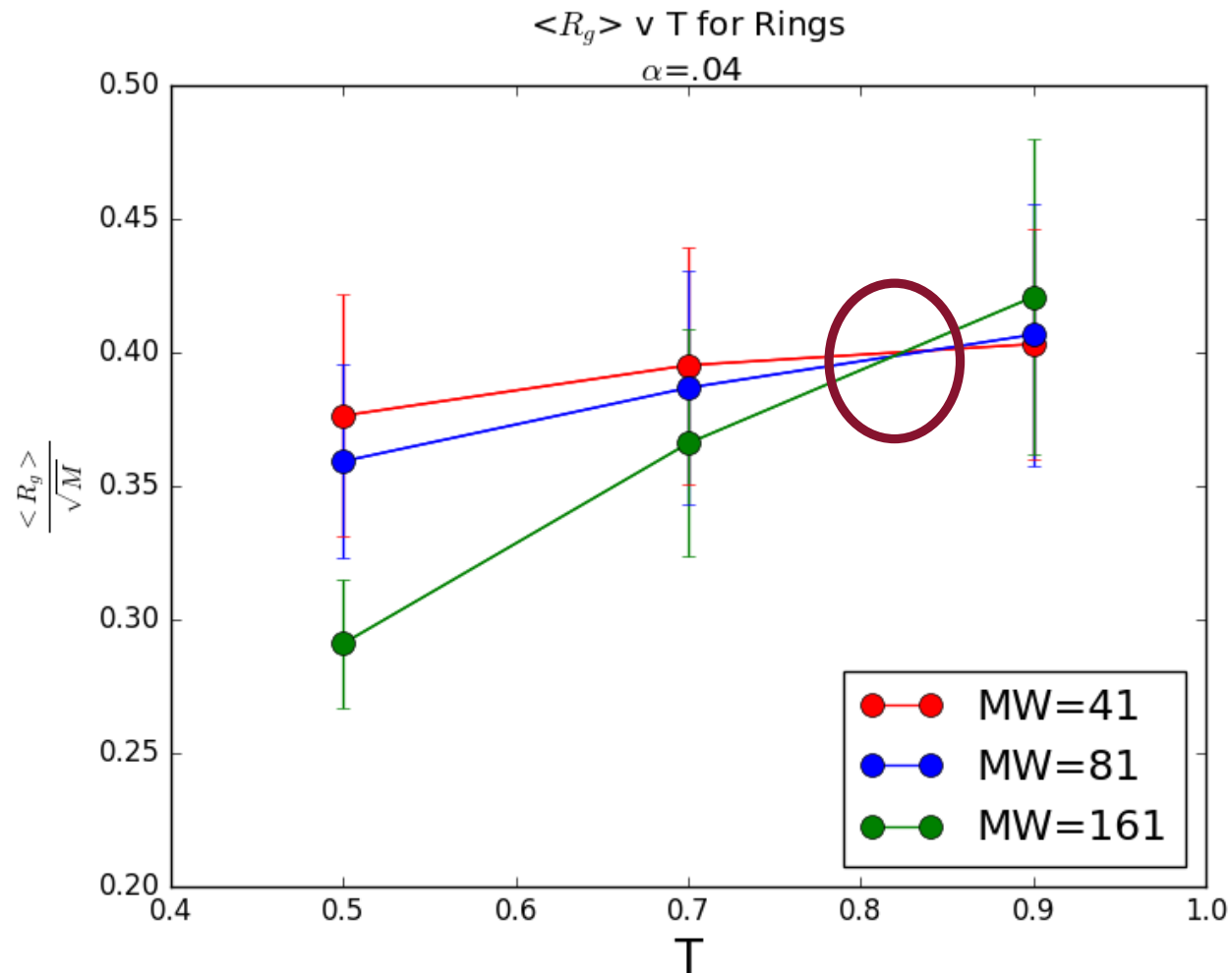


Swollen Ring



Collapsed Ring

# INTERMEDIATE REGION-RINGS



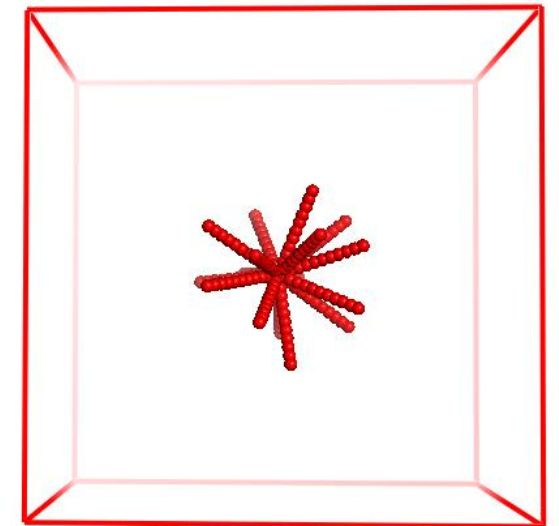
- $\alpha = 0.04$
- $\theta$ -temperature in range  $0.8 < \theta < 0.9$



# FUTURE WORK

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- Increase resolution of search for  $\theta$ -temperature
  - Explore  $0 < \alpha < 0.06$
  - Explore more temperatures within range  $0.5 < T < 0.9$
- Explore different types of molecular architectures
  - Find  $\theta$ -temperature for branched polymers



Branched/Star Polymer



# ACKNOWLEDGMENTS



- Dr. Alexandros Chremos
  - Dr. Jack Douglas
- Computational Soft Materials Working Group (COMSOFT)
- NIST Material Measurement Laboratory (MML)
- NIST Summer Undergraduate Research Fellowship (SURF) Program
  - Le Moyne College