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# Introduction to PNR

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**NIST** Center for  
Neutron Research



# What is PNR For?

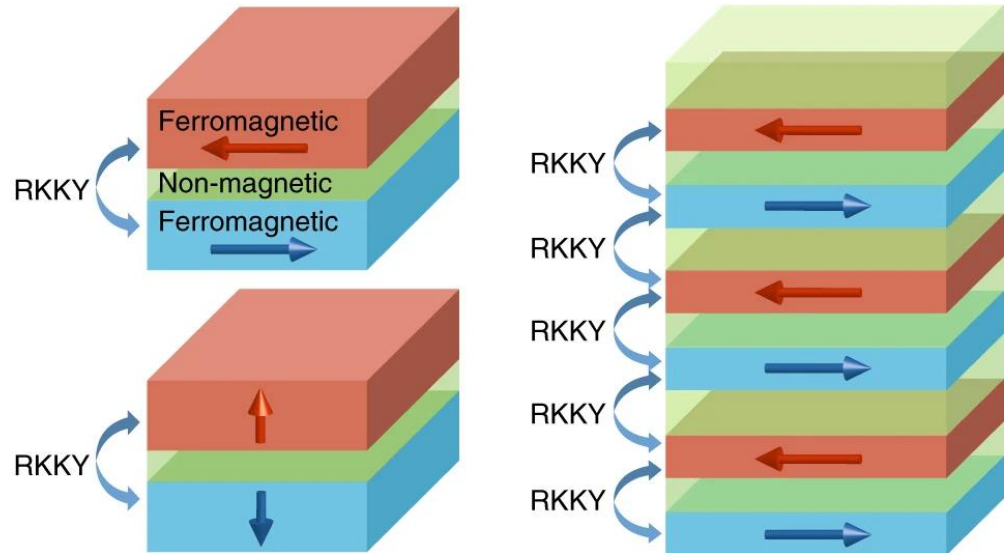
## Magnetometry

Measures entire sample,  
reports aggregate properties

## Electrical Transport

Probes conductive layers preferentially.  
Interpretation complex, not quantitative

What if we have a  
multilayer structure? A  
GMR stack, for example?



*R. A. Duine et al., Nature Physics 14, 217 (2018)*

# What is PNR For?

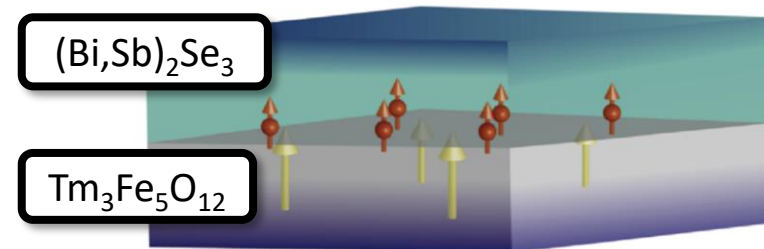
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Measures entire sample,  
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What about a magnetic  
proximity effect?

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*C. Tang et al., Science Advances 3, e1700307 (2017)*

# What is PNR For?

## Magnetometry

Measures entire sample,  
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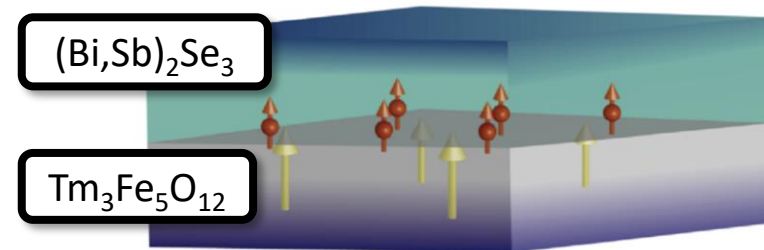
What about a magnetic  
proximity effect?

## Magnetic X-ray Spectroscopy

Element-specific magnetic  
characterization

## Electrical Transport

Probes conductive layers preferentially.  
Interpretation complex, not quantitative

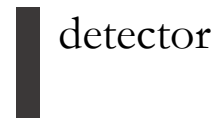
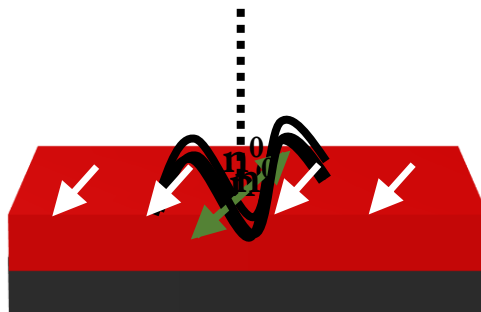
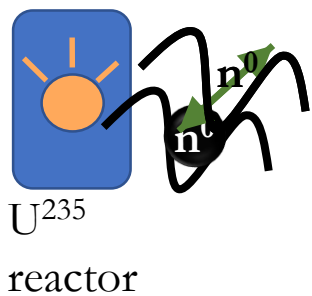
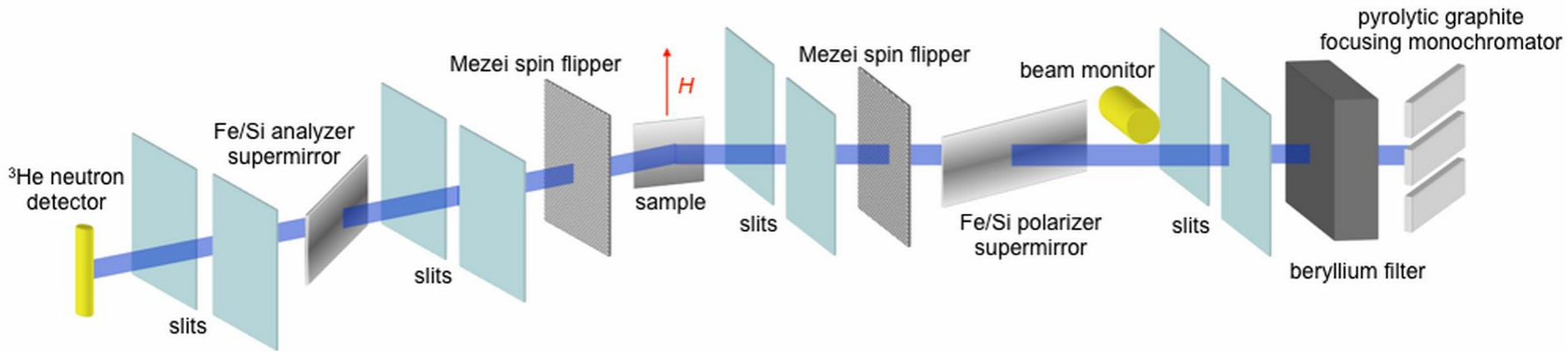


*C. Tang et al., Science Advances 3, e1700307 (2017)*

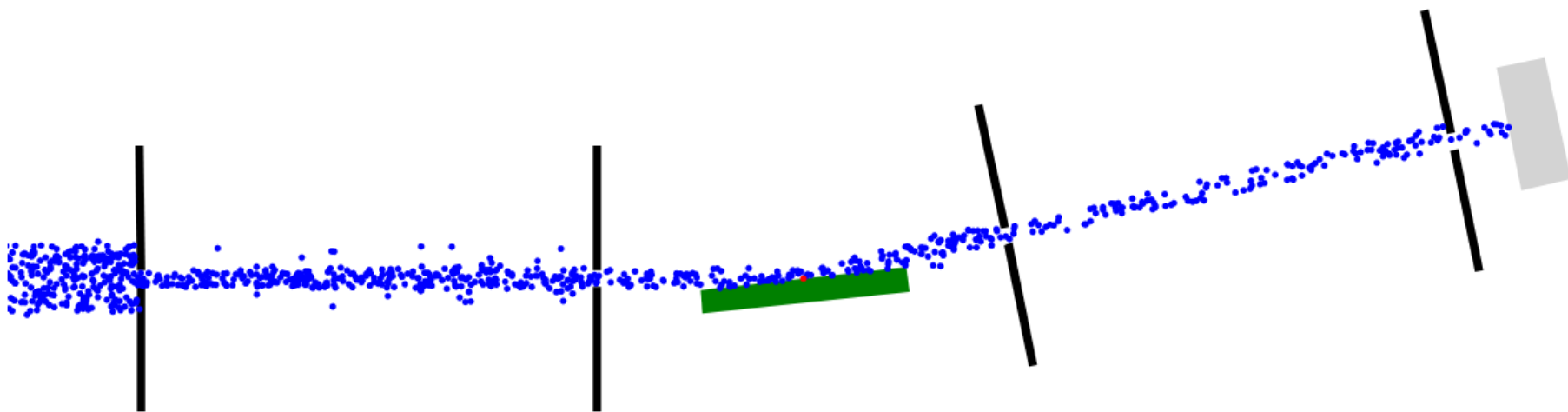
## Polarized Neutron Reflectometry

Depth-resolved magnetic  
characterization

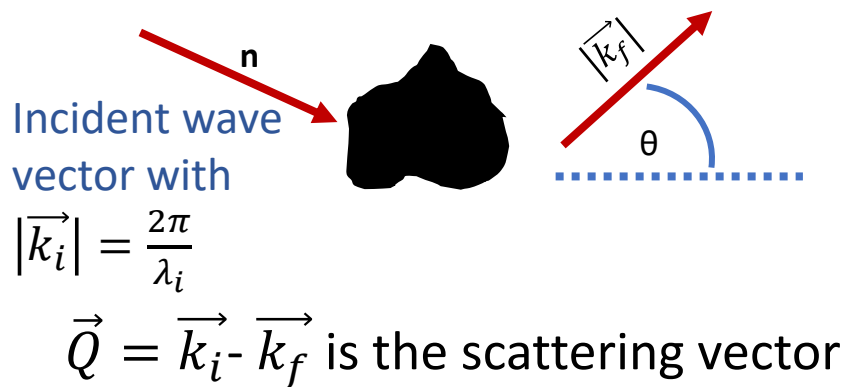
- Which layers are magnetic?
- What direction are they pointing?
- Dead layers? Proximity Effects?  
Interface exchange coupling?



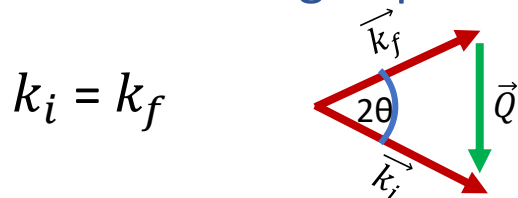
[https://ncnr.nist.gov/instruments/magik/d3-science/reflectometer\\_alignment\\_sim.html](https://ncnr.nist.gov/instruments/magik/d3-science/reflectometer_alignment_sim.html)



Because is a scattering technique where collect data as a function of angle, this is a **reciprocal space** technique

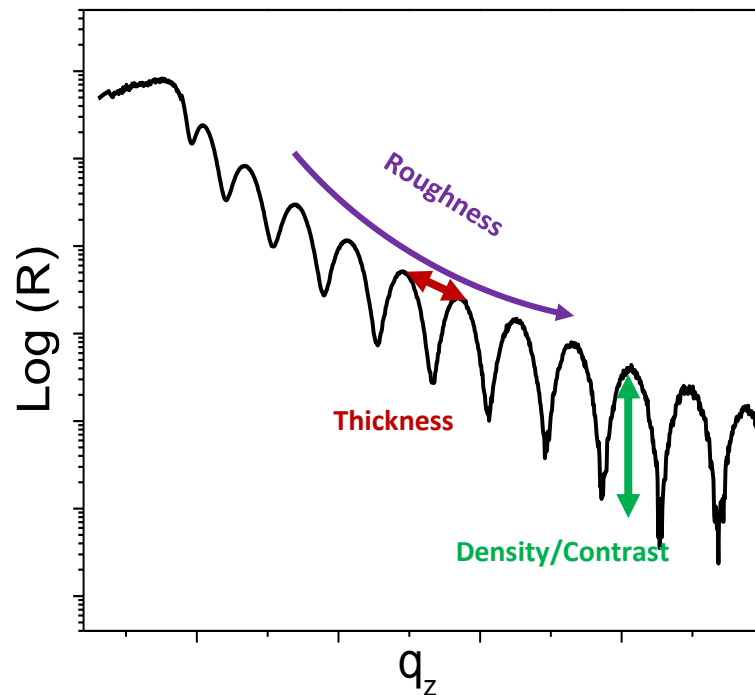


Elastic scattering implies:



$$Q = \frac{4\pi}{\lambda} \sin \theta$$

$$d \approx \frac{2\pi}{Q}$$



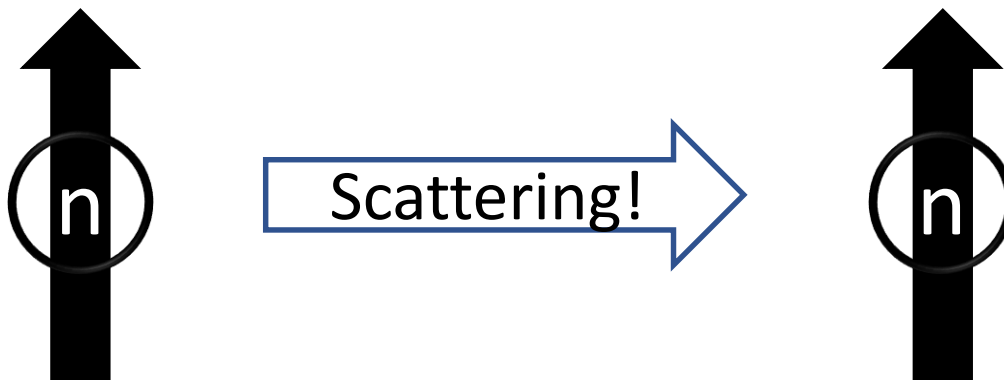
Neutron reflectometry is sensitive to chemical and in-plane magnetization depth dependence

Interacts with *Magnetic Fields*

Spin  $\frac{1}{2}$

$$\vec{\mu}_n = -1.913 \mu_N \vec{\sigma}$$

Polarization Analysis:



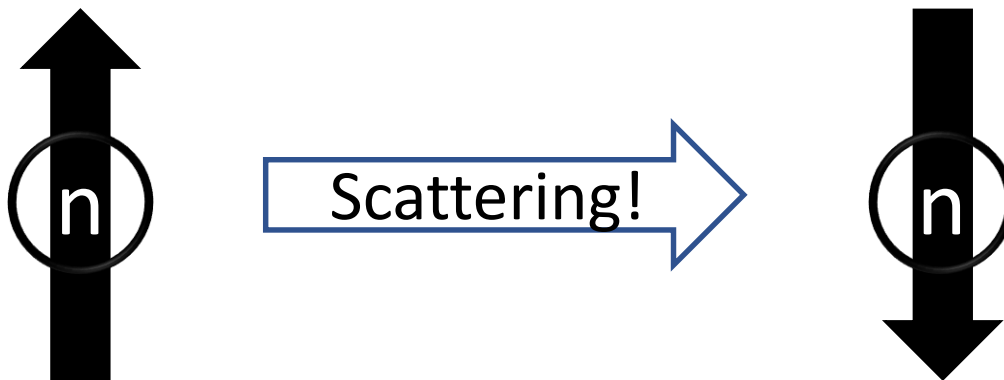


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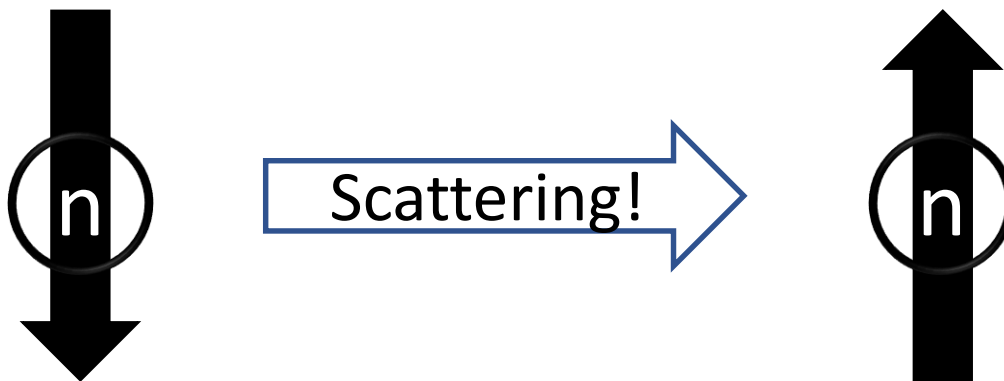


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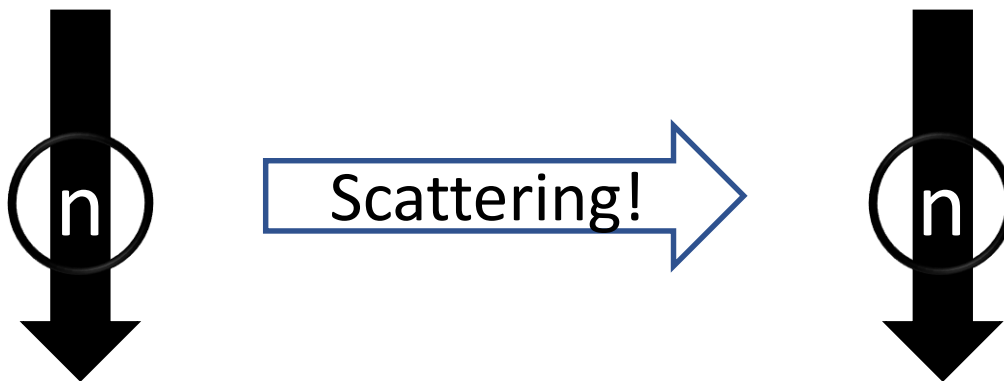


Interacts with *Magnetic Fields*

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Polarization Analysis:



## Magnetic Sensitivity:

Non-spin flip ( $\uparrow\uparrow$  or  $\downarrow\downarrow$ )

-  $M \parallel H$

Spin-flip (or  $\downarrow\uparrow$ )

-  $M \perp H$

Both Cases

-  $M \perp Q$

## Continuum Limit:

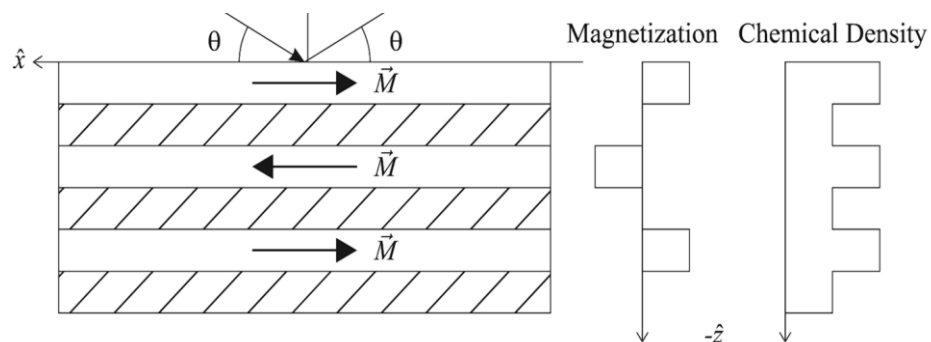
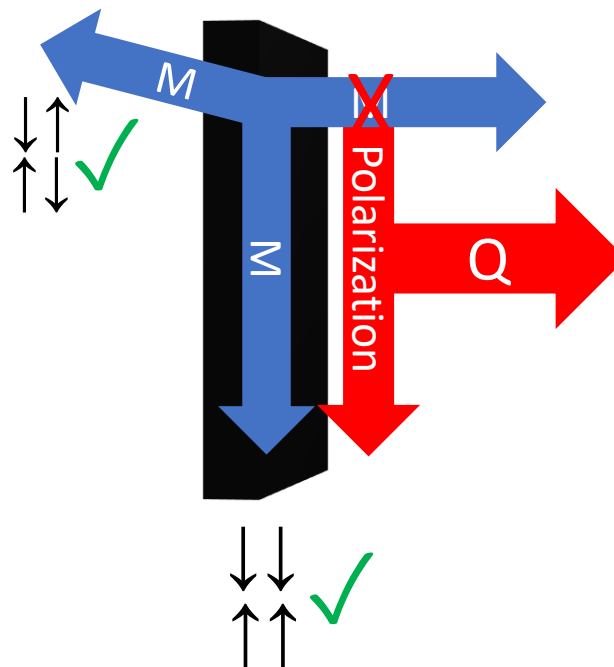
Scattering Length Density (SLD)

$$SLD_{\uparrow\uparrow} = \rho_N(Z) + \rho_M(Z)$$

$$SLD_{\downarrow\downarrow} = \rho_N(Z) - \rho_M(Z)$$

$$\rho_N = \sum_{j=1}^M N_j b_j$$

$$\rho_M = \mp \frac{m}{2\pi\hbar^2} \mu B$$



## Magnetic Sensitivity:

Non-spin flip ( $\uparrow\uparrow$  or  $\downarrow\downarrow$ )

-  $\mathbf{M} \parallel \mathbf{H}$

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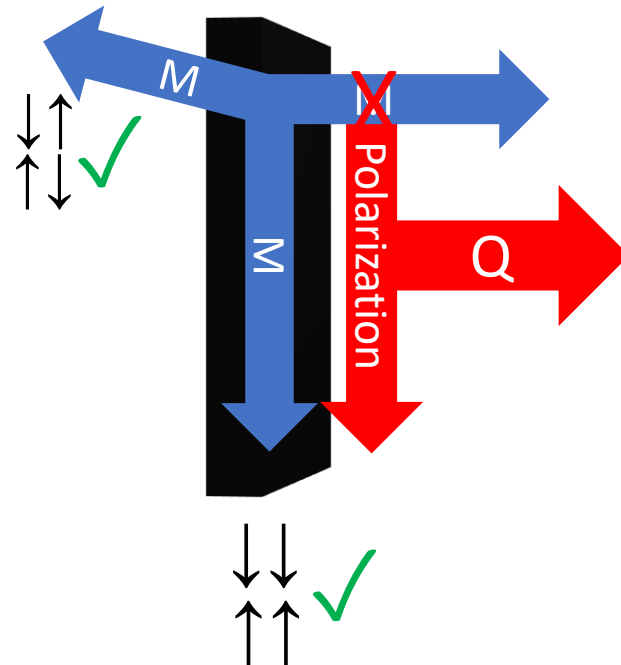
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$$\rho_N = \sum_{j=1}^M N_j b_j$$

$$\rho_M = \mp \frac{m}{2\pi\hbar^2} \mu B \rightarrow \mathbf{M} = \rho_M / (2.853 \times 10^{-9} \text{ \AA}^{-2} \text{ cm}^3/\text{emu})$$



Fitzsimmons and Majkrzak: <https://www.ncnr.nist.gov/instruments/pbr/references/Fitz.pdf>

**Table 1 Listing of common elements and their neutron nuclear and magnetic scattering length densities.**

Material	Number density, $N$ [ $\text{\AA}^{-3}$ ]	Nuclear scattering length, $b$ [ $\text{\AA}$ ]	Magnetic moment, $\mu$ [ $\mu_B$ ]	Nuclear scattering length density, $\rho_n$ [ $\text{\AA}^{-2}$ ]	Magnetic scattering length density, $\rho_m$ [ $\text{\AA}^{-2}$ ]
Ag	$5.86 \times 10^{-2}$	$5.92 \times 10^{-5}$		$3.47 \times 10^{-6}$	
Al	6.02	3.45		2.08	
Al <sub>2</sub> O <sub>3</sub>	2.13	24.4		5.21	
Au	5.90	7.90		4.66	
Co	9.09	2.49	1.715	2.26	$4.12 \times 10^{-6}$
Fe	8.47	9.45	2.219	8.00	$4.97 \times 10^{-6}$
FeF <sub>2</sub>	2.75	20.76		5.71	
Fe <sub>2</sub> O <sub>3</sub> (hematite)	2.00	36.32		7.26	
Fe <sub>3</sub> O <sub>4</sub> (magnetite)	1.35	51.57	4.1	6.97	$1.46 \times 10^{-6}$
GaAs	2.21	13.87		3.07	
LaAlO <sub>3</sub>	1.84	29.11		5.34	
LaFeO <sub>3</sub>	1.65	35.11		5.78	
LaMnO <sub>3</sub>	1.71	21.93		3.75	
MgF <sub>2</sub>	3.07	16.68		5.12	
MgO	5.35	11.18		5.98	
MnF <sub>2</sub>	2.58	7.58		1.96	
Nb	5.44	7.05		3.84	
Ni	9.13	10.3	0.604	9.40	$1.46 \times 10^{-6}$
<sup>58</sup> Ni	9.13	14.4	0.604	13.14	$1.46 \times 10^{-6}$
<sup>62</sup> Ni	9.13	-8.7	0.604	-7.94	$1.46 \times 10^{-6}$
Ni <sub>81</sub> Fe <sub>19</sub>	8.93	10.14	1.04	9.06	$2.46 \times 10^{-6}$
NiO	5.49	16.11		8.84	

## Continuum Limit:

Scattering Length Density (SLD)

$$SLD_{\uparrow\uparrow} = N(Z) + M(Z)$$

$$SLD_{\downarrow\downarrow} = N(Z) - M(Z)$$

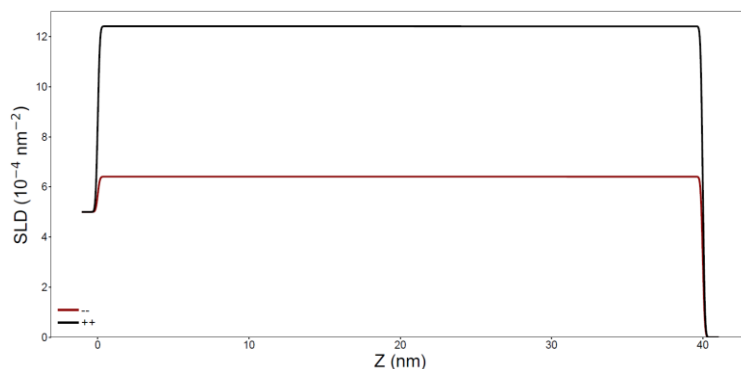
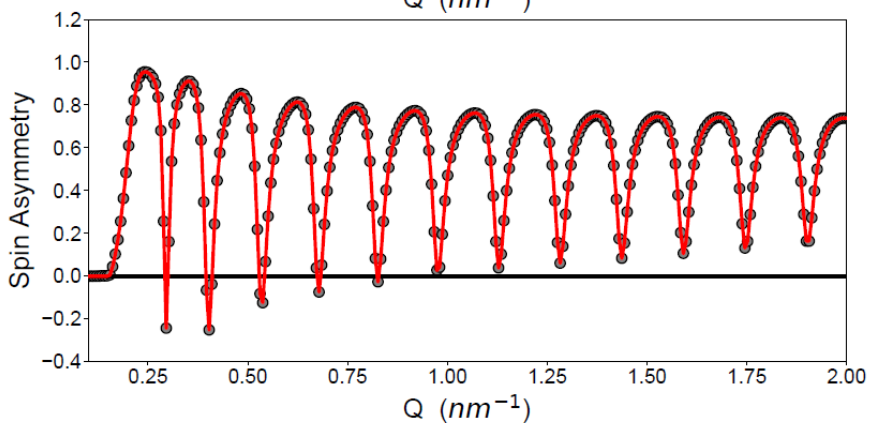
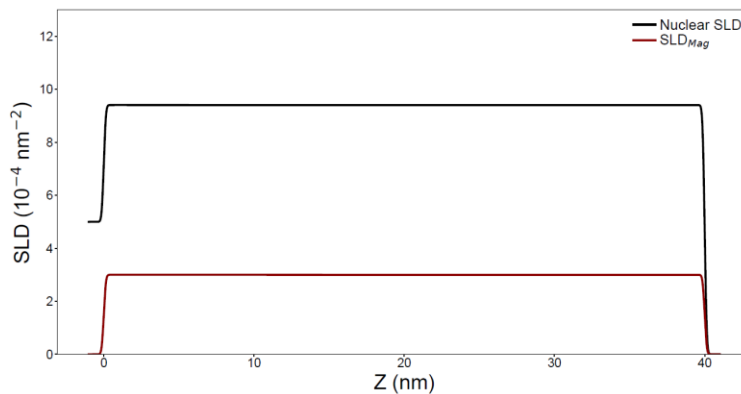
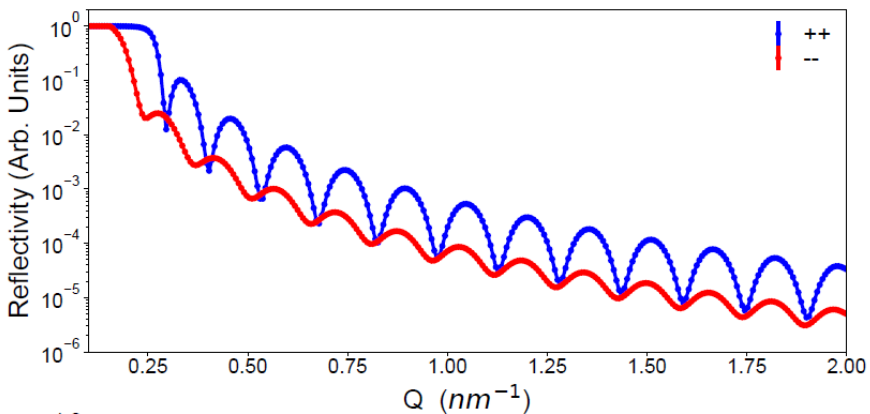
$$R = (N + M)^2 = N^2 + 2NM + M^2$$

$$SA = (\uparrow\uparrow - \downarrow\downarrow) / (\uparrow\uparrow + \downarrow\downarrow) = 2NM / (N+M)^2$$

Where  $N$  and  $M$  are the Fourier transform of the  $\rho_N$  and  $\rho_M$  profiles.

More complicated at the “Critical Edge”

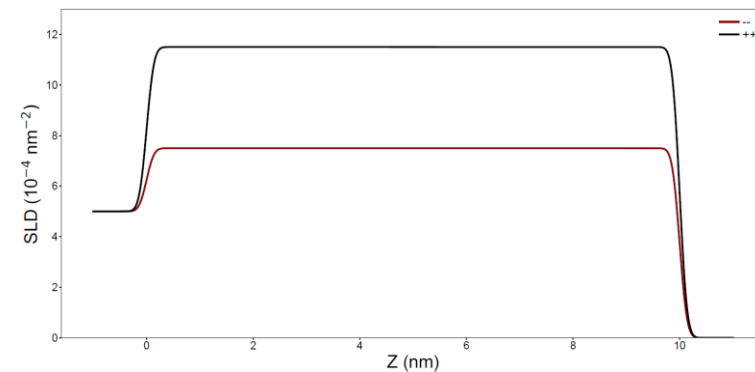
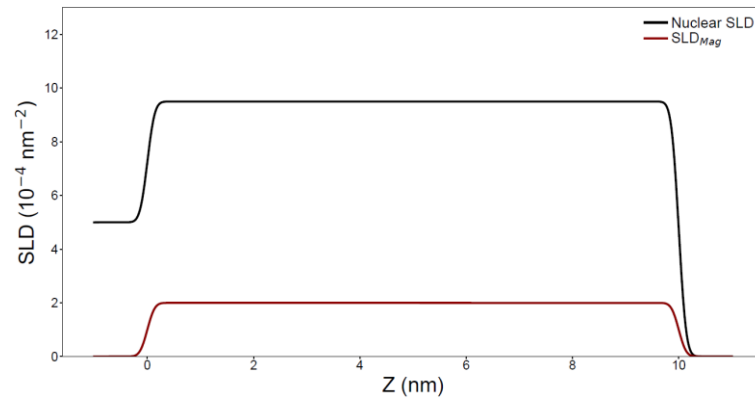
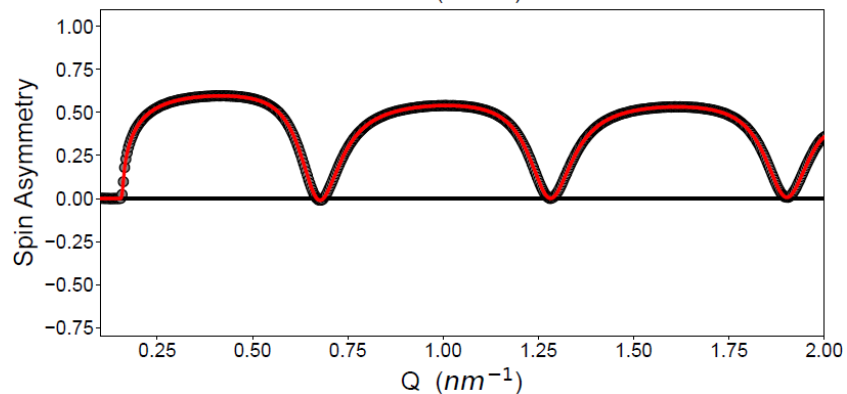
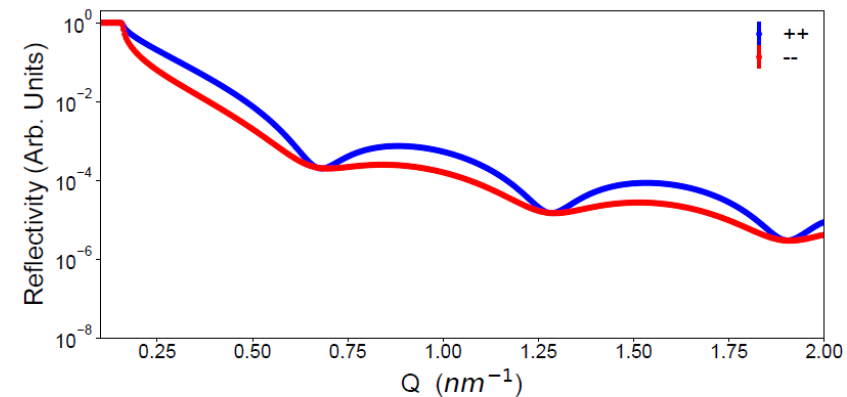
# What should data look like?



Here we see the simulated reflectivity of a 40 nm thick Ni film on MgO over a  $Q$ -range of  $2 \text{ nm}^{-1}$

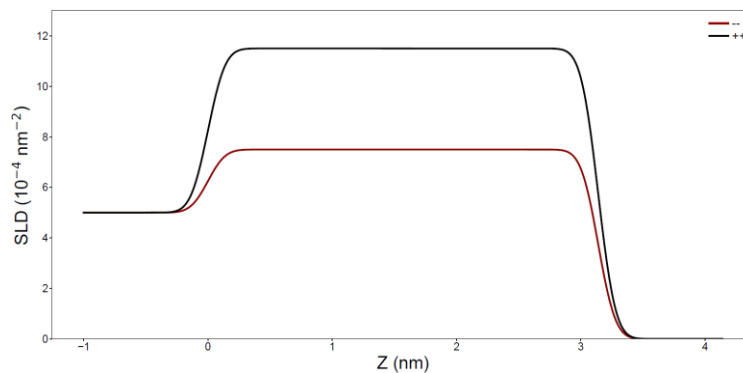
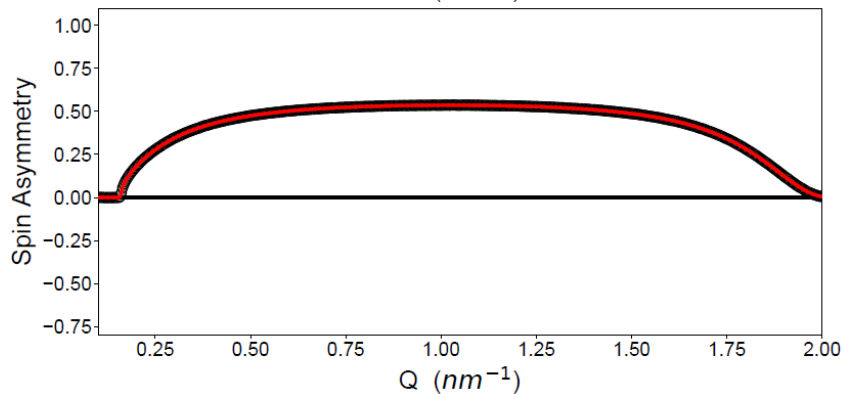
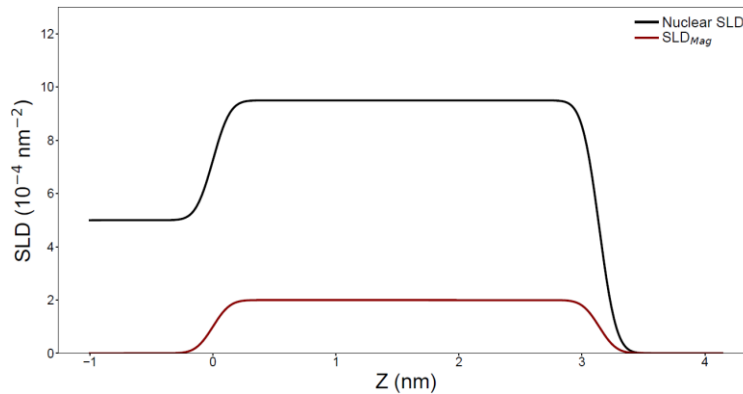
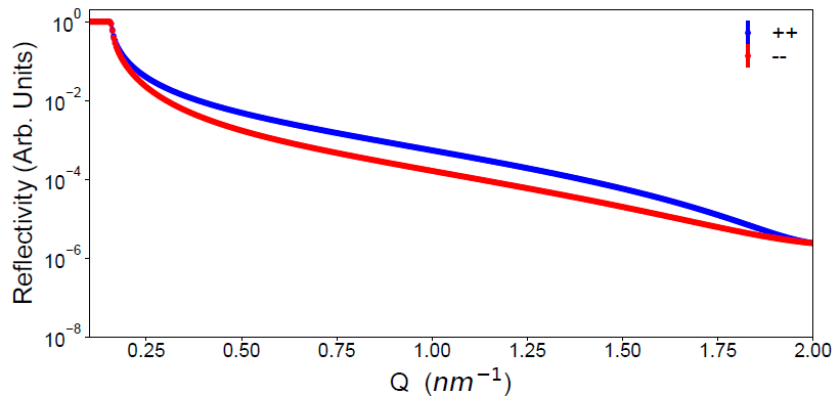


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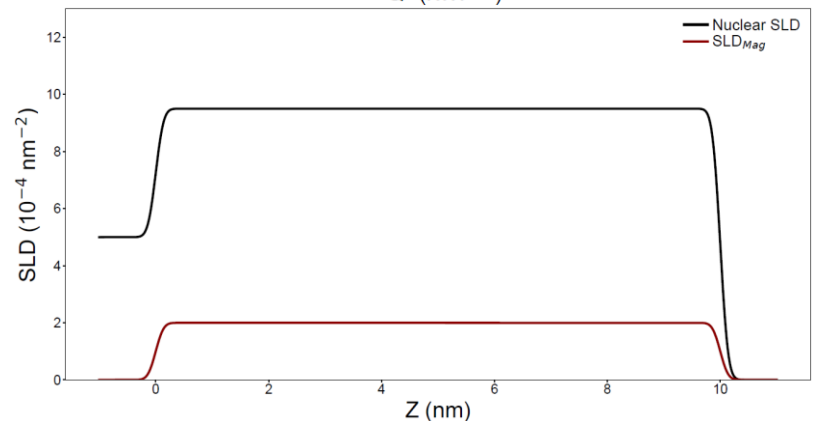
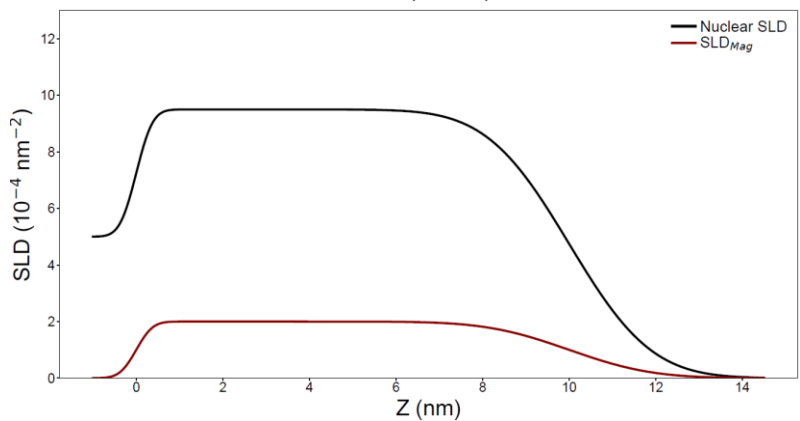
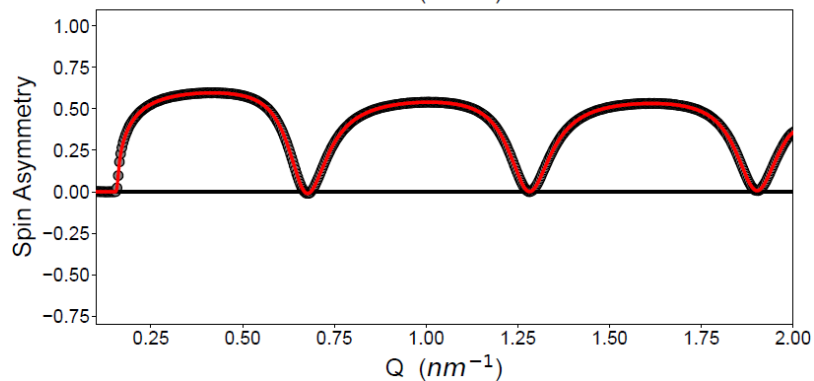
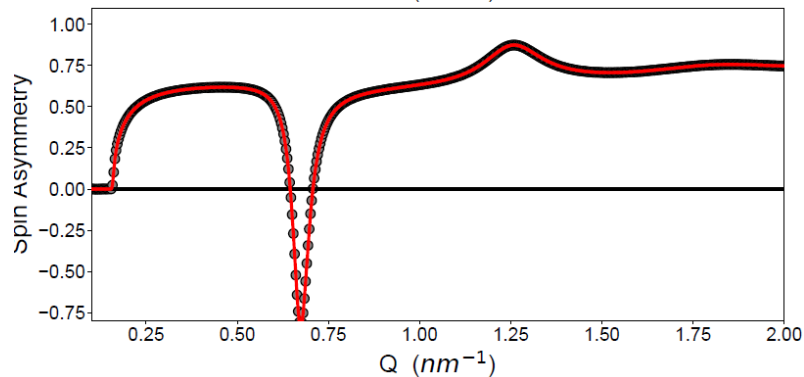
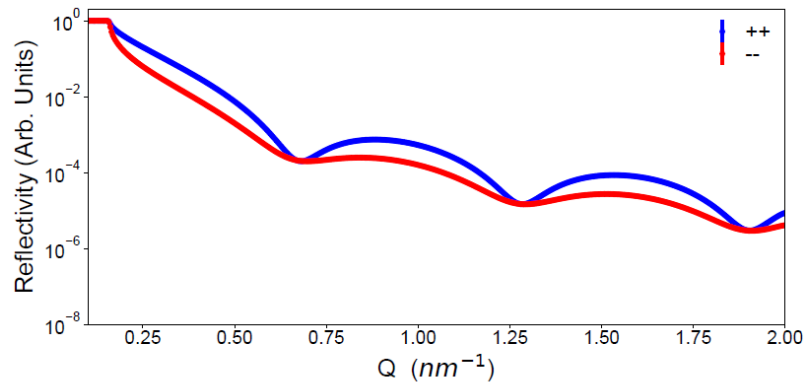
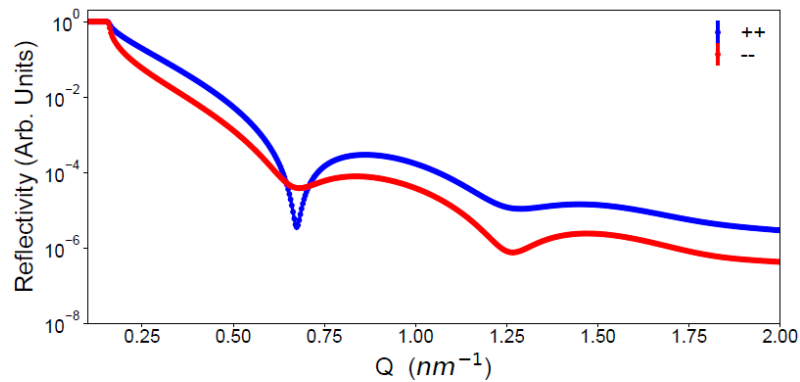


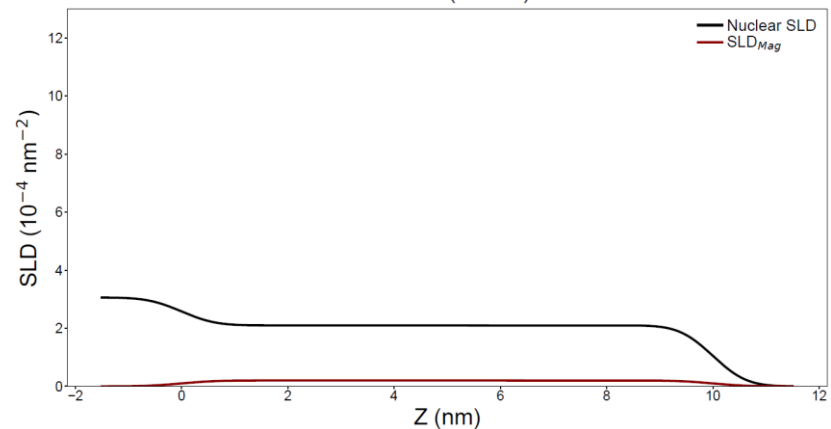
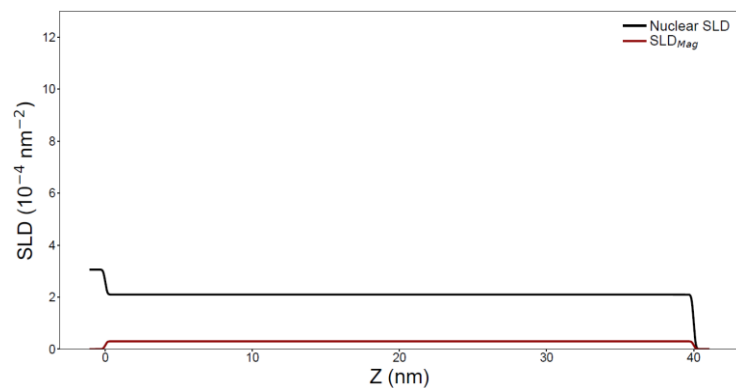
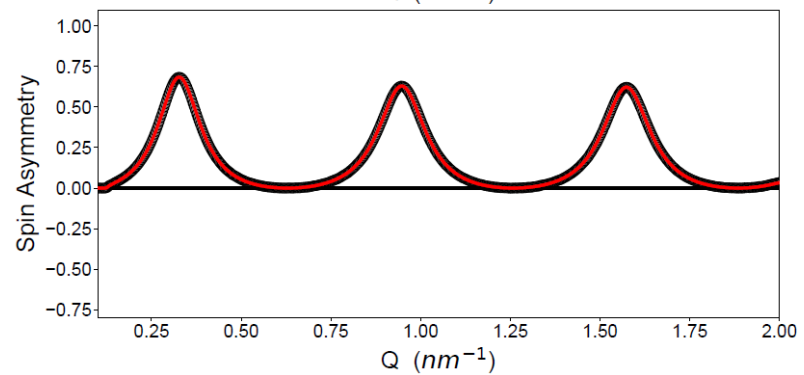
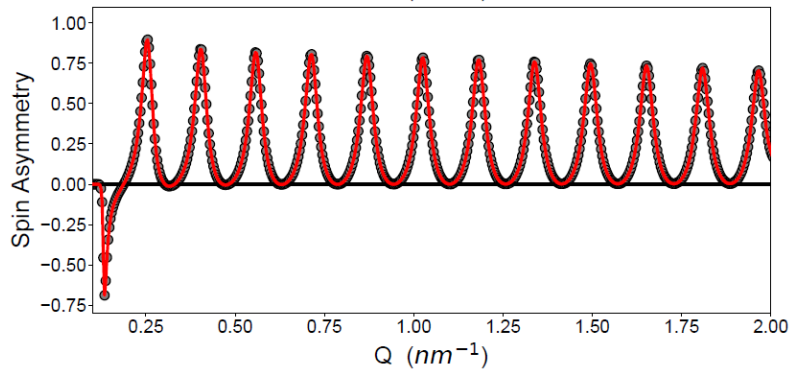
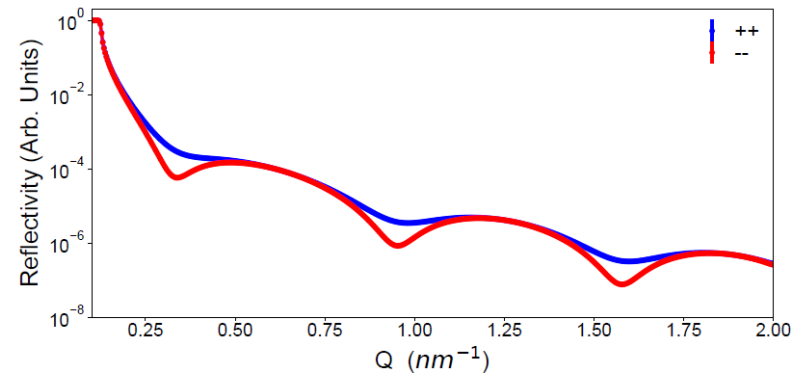
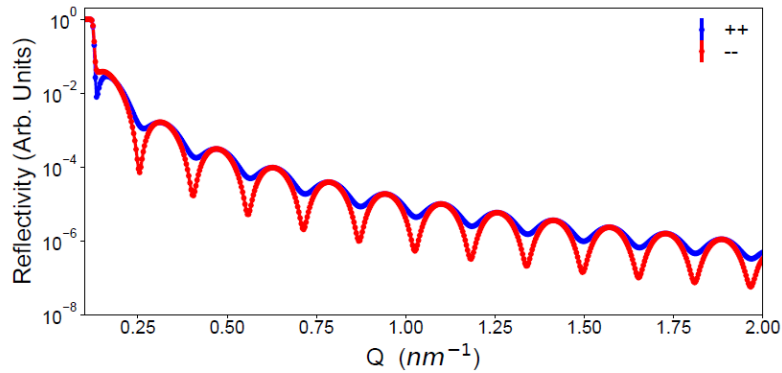
Same system, but 10 nm instead of 40 nm

# What should data look like?

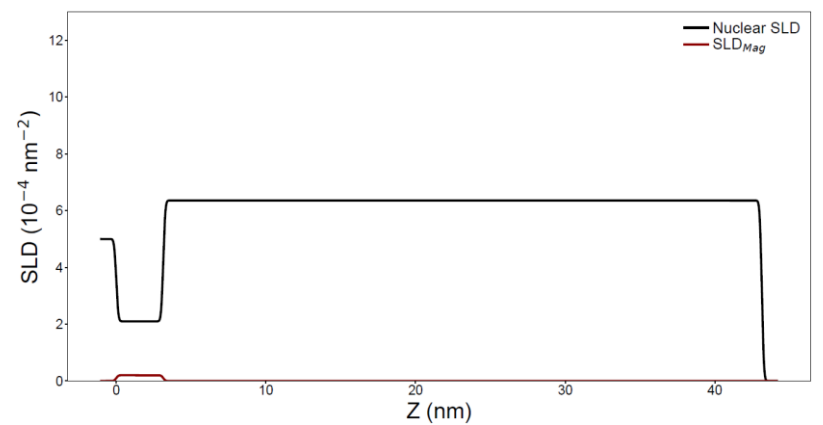
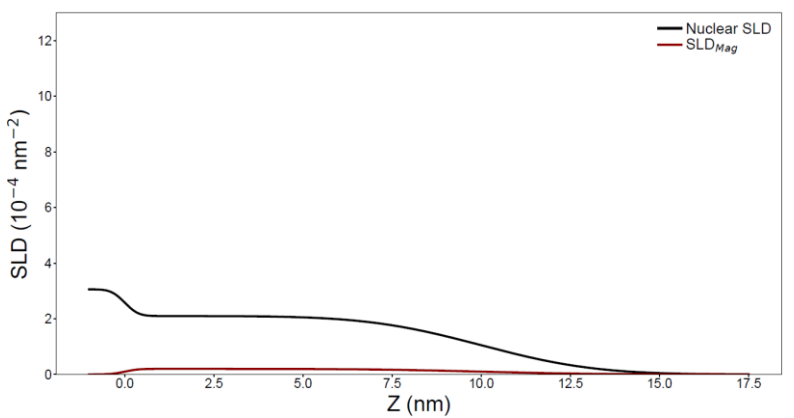
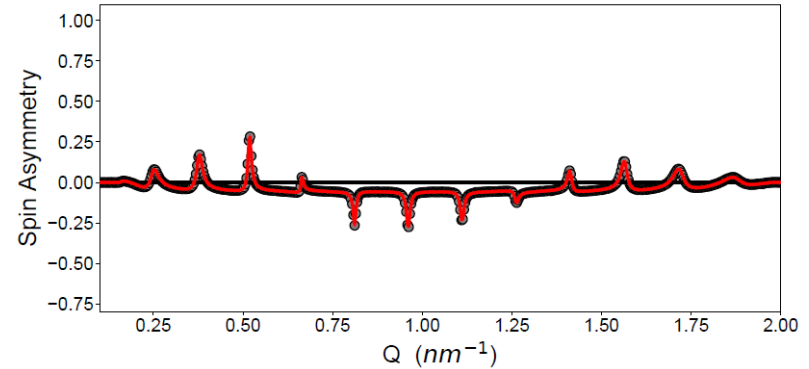
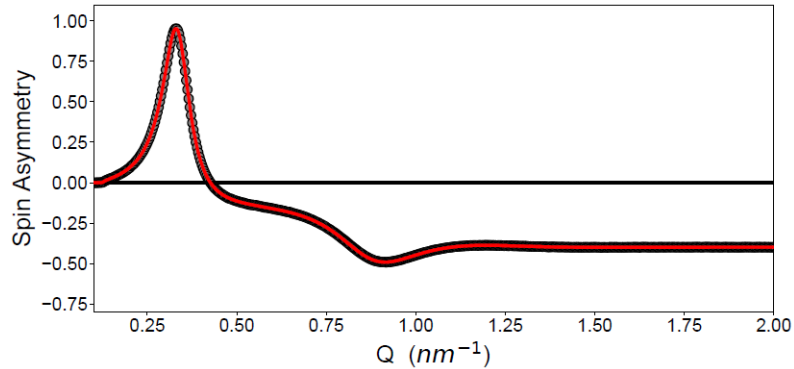
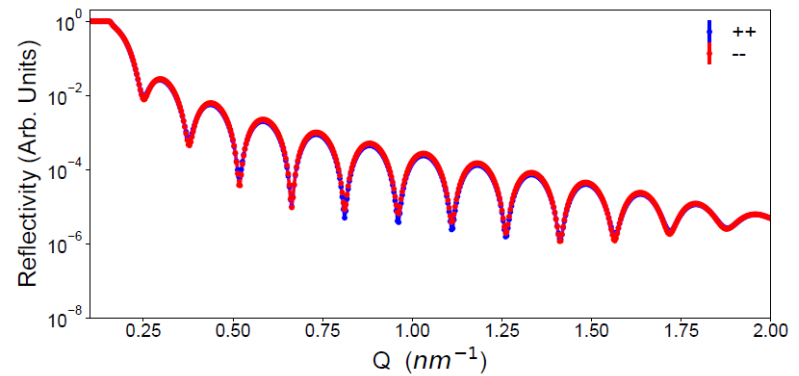
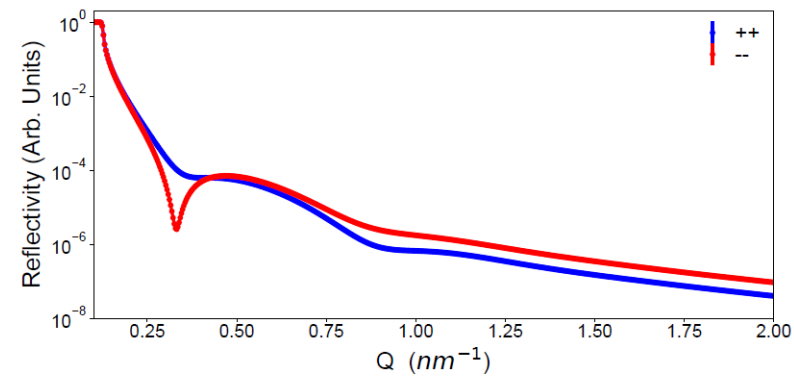


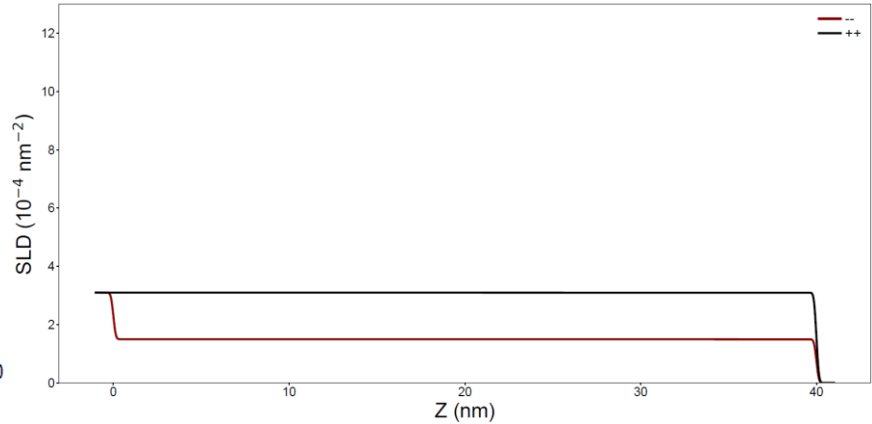
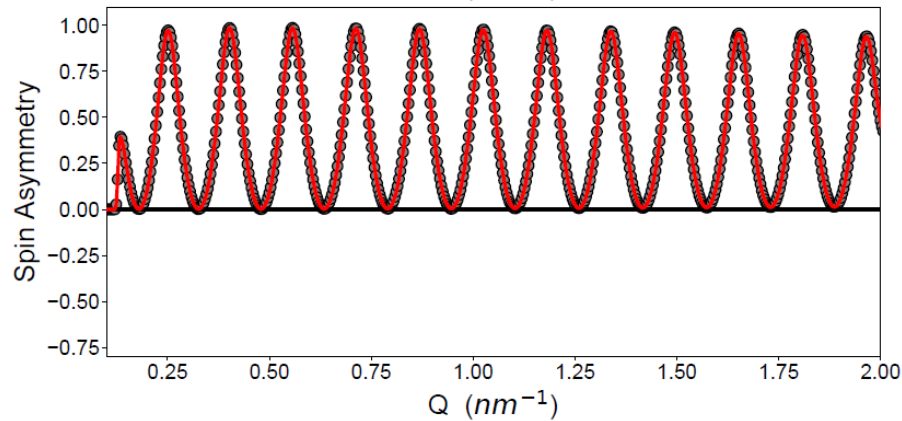
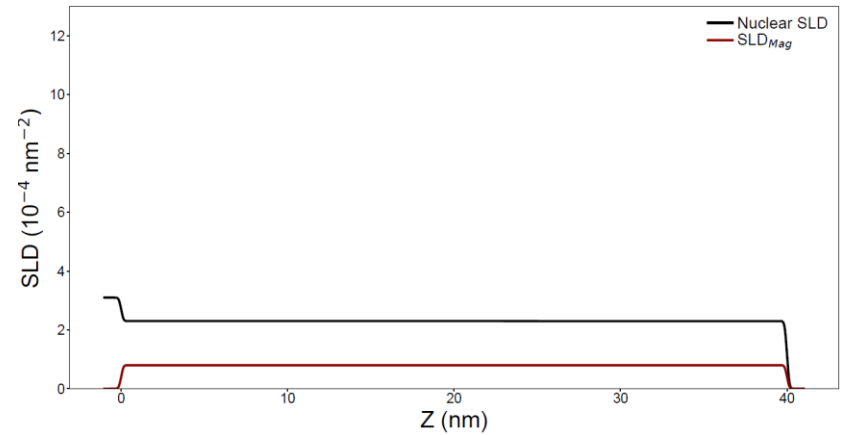
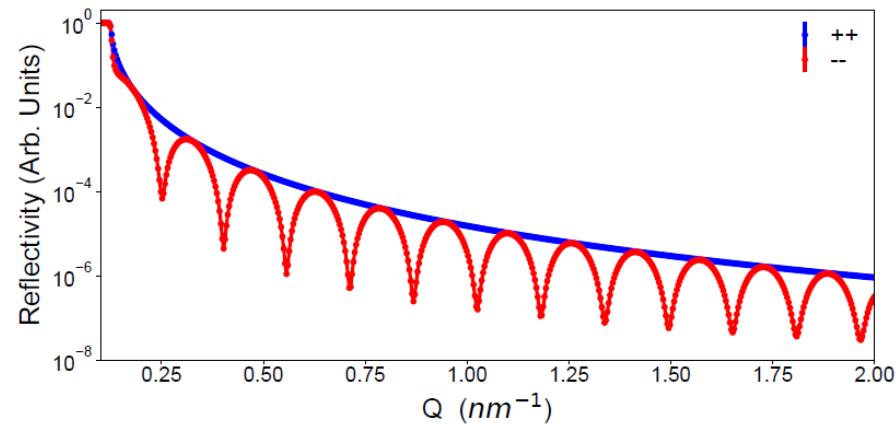
Same system, but 3 nm instead of 10 nm



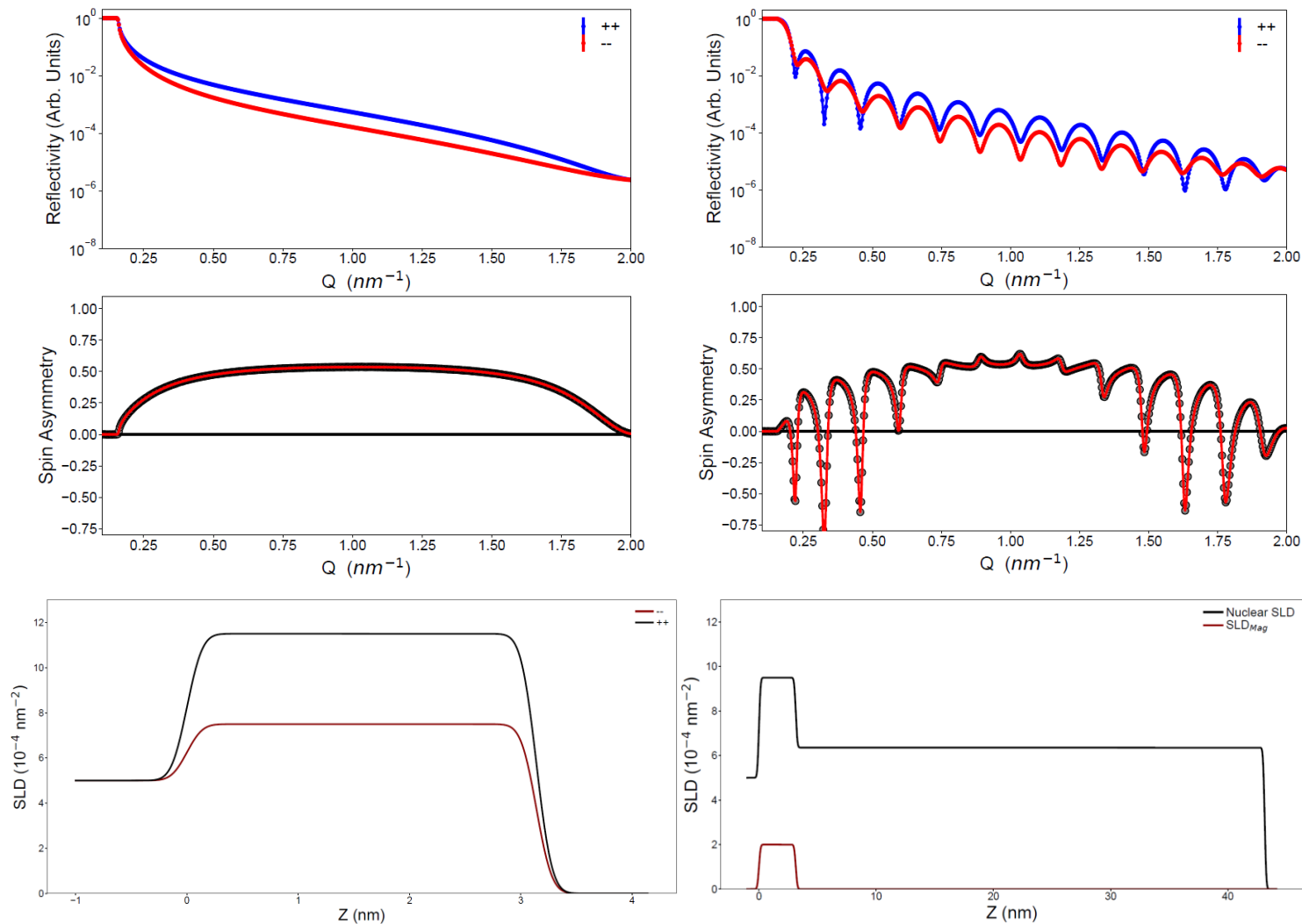


# Difficult (Real) Cases



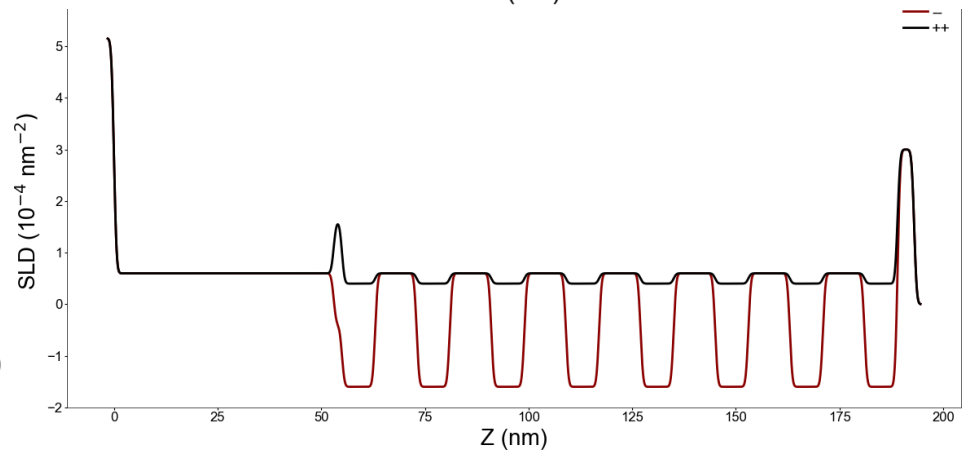
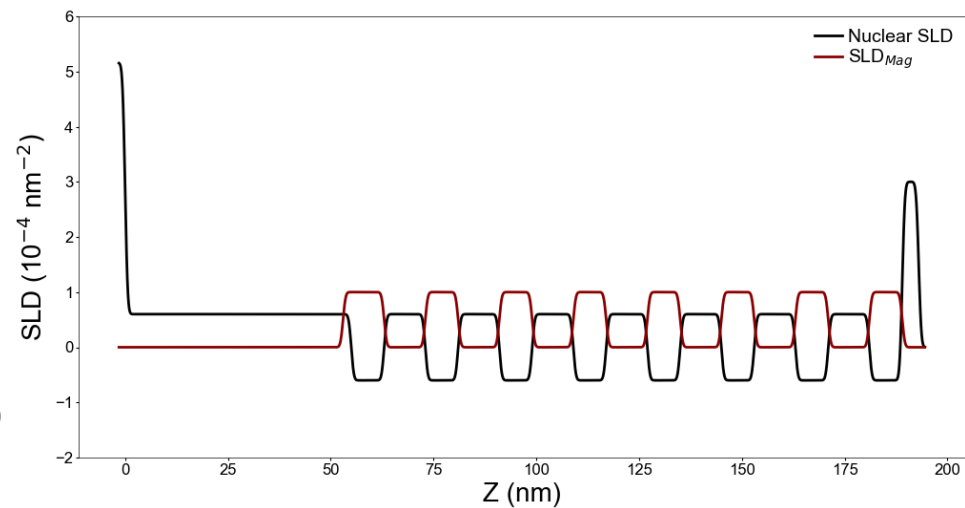
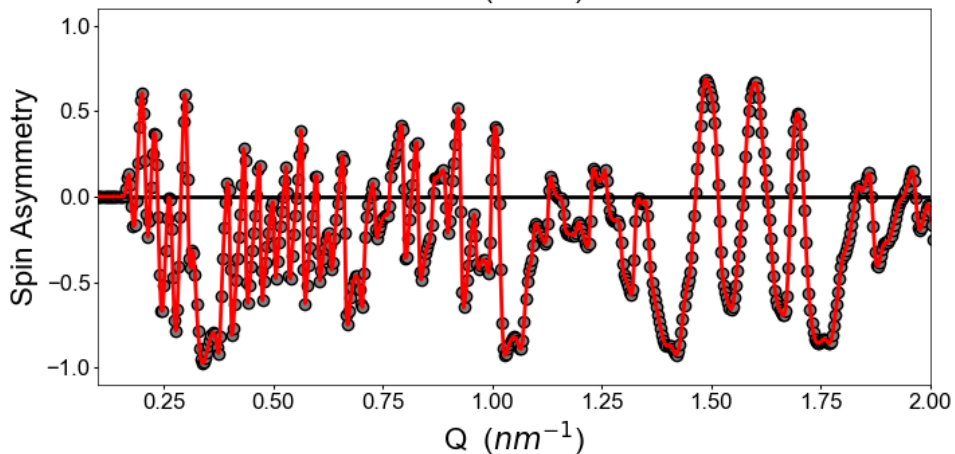
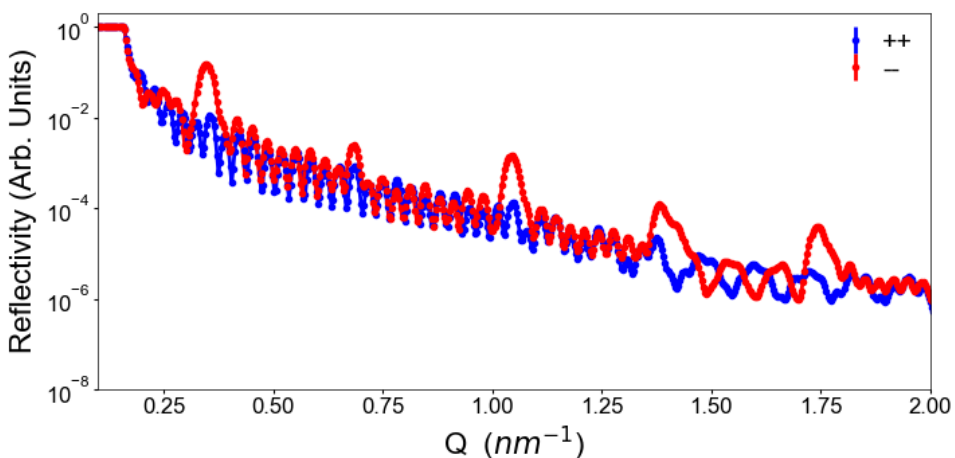


One can sometimes find systems where  $\rho_N^{\text{Substrate}} = \rho_N^{\text{Film}} + \rho_M^{\text{Film}}$  for one of the two spin states. In this case we expect oscillations in one of the spin-states and a  $R \sim Q^{-4}$  dependence for the other.



Here we see that the thick capping layer creates high-frequency features in the spin asymmetry, but the envelope function associated with the magnetic layer remains.

# Superlattice

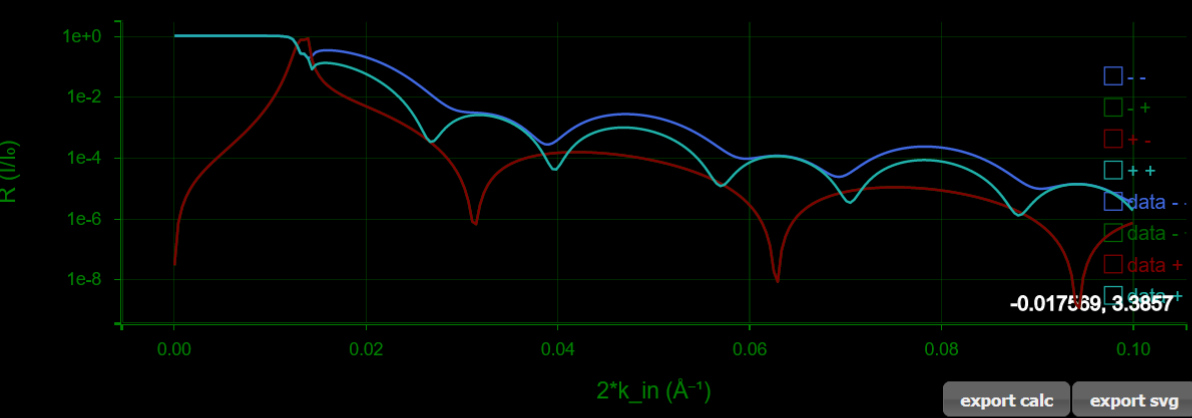


- Information-rich superlattice peaks (Bragg reflections)
- Negative scattering length density is a real thing



[https://www.ncnr.nist.gov/instruments/magik/calculators/calcR\\_mag\\_d3\\_dark.html](https://www.ncnr.nist.gov/instruments/magik/calculators/calcR_mag_d3_dark.html)

Load (\*.refl) datafile:  No files selected.



$R (I/I_0)$

$2 \cdot k_{in} (\text{\AA}^{-1})$

-0.017569, 3.3857

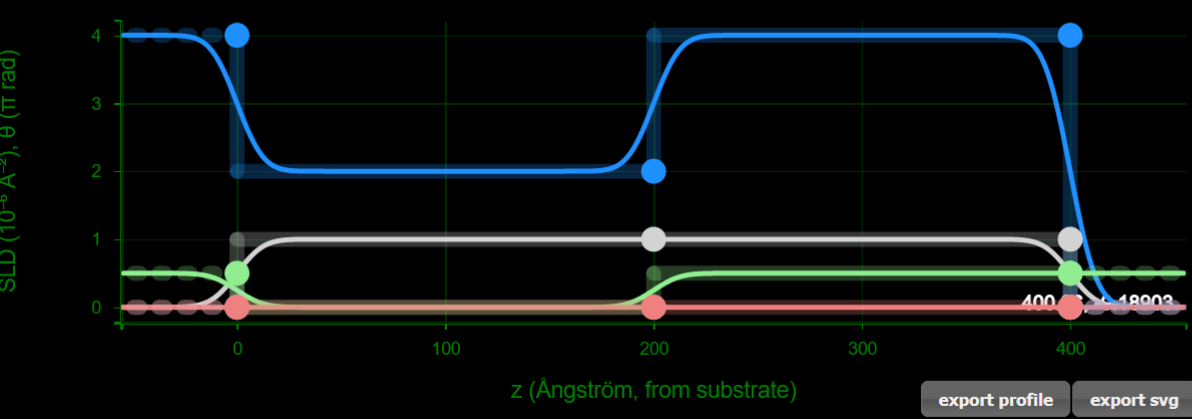
reflectivity  phase  spin asymmetry

qmin 0.0001 qmax 0.1 nPts 251 H 0 AGUIDE 270

y-scale: linear  log

thickness (Å)	roughness (above, Å)	SLDn x10 <sup>-6</sup>	SLDm x10 <sup>-6</sup>	$\theta$ (π rad)	iSLDn x10 <sup>-6</sup>		
0.0000	10.000	4.0000	0.0000	0.50000	0.0000	+after	x
200.00	10.000	2.0000	1.0000	0.0000	0.0000	+after	x
200.00	10.000	4.0000	1.0000	0.50000	0.0000	+after	x
0.0000	0.0000	0.0000	0.0000	0.50000	0.0000	+after	x

edit mode  fit mode



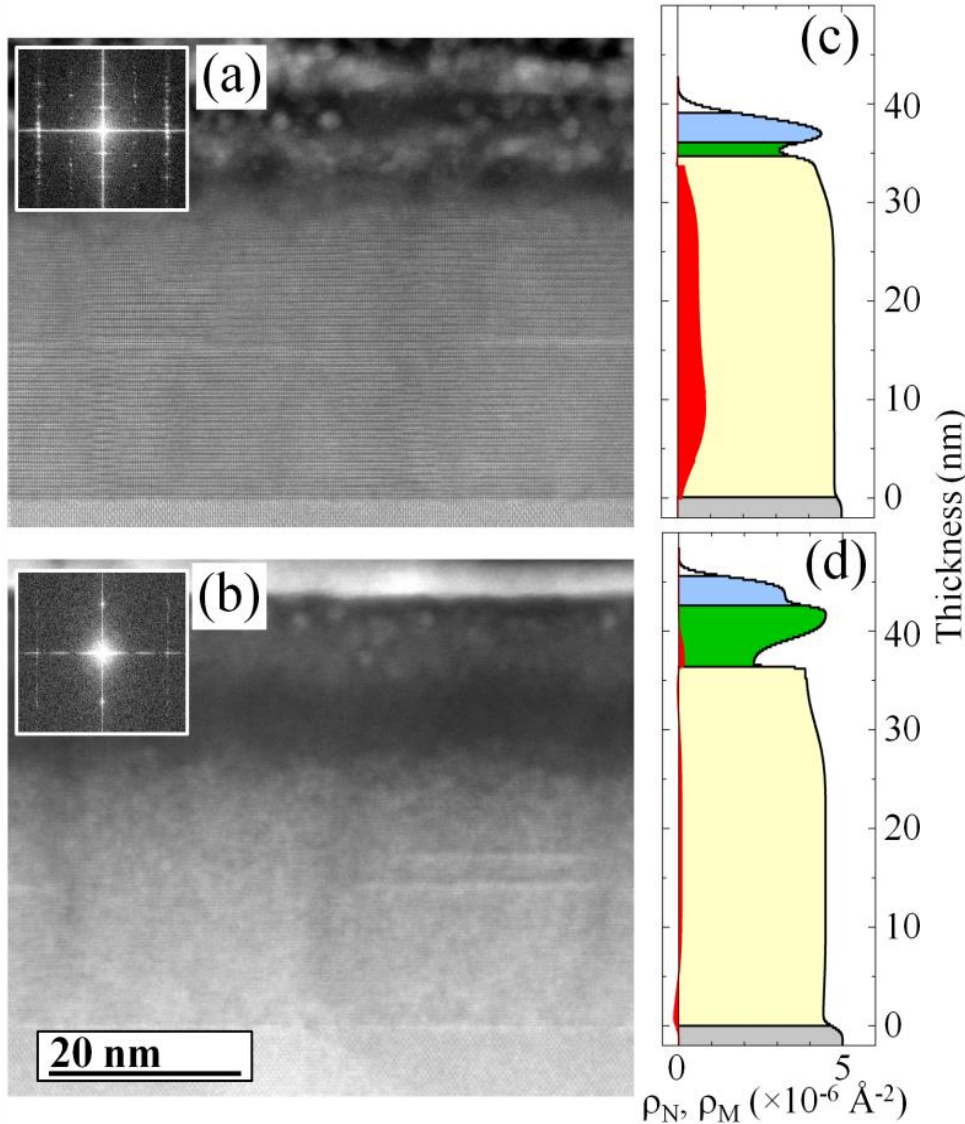
$SLD (10^{-6} \text{\AA}^{-2}), \theta (\pi \text{ rad})$

$z (\text{\AA} \text{ngstr\AA} \text{m, from substrate})$

400 18003

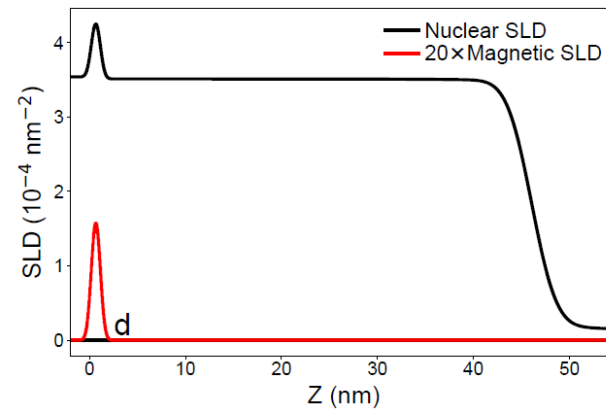
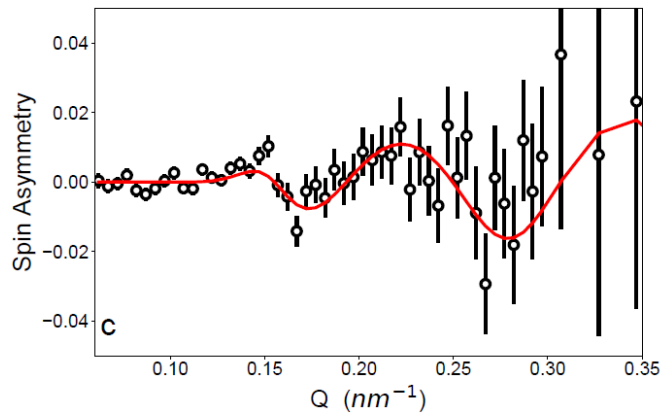
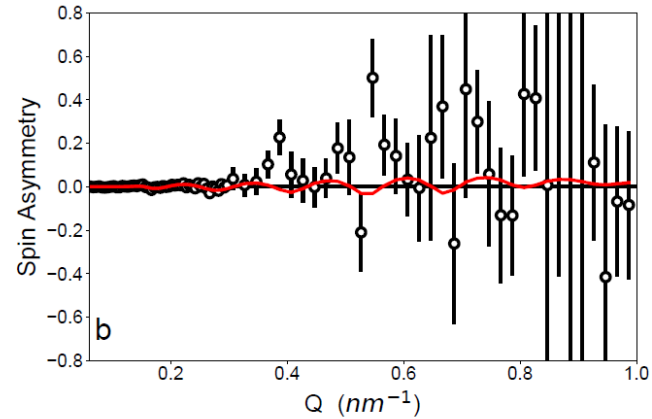
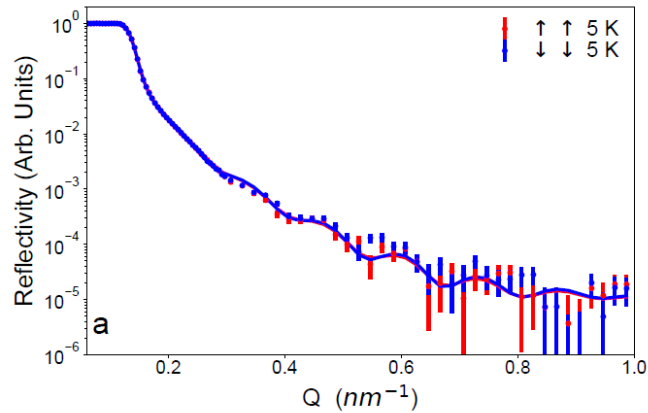
Last modified 01/25/2021 11:49:21 by website owner: NCNR (attn: Brian B. Maranville)  
Please cite as <https://doi.org/10.6028/jres.122.034> bib

# Should We Trust PNR?

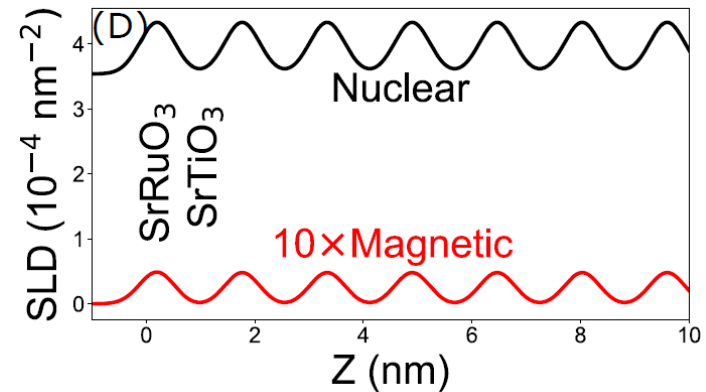
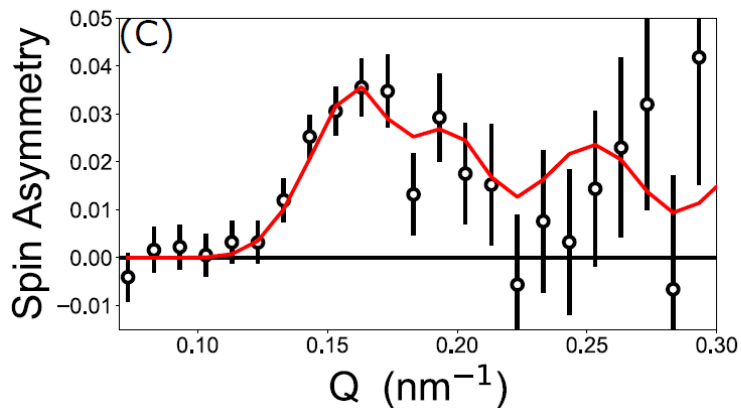
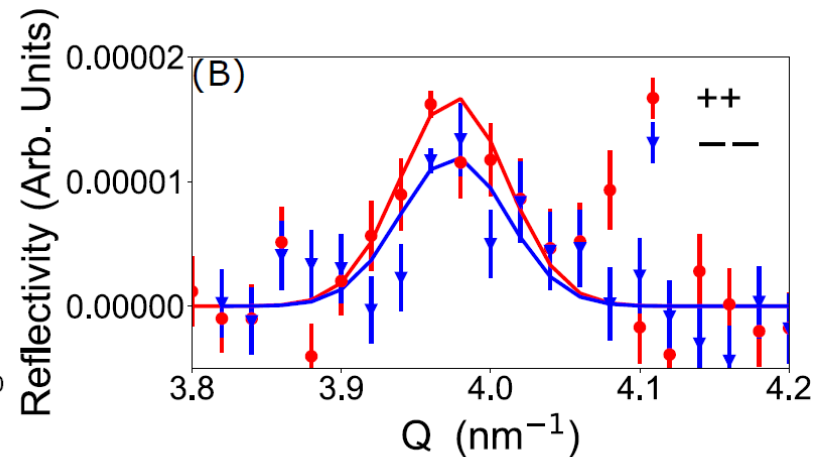
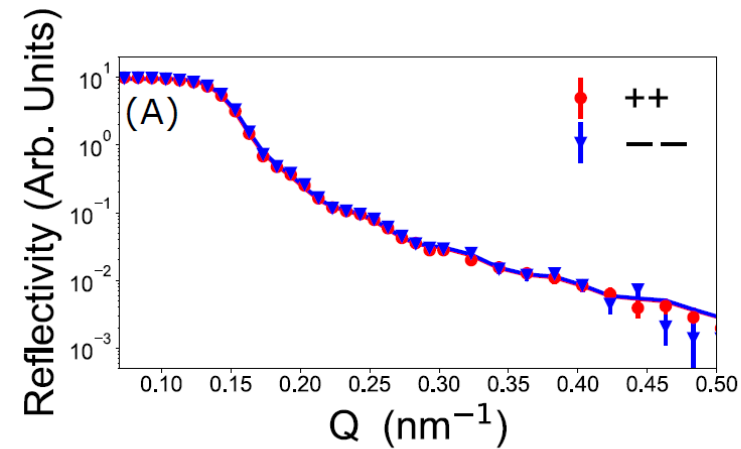


- PNR provides extremely accurate depth profiles
  - Structural
  - Magnetic
- Can ALSO extract parameters like density/composition
- Sensitive enough to detect  $\sim 3\%$  variations in oxygen content

D. A. Gilbert et al., *Phys. Rev. Mat.* **2**, 104402 (2018)



A single unit cell with a net magnetization of 40 emu/cc



SrRuO<sub>3</sub> (1 u.c.)/SrTiO<sub>3</sub> (3 u.c.)

Z. Cui, *Science Advances* **6**, eaay0114 (2020)