

## SOP 8

### Recommended Standard Operating Procedure for Medium Accuracy Calibration of Mass Standards by Modified Substitution

#### 1 Introduction



1.1 This SOP describes procedures to be followed for calibration and conformity assessment of mass standards for particular classes of documentary standards (e.g., NIST Class F, ASTM<sup>1</sup> Class 5, 6, 7 or OIML<sup>2</sup> Classes M<sub>1</sub>, M<sub>2</sub>, and M<sub>3</sub>) where the uncertainty is usually much smaller than the tolerance application provided the laboratory maintains standards and balances used for higher precision work. This procedure permits the metrologist to report that the weights being calibrated were compared against a reference standard with the results reported on the laboratory calibration certificate. The comparison is important because the built-in weights of a balance do not represent laboratory standards or provide metrological traceability unless they have been formally calibrated. If a State law or other regulation requires that field weights be compared against the State (or reference) standards, this procedure can be used to fulfill this requirement. It is suitable for calibration when moderate accuracy is required, and limits, but does not eliminate errors due to drift. The procedure incorporates measurement assurance steps to ensure the validity of the standards and the measurement process through the use of check standards. Decision criteria for uncertainty and tolerance evaluations include two components: 1) the expanded uncertainty, U, must be  $< 1/3$  of the applicable tolerances published in ASTM E617, OIML R111, and/or NIST Handbook 105-1 documentary standards and 2) the absolute value of the conventional mass correction value plus the expanded uncertainty must be less than the applicable tolerance to confidently state that mass standards are in or out of tolerance. If uncertainty to tolerance ratios are greater than required, SOP 7 (single substitution) or SOP 4 (double substitution) procedures are preferred. SOP 8 may be used for any nominal values provided adequate standards and equipment are available. Detailed measurement ranges, standards, equipment, and uncertainties for this SOP are generally compiled in a separate document in the laboratory.

Note: When using SOP 8, the laboratory often uses working standards that are equivalent or only slightly better than customer's weights. If this is the case, the working standards must have a higher level of calibration than the weights being calibrated. Therefore, the laboratory will need standards, balances, procedures, and uncertainties better than the customer weights and this procedure to calibrate the laboratory working standards.

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<sup>1</sup> ASTM International (formerly the American Society for Testing and Materials) publishes the E617 standard for mass specifications and tolerances.

<sup>2</sup> OIML is the International Organization for Legal Metrology. Weight classes are published in OIML R111, which is freely available at <http://www.oiml.org>.



## 1.2 Prerequisites

- 1.2.1 Valid calibration certificates with appropriate values and uncertainties must be available for all the standards used in the calibration. All standards must have demonstrated metrological traceability to the international system of units (SI), which may be to the SI, through a National Metrology Institute such as NIST.
- 1.2.2 Standards must be evaluated to ensure that standard uncertainties for the intended level of calibration are sufficiently small. Reference standards should not be used to routinely calibrate customer standards using this procedure.
- 1.2.3 Verify that the balance that is used is in good operating condition with sufficiently small process standard deviation as verified by a valid control chart or preliminary experiments to ascertain the performance quality when a new balance is put into service.
- 1.2.4 Verify that the operator is experienced in precision weighing techniques and has had specific training in SOP 7, SOP 8, SOP 29, and GMP 10.
- 1.2.5 Laboratory facilities must comply with the following minimum conditions to meet the expected uncertainty possible with this procedure and to comply with the balance manufacturer's operating conditions specified for the balance. The laboratory should have demonstrated environmental controls for a minimum of 24 hours before a calibration.

**Table 1. Environmental conditions.**

Echelon <sup>3</sup>	Temperature Requirements During a Calibration	Relative Humidity (%)
III	Lower and upper limits: 18 °C to 27 °C Maximum changes: ± 5 °C / 12 h and ± 3 °C / h	40 to 60 ± 20 / 4 h

- 1.2.6 As a practical guideline, a waiting time of 24 hours is recommended for weights calibrated with this procedure to become equilibrated in the laboratory. If weights are extremely hot or cold additional equilibration may be needed to address problems with condensation and frozen surfaces. Weights must be completely dry prior to calibration. Minimum equilibration times are provided in the following table.

<sup>3</sup> Echelon III corresponds to weights of Classes OIML M<sub>1</sub>, M<sub>2</sub>, and M<sub>3</sub>, NIST Class F or ASTM Classes 5, 6 and 7. Uncertainty values must be fully assessed if this procedure is attempted for any higher-class weights. This procedure does not provide adequate redundancy for OIML Classes E<sub>1</sub> or E<sub>2</sub>, ASTM Classes 000, 00, 0, or 1 and SOP 5 or SOP 28 must be used.

**Table 2. Stabilization time.**

Temperature Range for the Artifact	Minimum Equilibration Time
Inside upper or lower limits $> 18\text{ }^{\circ}\text{C}$ and $< 27\text{ }^{\circ}\text{C}$	None
Outside of upper or lower limits $< 18\text{ }^{\circ}\text{C}$ or $> 27\text{ }^{\circ}\text{C}$	24 hours/overnight

## 2 Methodology

### 2.1 Scope, Precision, Accuracy


This method is applicable to all lower echelon mass calibration provided that the uncertainty requirements can be met. The achievable precision using this procedure is appropriate, provided the expanded uncertainty of the measurement is no more than one-third of the permissible tolerance of the calibrated mass standard. The accuracy achievable with this procedure depends on the accuracy of the calibration of the working standards and the precision of the intercomparison.

### 2.2 Summary

The mass to be calibrated is compared with a calibrated working standard by a modified substitution procedure. The comparison may be made using a single-pan, an equal-arm, or a fully-electronic balance. The reference standard is placed on the balance to obtain a convenient reference point and a sensitivity test is conducted. The error (departure from nominal value) of the weight calibrated is determined by comparing its reading to the reading obtained for the reference standard. A weight is within tolerance when the absolute value of its error plus its uncertainty does not exceed the tolerance established for the class of weight.


### 2.3 Apparatus/Equipment

2.3.1 Single-pan (Option A and A<sub>1</sub>), full-electronic balance (Option B), or equal-arm balance (Option C) with sufficient capacity for the load calibrated and with resolution equal to or less than one-tenth of the applicable tolerance of the standards to be calibrated.

2.3.2 Calibrated working standards, of nominally equal mass to the unknown mass standards being calibrated. Mass standards must have an expanded uncertainty less than one-tenth of the tolerance calibrated. 

2.3.3 Calibrated sensitivity weights, and tare weights if needed, with current calibration certificates selected according to SOP 34.

2.3.4 Uncalibrated counterweights, *T*, of approximately the same mass as the standard weights (for option C).

2.3.5 Calibrated environmental equipment to monitor laboratory conditions and to perform buoyancy corrections if needed. See SOP 2 for appropriate accuracy limits. 

## 2.4 Procedure - Option A, Use of Single-Pan Mechanical Balance

- 2.4.1 Select a reference standard of the same nominal value as the weight being calibrated. Place the standard on the balance pan. Adjust the optical scale reading (See GMP No. 4) to approximately midscale using uncalibrated tare weights and the balance's coarse and fine Zero controls. This setting must not be altered during a measurement sequence. Record the reading as  $O_1$ .
- 2.4.2 Add a sensitivity weight equal to approximately one-quarter full scale reading and record reading as  $O_2$ .
- 2.4.3 Calculate the value of a scale division using the equation in 3.2. If it is within  $\pm 2\%$  of nominal value (usual case), or another value  $< 2\%$  of nominal stated by the laboratory, the nominal value of a division can be used for tolerance testing.
- 2.4.4 Remove the sensitivity weight and adjust the optical scale to account for the corrected value of the standard used.

Example: Suppose that the nominal range of the optical scale is 100 mg and that the reference standard has a correction of -2.5 mg. The optical scale is adjusted to read 47.5 mg when the standard is on the pan. Under this condition, the reading 50.0 mg represents the nominal mass of the reference standard. The direction and magnitude of the deviation from 50.0 mg indicates the actual deviation of the calibrated weight from nominal.

- 2.4.5 Remove the Standard.
- 2.4.6 Place the weight to be calibrated on the balance pan, read the optical scale and record the reading as  $X_n$ . The error in the weight is the amount by which the indication deviates from the mid-scale reading. If the weight indication is more than the mid-scale value, the weight is heavy by the indicated difference; if the indication is less than the mid-scale value, the weight is light. E.g., A scale indication of 30.1 mg will indicate that the calibrated weight is 19.9 mg lighter than nominal.
- 2.4.7 After several weights have been calibrated (no more than 10 unknown weights may be calibrated without rechecking the standard or check standard), put the standard on the balance pan and record the reading. The difference between this indication and the previous one for the standard indicates a balance drift. This drift will normally be very small. If the drift exceeds 5% to 10% (limits determined by the laboratory) of the tolerance applicable to the weights being calibrated or affects a measurement result to the extent that a weight may be out of tolerance, the measurement should be repeated and more frequent checks of the standard should be made or a more appropriate procedure should be used. The average drift may be monitored over time to be included as a component of the uncertainty; otherwise 5% to 10% of the applicable tolerance, as determined by the

laboratory, as a rectangular distribution may be included in the uncertainty calculations.

- 2.4.8 Readjust the optical scale at any time that a significant difference is observed when rechecking a standard.
- 2.4.9 Calculate the mass correction for the unknown weights using the appropriate equation in Section 3.

## 2.5 Procedure - Option A<sub>1</sub>, Use of Single-Pan Mechanical Balance

- 2.5.1 Select a reference standard of the same nominal value as the weight being calibrated. Place the standard on the balance pan. Adjust the optical scale reading (See GMP No. 4) to midscale using uncalibrated tare weights and the balance's coarse and fine Zero controls. This setting must not be altered during a measurement sequence. Record the reading as  $O_1$ .
- 2.5.2 Add a sensitivity weight equal to approximately one-quarter full scale reading and record reading as  $O_2$ .
- 2.5.3 Calculate the value of a scale division using the equation in 3.2. If the sensitivity is within  $\pm 2\%$  of nominal value (usual case) of the scale division), or another value  $< 2\%$  of nominal stated by the laboratory, the nominal value of a division may be used.
- 2.5.4 Remove the sensitivity weight and re-adjust the optical scale to obtain a midscale indication, if the indication has changed from that set in 2.5.1.
- 2.5.5 Remove the Standard.
- 2.5.6 Place the weight to be calibrated on the balance pan, read the optical scale, and record the indication as  $X_n$ . Using Eqn. (1) calculate the mass correction of the weight. The mass error is the deviation from the nominal value.
- 2.5.7 Monitor drift.

After several weights have been calibrated (no more than 10 unknown weights may be calibrated without rechecking the standard or check standard), put the standard on the balance pan and record the reading. The difference between this indication and the previous one for the standard indicates a balance drift. Evaluate and account for drift per Section 2.8.

- 2.5.8 Readjust the optical scale at any time that a significant difference is observed when rechecking a standard.
- 2.5.9 Calculate the correction of the unknown using the equation:


$$C_x = C_s + (X_n - O_1) \quad \text{Eqn. (1)}$$

## 2.6 Procedure - Option B, Use of Full Electronic Balance



- 2.6.1 Select a reference standard of the same nominal value as the weight being calibrated. Place the standard on the pan. Zero the balance and record the stable reading as  $O_1$ . A stopwatch may be used to monitor consistent timing of balance stability but is not required.
- 2.6.2 Add a calibrated sensitivity weight ( $sw \geq 2$  times the tolerance but not exceeding 0.5 % of the balance capacity) and record the reading as  $O_2$ . Verify whether the nominal scale division is within  $\pm 2$  % of nominal value of the scale division using the equation in 3.2. If so, the nominal value of the scale division may be used. This value may be monitored less frequently than each operation if stability of the sensitivity factor has been demonstrated and documented.
- 2.6.3 Remove the sensitivity weight and zero the balance,  $O_3$ , so weight differences,  $d$ , can be read directly from the balance indications.
- 2.6.4 Remove all weights from the balance pan.
- 2.6.5 Place the weight to be calibrated on the balance pan. Record the reading as  $X_n$ .
- 2.6.6 Monitor drift.

After several weights have been calibrated ((no more than 10 unknown weights may be calibrated without rechecking the standard and check standard), put the standard on the balance pan and record the reading. The difference between this indication and the previous one for the standard indicates a balance drift. Evaluate and account for drift per Section 2.8

- 2.6.7 Readjust the zero at any time that a significant difference is observed when rechecking a standard.
- 2.6.8 Calculate the mass correction for each weight using the equation: 

$$C_x = C_s + (X_n - O_1) = C_s + X_n, \text{ when } O_1 \text{ is zeroed} \quad \text{Eqn. (2)}$$

## 2.7 Procedure - Option C, Use of Equal Arm Balance

2.7.1 Select a reference standard of the same nominal value as the weight being calibrated. Place the standard on the left balance pan together with small, calibrated weights equal to the correction required for the standard, provided it is light. If needed, add sufficient counterweights to the right pan to obtain a sum of turning points of approximately twice the midscale value. If necessary, number the graduated scale such that adding weights to the left pan will increase the balance reading. Record the sum of the turning points as  $O_1$ .

2.7.2 Add an appropriate calibrated sensitivity weight to the left pan and record the sum of the turning points as  $O_2$ . Calculate the sensitivity using this equation:

$$\text{sensitivity} = \frac{CM_{sw}}{(O_2 - O_1)} \quad \text{Eqn. (3)}$$

where  $CM_{sw}$  is the conventional mass of the sensitivity weight.

2.7.3 Remove all weights from the left pan.

2.7.4 Place the weight to be calibrated on the left pan. If the standard used in 2.7.1 was heavy, add small correction weights to the left pan, equivalent to the correction required for the standard. Add small, calibrated tare weights as required to the left or right pan to obtain an approximate balance and record the sum of the turning points as  $X_n$ .

2.7.5 Calculate the mass correction of the calibrated weight(s) as follows.

2.7.5.1 If added tare weights are placed on the left pan ( $t_x$ ).

$$C_x = (X_n - O_1) \left[ \frac{CM_{sw}}{(O_2 - O_1)} \right] - CM_{t_x} \quad \text{Eqn. (4)}$$

2.7.5.2 If added tare weights are placed on the right pan ( $t_s$ ).

$$C_x = (X_n - O_1) \left[ \frac{CM_{sw}}{(O_2 - O_1)} \right] + CM_{t_s} \quad \text{Eqn. (5)}$$

2.7.6 Monitor drift.

After several weights have been calibrated (no more than 10 unknown weights may be calibrated without rechecking the standard or check standard), put the standard on the balance pan and record the reading. The difference between this indication and the previous one for the standard indicates a balance drift. Evaluate and account for drift per Section 2.8.

## 2.8 Drift Evaluation



Drift effects will normally be very small. If the drift exceeds 5 % to 10 % (limits determined by the laboratory, not to exceed 10 %) of the tolerance applicable to the weights being calibrated, or affects a measurement result to the extent that a weight may be out of tolerance, the measurement should be repeated and more frequent checks of the standard should be made or a more appropriate procedure should be used. The average drift may be monitored over time to be included as a component of the uncertainty; otherwise 5 % to 10 % of the applicable tolerance, as determined by the laboratory, as a rectangular distribution may be included in the uncertainty calculations.

## 2.9 Tolerance Evaluation



Compare the correction plus the expanded uncertainty of the calibrated weight(s) with the tolerance for the class of weights to which it belongs. If the absolute value of the correction plus the expanded uncertainty is numerically smaller than the tolerance, the weight is within tolerance. If the correction is larger than permissible, the weight is outside the tolerance and appropriate action should be taken. It is recommended that weights whose absolute value of the correction exceeds 75 % of the tolerance limit be adjusted closer to the nominal value where possible. Laboratories may set suitable alternative limits, taking care to ensure that the mass value plus (or minus) the uncertainty is within the tolerance limits.




**Table 3. Example of weighing sequence.**


Measurement No.	Weights on Pan	Observation
1	$S$	$O_1$
2	$S + sw$	$O_2$
3	$S$	$O_3$
4	$X_1$	$O_4$
5	$X_2$	$O_5$
6	$X_3$	$O_6$
7	$X_4$	$O_7$
8	$X_5$	$O_8$
9	$X_6$	$O_9$
10	$X_7$	$O_{10}$
11	$X_8$	$O_{11}$
12	$X_9$	$O_{12}$
13	$X_{10}$	$O_{13}$
14	$S_c$	$O_{14}$
15	$S$	$O_{15}$

### 3 Calculations

3.1 Air buoyancy corrections are generally not made with the modified substitution, although with the use of spreadsheets and the need to record environmental conditions, there is no reason why the buoyancy correction may not be routinely included (mass densities must be known or assumed). When performed, use SOP 2, Option B.

3.2 Evaluate the sensitivity of the balance: 

$$\text{sensitivity} = \frac{CM_{sw}}{(O_2 - O_1)} \quad \text{Eqn. (6)}$$

If the sensitivity error is less than 2 % of the nominal value of a division on the optical scale or the electronic range of operation, proceed with the modified substitution. If the sensitivity error is greater, SOP 7, Single Substitution may be acceptable. This value may be monitored less frequently on electronic balances if stability of the sensitivity factor has been demonstrated and documented. If corrections for sensitivity are not made, an uncorrected systematic error may be incorporated into the uncertainty but the balance sensitivity requires periodic evaluation; the uncertainty value may be calculated as 2 % of the applicable tolerance as the sensitivity is multiplied by the difference between the standard and the unknown ( $d$ ). 

3.3 Calculate the conventional mass correction,  $C_x$ , for the unknown weight as  $C_x = CM_i - N_x$ , according to the optional sequence used. In each case, the conventional mass corrections for the standard weight(s) are included.

**Table 4. Symbols used.**

Symbol	Description
$CM_i$	Conventional mass of weight $i$
$N_s$	Nominal value of the standard, $S$
$N_x$	Nominal value of the unknown, $X$
$C_i$	Conventional mass correction of weight $i$
$d$	Measured difference between $X$ and $S$

- 3.4 Calculate the conventional mass correction of each unknown weight as follows if the correction for the standard IS NOT used in setting a reference point on the balance:



$$C_x = C_s + d \quad \text{Eqn. (7)}$$

$$C_x = C_s + (X_n - O_1) \quad \text{Eqn. (8)}$$

Note: If an electronic balance is used and zeroed with the standard on the balance,  $O_1$  is "0" and  $d$  becomes the  $X_n$  balance reading.

- 3.5 Calculate the conventional mass correction of each unknown weight as follows if the correction for the standard IS used in setting a nominal reference point on the balance:

$$C_x = (X_{\text{balance reading}} - N_{\text{nominal reference point}}) \quad \text{Eqn. (9)}$$

Note: In this case the standard and its correction are used to artificially *set* a perfect nominal reference point for use in comparing the unknown weights.

- 3.6 If tare weights and unequal nominal values are used, use the following equation for modifying section 3.3:



$$C_x = C_s + CM_{ts} - CM_{tx} + (X_n - O_1) + N_s - N_x \quad \text{Eqn. (10)}$$

#### 4 Measurement Assurance



- 4.1 Duplicate the process with suitable check standards for each nominal load or a designated number of check standards per balance (See GLP 1, SOP 9, and SOP 30).
- 4.2 Evaluate the value against the expected limits and plot the check standard value on the control chart to monitor changes over time.

All values must be entered in the control chart, even if failing this statistic, unless a mistake (i.e., typographical error) is identified and corrected, to ensure the variability obtained for the process is not unduly reduced over time. The observed value of the check standard is compared to the accepted mean value of the check standard and divided by the standard deviation for the check standard observations over time.

A t-test may be incorporated to check the observed value of the check standard against the accepted value using the following equation and a 95 % confidence level. The t-statistic is calculated for stability analysis. This equation monitors stability over time, but should not be used to assess for bias. A calculated t-value less than two is within the warning limits of the process. A calculated t-value between two and three represents a value between the warning limits and control/action limits. A calculated t-value exceeding three represents a value outside of the control/action limits and suitable action must be taken. Calculated values of the t-statistic may also be monitored over time to determine the presence of drift.

$$t = \frac{(S_c - \bar{S}_c)}{s_p} \quad \text{Eqn. (11)}$$

- 4.3 Check standard measurement results obtained over time are used to calculate the standard deviation of the measurement process,  $s_p$ .
- 4.4 The mean value of the check standard over time is also compared to an appropriate reference value of the check standard with respect to their applicable expanded uncertainties to evaluate bias and drift over time. Excessive drift or bias must be investigated and followed with suitable corrective action. See SOP 9, Section 3.5.3 and Section 8.16 for assessment methodology.
- 4.5 Where SOP 9 is followed and check standards are used for 2 to 3 nominal values per balance, more frequent calibration intervals may be needed to monitor the working standards and the larger standard deviation of the nominal values bracketing the nominal value should be used. If check standards were already checked on a given day and found to be in control, additional evaluations may be conducted, but are not required.

## 5 Assignment of Uncertainty

The limits of expanded uncertainty,  $U$ , include estimates of the standard uncertainty of the mass standards used,  $u_s$ , estimates of the standard deviation of the measurement process,  $s_p$ , and estimates of the effect of other components associated with this procedure,  $u_o$ . These estimates should be combined using the root-sum-squared method (RSS), and the expanded uncertainty,  $U$ , reported with a coverage factor of two ( $k = 2$ ), to give an approximate 95 % level of confidence. See SOP 29 for the complete standard operating procedure for calculating the uncertainty.

- 5.1 The expanded uncertainty for the standard,  $U$ , is obtained from the calibration certificate. The combined standard uncertainty,  $u_c$ , is used and not the expanded uncertainty,  $U$ , therefore the reported uncertainty for the standard will usually be divided by the coverage factor  $k$ . Where the coverage factor or confidence interval is not given, the laboratory should either contact the calibration provider to obtain the correct divisor or use a value of  $k = 2$ , assuming that the expanded uncertainty was reported with an approximate 95 % confidence interval (95.45 %).


- 5.2 Standard deviation of the measurement process from control chart performance (See SOP No. 9.) The value for  $s_p$  is obtained from the control chart data for check standards using modified substitution measurements. Where the standard deviation of the measurement process from the control chart is less than the resolution of the balance being used, the laboratory may round up to the value of the balance division or use the larger of the standard deviation of the process or the following estimate for repeatability is used to represent the standard deviation of the process:

$$s_p = \frac{d}{\sqrt{3}} \approx 0.6d \quad \text{Eqn. (12)}$$

- 5.3 Uncertainty associated with allowable drift. Include the monitored average drift for each balance and procedure as a rectangular distribution, or include a value that is between 5 % and 10 % of the applicable tolerance (limit set by laboratory policy) for the weight, again as a rectangular distribution. Whenever the drift exceeds the limit of drift stated by the laboratory, conduct a root cause analysis to determine the cause; this situation may require fewer weights to be calibrated in the weighing series, service of the balance, better environmental controls, additional training, and practice by the metrologist, or increasing the allowable drift limits (not to exceed 10 %).
- 5.4 Uncertainty associated with allowable sensitivity error,  $u_{se}$ . This procedure allows for up to 2 % error (stated by the laboratory) in the optical or electronic range of use. This may result in calibration errors up to 2 % of the applicable tolerance. This is potentially another uncorrected systematic error that may be treated as a rectangular distribution. This value may be monitored less frequently than each operation if stability of the sensitivity factor has been demonstrated. Whenever the sensitivity error exceeds the limit stated by the laboratory, conduct a root cause analysis to determine the cause; this situation may require service of the balance, better environmental controls, additional training, and practice by the metrologist, or increasing the allowable sensitivity error limits (not to exceed 2 %).
- 5.5 Uncertainty associated with uncorrected air buoyancy. When buoyancy corrections are not made, the resulting uncorrected systematic error may be treated as a rectangular distribution, with the magnitude of the maximum uncorrected buoyancy correction determined using equations provided in SOP 2. The uncertainty associated with air density and its associated factors may be considered negligible for this procedure or may be calculated using the options provided in SOP 4 or 5.
- 5.6 Uncertainty associated with bias that is observed in the check standards as determined through analysis of the control charts. When bias is observed in the control charts, it must be assessed according to the equations provided in SOP 29 and may be incorporated as an uncorrected systematic error using the equations in SOP 29.
- 5.7 Example components to be considered for an uncertainty budget table are shown in the following table.

**Table 5. Example uncertainty budget table.**

Uncertainty Component Description	Symbol	Source	Typical Distribution
Uncertainty of the standard mass(es) (5.1)	$u_s$	Calibration certificate	Normal divided by coverage factor
Accepted standard deviation of the process (5.2)	$s_p$	Control chart, standard deviation chart	Normal or estimated rectangular if actual $s_p$ is less than balance resolution
Uncertainty of the allowable drift (5.3)	$u_{drift}$	5 % to 10 % of the tolerance (stated by lab)	Rectangular
Uncertainty of the allowable sensitivity error (5.4)	$u_{se}$	SOP 8, < 2 % of the sensitivity times the applicable tolerance	Rectangular
Uncertainty of the maximum magnitude of the buoyancy correction (5.5)	$u_b$	SOP 2	Rectangular
Uncertainty associated with bias (5.6)	$u_d$	Control chart, proficiency tests	See SOP 29

5.8 Draft a suitable uncertainty statement for the certificate. For example: 

The uncertainty reported is the root sum square of the standard uncertainty of the standard, the standard deviation of the process, and the uncertainty associated with the buoyancy corrections, multiplied by a coverage factor of 2 ( $k = 2$ ) for an approximate 95 percent confidence interval. Factors not considered in the evaluation: magnetism (weights are considered to meet magnetism specifications unless measurement aberrations are noted), balance eccentricity and linearity (these factors are considered as a part of the measurement process when obtaining the standard deviation of the process when using a check standard with adequate degrees of freedom).

NOTE: Where inadequate degrees of freedom are available,  $k$ , is determined using the appropriate degrees of freedom and the 95.45 % column in the table from Appendix A of NISTIR 6969, SOP 29.

6 Certificate 

6.1 Report results as described in SOP No. 1, Preparation of Calibration Certificates. Report the conventional mass, environmental conditions during the calibrations, and calculated expanded uncertainties with coverage factor(s).

6.2 Conformity assessment. 

Evaluate compliance to applicable tolerances as needed or required by the customer or by legal metrology requirements. Decision criteria for uncertainty and tolerance evaluations include two components: 1) the expanded uncertainty,  $U$ , must be < 1/3 of the applicable tolerances published in ASTM E617, OIML R111, and/or NIST Handbook 105-1 documentary standards and 2) the absolute value of the

conventional mass correction value plus the expanded uncertainty must be less than the applicable tolerance to confidently state that mass standards are in or out of tolerance. Compliance assessments must note the applicable documentary standard and which portions of the standard were or were not evaluated.

## Appendix - Modified Substitution Data Sheet



### Laboratory data and conditions:

Operator		Before	After
Date		Temperature	
Balance		Pressure	
Load		Relative Humidity	
Standard deviation of the process, from control chart, $s_p$		Degrees of Freedom	

### Mass standard(s) data:

ID	Nominal	Mass Correction*	Expanded Unc: from cal. certificate	Unc: $k$ factor	Density g/cm <sup>3</sup>
$S$					
$t_S$					
$\bar{X}$		TBD	TBD	TBD	
$t_x$					
$S_c$					
$t_{S_c}$					
$sw$					

\*Mass Correction = True Mass with buoyancy correction. Mass Correction = Conventional Mass with no buoyancy correction.

### Observations:

Observation No.	Weights (Insert ID of X)	Balance Observations, Units
Time:		
1 ( $O_1$ )	$S$	
2 ( $O_2$ )	$S + sw$	
Error < 2 % of optical scale or electronic range? <input type="checkbox"/> Yes <input type="checkbox"/> No		
3 ( $O_3$ )	$S$	
4 ( $O_4$ )	$X_1$	
5 ( $O_5$ )	$X_2$	
6 ( $O_6$ )	$X_3$	
7 ( $O_7$ )	$X_4$	
8 ( $O_8$ )	$X_5$	
9 ( $O_9$ )	$X_6$	
10 ( $O_{10}$ )	$X_7$	
11 ( $O_{11}$ )	$X_8$	
12 ( $O_{12}$ )	$X_9$	
13 ( $O_{13}$ )	$X_{10}$	
14 ( $O_{14}$ )	(See Section 4.5) $S_c$	
15 ( $O_{15}$ )	$S$	
Time:	Drift < Specified Tolerance Limit? <input type="checkbox"/> Yes <input type="checkbox"/> No	
Check Standard in Control?	<input type="checkbox"/> Yes <input type="checkbox"/> No	

Up to 10 unknown weights may be checked with this procedure if the drift is less than tolerance limits specified by the laboratory.

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