

Function Secret Sharing for PSI-CA: With Applications to Private Contact Tracing

Speaker:

Steve Lu, CEO, Stealth Software Technologies, Inc.

Contact: steve@stealthsoftwareinc.com

Joint Work with:

Samuel Dittmer

Yuval Ishai

Rafail Ostrovsky



Mohamed Elsabagh

Nikolaos Kiourtis

Brian Schulte

Angelos Stavrou

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Intro

Our Approach

- **We describe new methods of increasing accuracy and privacy in decentralized contact tracing**
- **Key insight**
 - **Accuracy**: Context-aware risk score attached to tokens
 - **Robustness**: Hash location+time with token in TEE for hardening against malicious context attacks
 - **Privacy**: New cryptographic protocol that hides infected tokens and only reveals weighted risk score

mSense App – Decentralized Contact Tracing with Extensions

Key Innovations	High Level System Requirements
<p>1. Tracking risk of infection; not tracking people</p> <ul style="list-style-type: none">•Does NOT expose all contacts•Does expose probable exposure <p>2. Hardware proximity sensing and geolocation</p> <ul style="list-style-type: none">•Edge anonymization for data at rest and in transit•Server-side cryptographic calculations on anonymized users and locations <p>3. Fully encrypted database AND computation</p> <ul style="list-style-type: none">•Fast updates with parallel scaling•Data, queries, and responses are ALL encrypted; including from servers	<p>1. High Accuracy</p> <p>2. High Scalability</p> <p>3. Strong Privacy</p> <p>4. Robustness</p>

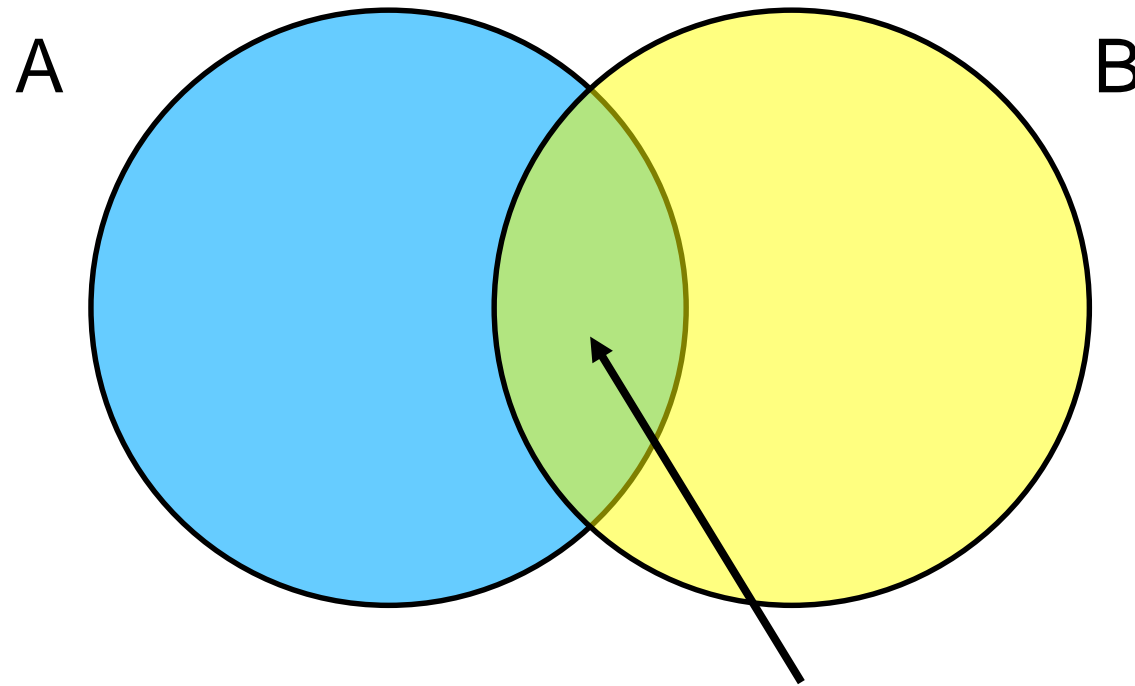
		Centralized [TraceTogether,...]	Decentralized [D3-PT, Apple/Google, PACT,...]	Epione [TSS+20]	CleverParrot [CKL+20]	This Work [mSense/ PSI-WCA]
Servers	Trusted Server	Yes	No	No	No	No
	Number of Servers	1	1	2	1	2
Privacy	Social Graph	Red	Green	Green	Green	Green
	Server	Red	Green	Green	Green	Green
	User-to-user	Green	Red	Green	Red	Green
Robustness Against	Relay	Red	Red	Red	Red	Green
	Replay	Red	Yellow	Yellow	Green	Green
	Upload Omission	Yellow	Red	Yellow	Feature	Green
	Trace Omission	Yellow	Red	Red	Red	Green

		Centralized [TraceTogether,...]	Decentralized [D3-PT, Apple/Google, PACT,...]	Epione [TSS+20]	CleverParrot [CKL+20]	This Work [mSense/ PSI-WCA]
<i>Tracing Cost</i>	User to Server Comm	$O(n)$	N/A	$O(n \log N)$	N/A	$O(nk)$
	Server to User Comm	$O(1)$	$O(N)$	$O(n)$	$O(N')$	$O(1)$
	User Crypto Work	N/A	Non-crypto $O(N)$ match	$O(n)$ asym	$O(N')$ asym	$O(n)$ sym
	Server Crypto Work	Non-crypto match	N/A	$O(nN)$ asym	N/A	$O(N)$ sym
	Rounds	1	0.5	2	0.5	1
Result	Result Returned	Yes/No	All "infected tokens"	Count of exposures	Tokens of exposures	Weighted risk score
Underlying Crypto	Primary Crypto Tools	Central trust	PRF-style "PSI"	DH-style PSI- CA plus 2PIR	DH-style PSI	PSI-(W)CA from FSS



Private Set Intersection

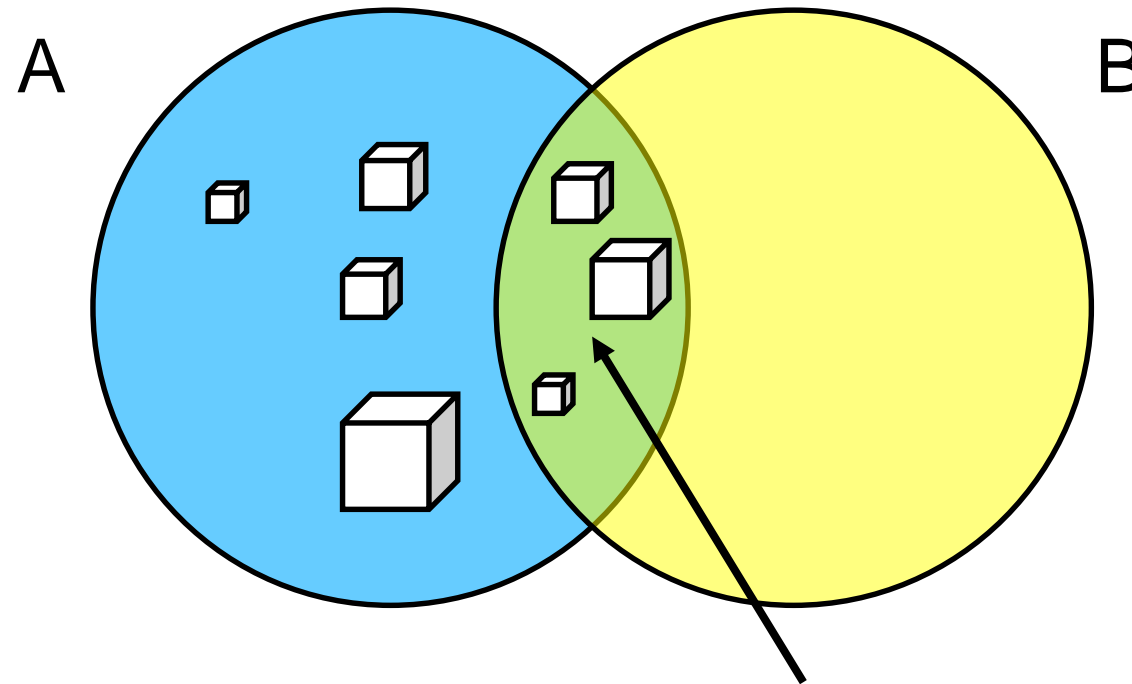
Private Set Intersection [M86, HFH99, FNP04, KS04, FIPR05,...]



Reveal only the intersection, hide non-intersected data



Private Set Intersection – Weighted Cardinality (PSI-WCA)



Reveal only the size intersection, hides the intersection and non-intersected data

A = Set of tokens I've received + mSense weights

B = Set of tokens of infected individuals

PSI-WCA provides weighted risk score!

Putting It Together

This work: Building PSI-(W)CA From Function Secret Sharing

What is Function Secret Sharing [GI14, BGI15, BGI16,...]?

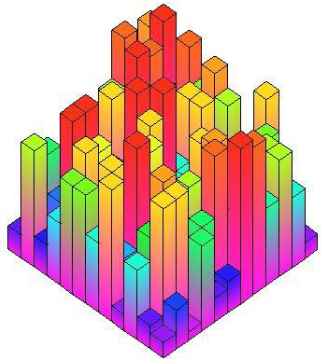
- Crypto protocol to split a function F into F_1 and F_2 such that $F_1(x)+F_2(x) = F(x)$ and individually F_1, F_2 **reveal nothing** about F

Theorem [GI14]: Sharing a point function P can be done using only symmetric-key crypto (e.g. AES)

$$P(x) = \begin{cases} b & \text{if } x=a \\ 0 & \text{otherwise} \end{cases}$$

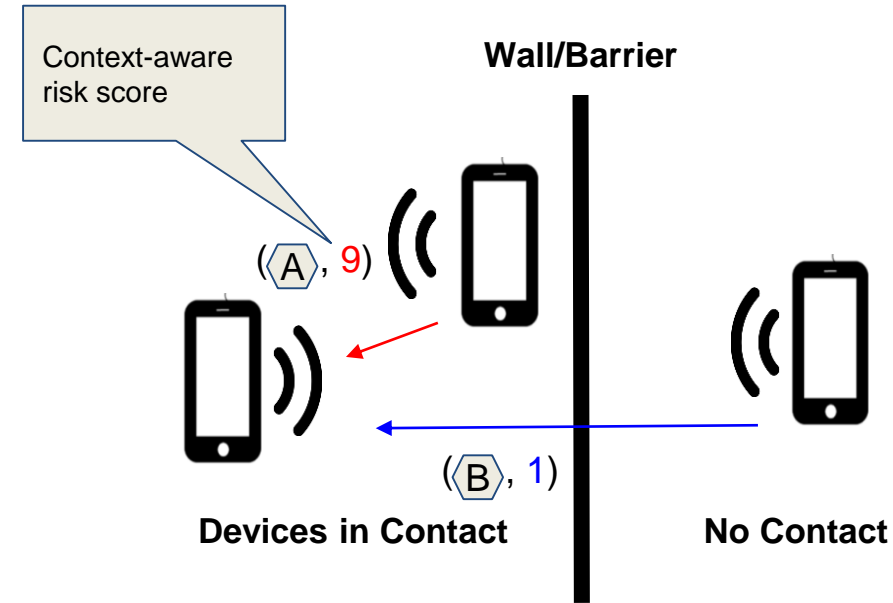
Token

Weight



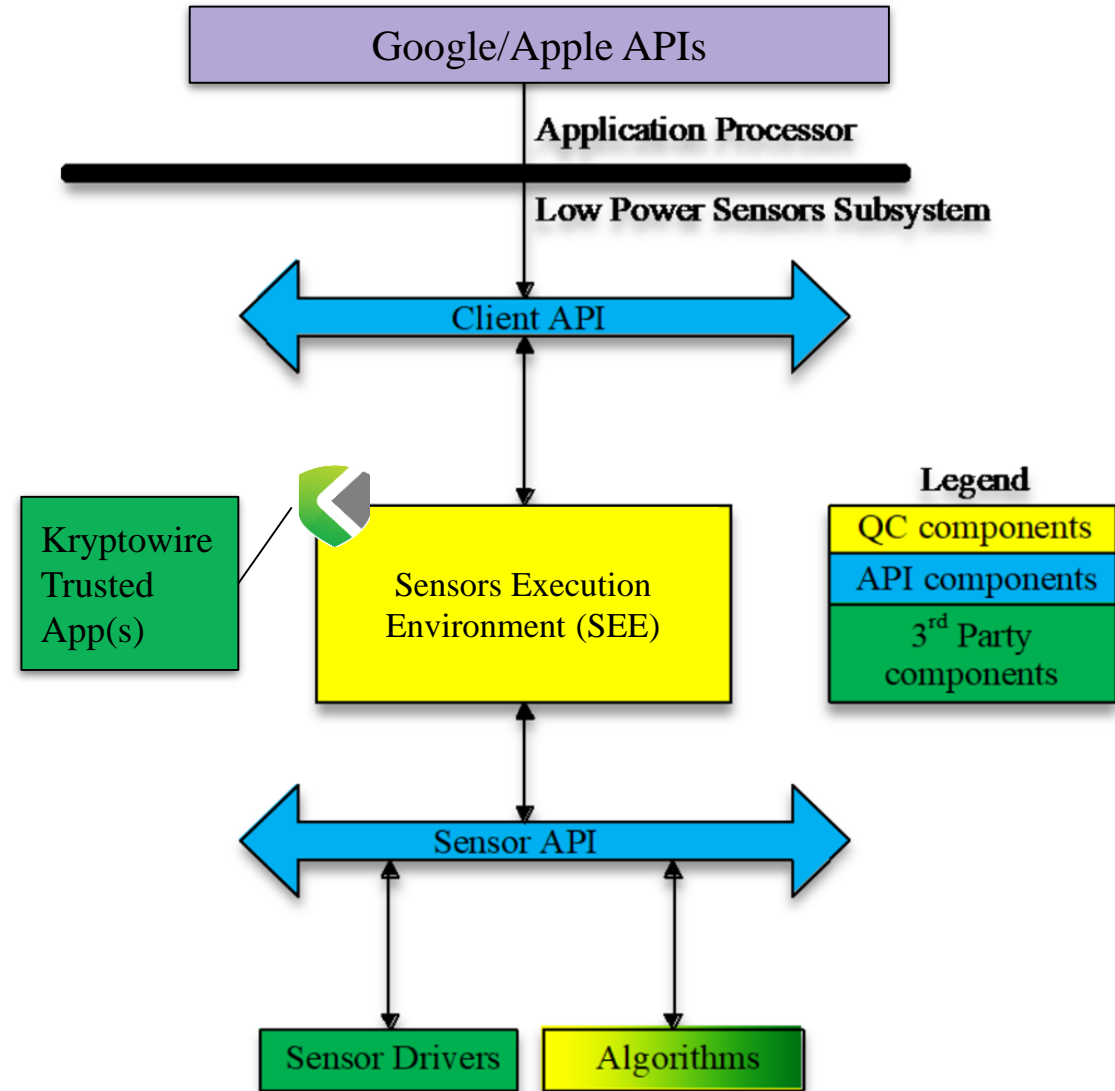
Situational Accuracy

- Improved sensor timings via chipset level access and experience
- Use of additional modalities to establish trusted location, sensor assisted positioning for more accurate location
- Utilize APIs to perform barrier detection (WiFi, Audio, etc)
- Context detection and baselining



Sensory Accuracy

- Access to the chipset level sensing environments with raw sensor data to assist in correcting for differences across APIs & Devices
- Chipset level applications work on wearables & mobile phones
- Access to raw sensory data and ability to load custom fusion algorithms



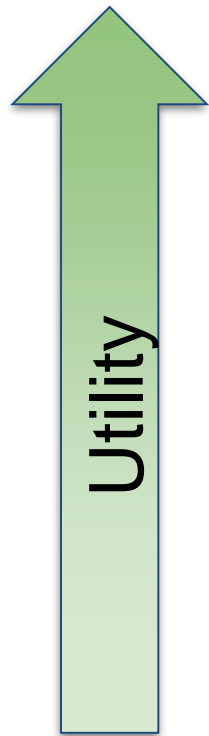
Building PSI-(W)CA From Function Secret Sharing

- For each token a_i , phone splits P_i into $P_{i,1}$ and $P_{i,2}$, sends each $P_{i,b}$ to server b (two servers)
 - Split server model has a long theoretical history (e.g. [CGKS95]) and recently used to great effect in practical privacy technologies (e.g [Prio])
- Each server b computes sum over all N infected tokens y_j , all n phone splits P_i :

$$\text{response}_b = \sum_{i=1}^n \sum_{j=1}^N P_{i,b}(y_j)$$

Sum of the responses = weighted risk score!

- Naïve computation is $O(nN)$, we also use careful combinatorial hashing to reduce server work



Utility

+ Client can analyze matched tokens
- Leaks matches
- No token context



Reveal all infected tokens
(Apple/Google, D3-PT)



+ Hides token match while providing count
- Counts alone gives no context or risk data

Reveal count of infected tokens encountered (Epione)



Reveal sum of context-aware weights
(Kryptowire + Stealth)



"Trusted"
Reveal yes/no

+ Hides everything
- Yes/no alone not useful in metropolitan areas

- **Tech: Private Set Intersection - Weighted Cardinality (PSI-WCA) via FSS**
 - Ideal tradeoff between privacy and utility for contact tracing
 - Unique Feature: Weights allow for encoding of context-aware risk data
 - Provides a useful risk score, leaks nothing else
 - One round, symmetric-key PSI, servers response 1 int



Privacy

Thank You!

Paper

arXiv: <https://arxiv.org/abs/2012.13053>