

**Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support**

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**Collaborators: Jian Cao, Gregory Olson, NIST, NIU and Others**

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**Workshop on Quantification of Uncertainties in Material Science**

**NIST, Gaithersburg, MD, January 14-15, 2016**

**Organized by [Maria Emelianenko \(GMU\)](#), [Igor Levin \(NIST\)](#) and [Qiang Du \(Columbia\)](#)**

**Northwestern Engineering**

Quotation from “[Making a World of Difference: Engineering Ideas into Reality \(An NAE Report\)](#)”

“Technological advances made over just a few decades are boosting economies, feeding the hungry, and healing the sick. .... New vaccines hold out the promise for tackling scourges like malaria and some cancers, while doctors save lives by replacing diseased heart valves—in some cases without open-heart surgery. ....

All these advances have come through engineering carried out in companies, universities, and national laboratories. Those efforts have created new materials like nanotubes and [high-strength alloys, manufacturing technologies like 3-D printing, software and algorithms for harnessing the power of supercomputers and mining vast stores of data](#), and countless other innovations. [Yet these examples barely scratch the surface of the remarkable changes wrought over the last quarter century.](#)”

[On October 7-9, 2015, the U.S. National Committee on Theoretical and Applied Mechanics](#)

(USNC/TAM) held a Workshop on [Predictive Theoretical and Computational Approaches for Additive Manufacturing](#) in the [US National Academies, Washington, DC](#). The three-

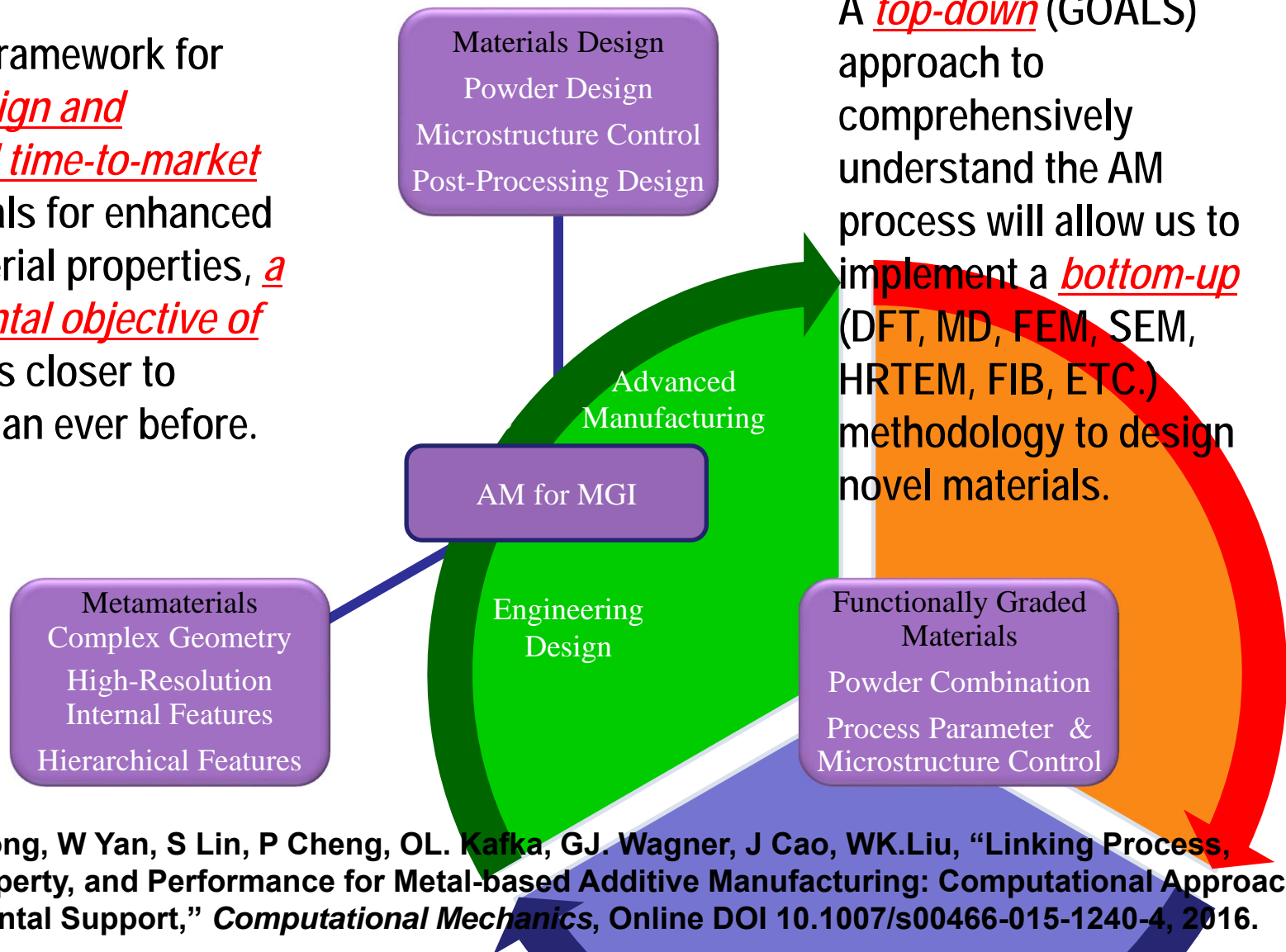
day workshop featured 24 presentations from speakers in academia, industry, and government labs. 50 experts attended the workshop in person, 200 joined through the webinar and over 2,000 viewers have already watched the video sessions. Please noted that the 190+ online viewers of the workshop was the highest viewing audience for the National Academies in-house video webcasting to date. We welcome you to visit the USNC/TAM site

[\(http://sites.nationalacademies.org/pga/biso/IUTAM/\)](http://sites.nationalacademies.org/pga/biso/IUTAM/) where you will be able to access the speakers’ session slides and videos.

**Additive Manufacturing (AM) for Materials Genome initiative (MGI)**

A stable framework for rapid design and improved time-to-market of materials for enhanced bulk material properties, a fundamental objective of the MGI, is closer to fruition than ever before.

A top-down (GOALS) approach to comprehensively understand the AM process will allow us to implement a bottom-up (DFT, MD, FEM, SEM, HRTEM, FIB, ETC.) methodology to design novel materials.



J Smith, W Xiong, W Yan, S Lin, P Cheng, OL. Kafka, GJ. Wagner, J Cao, WK.Liu, "Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support," *Computational Mechanics*, Online DOI 10.1007/s00466-015-1240-4, 2016.

## The materials system

## The equation

Materials system properties =  $A(\text{Building blocks, Interactions, Structure})$

↓  
Materials system genomes =  $A(\text{Archetypes, Interactions, Conformation})$

Materials system property is the entirety of the apparent property information that the material contains

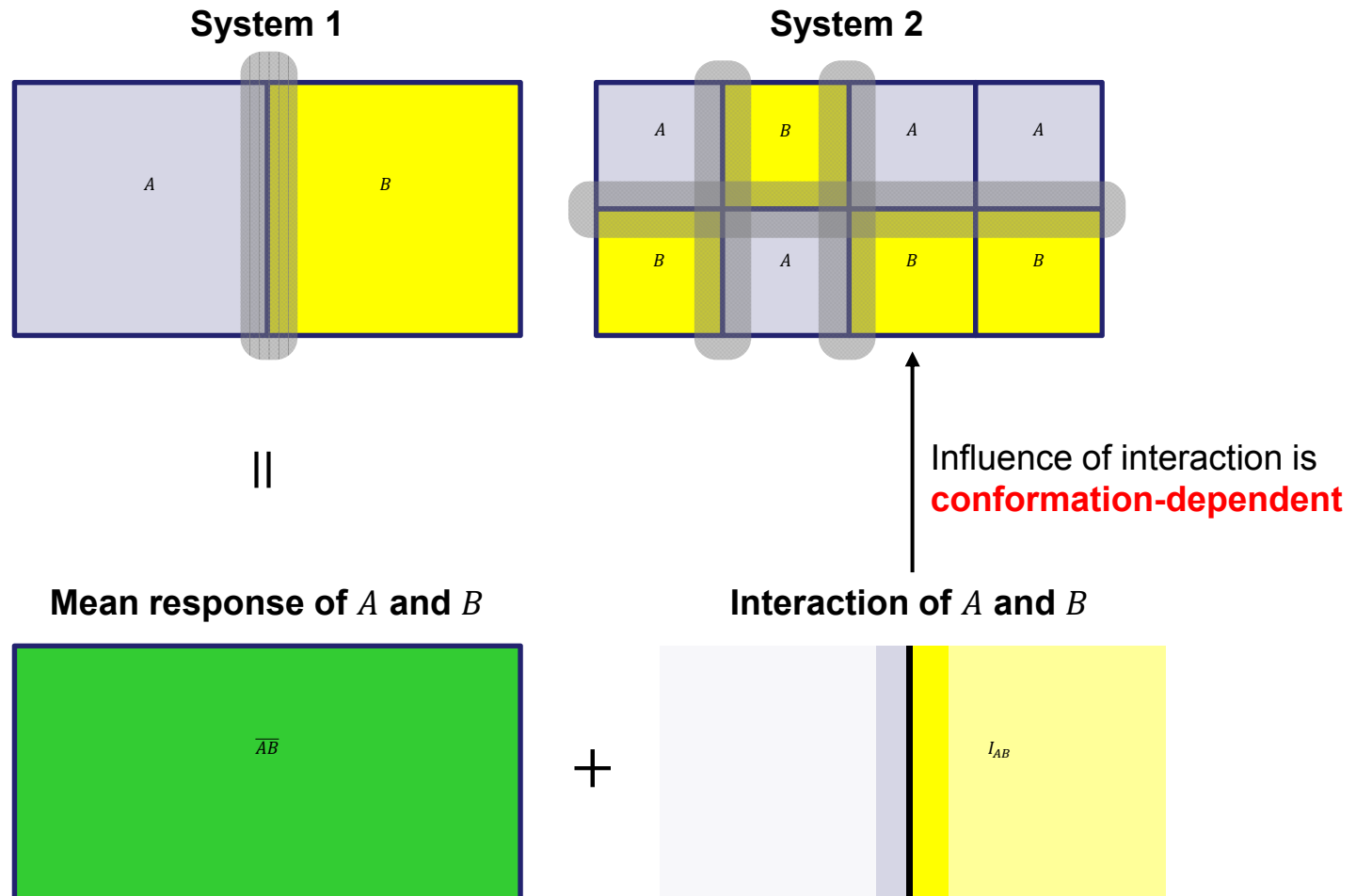
## Takeaways: the materials system depends on

- Building blocks of the material (individual components, phases),
- Interactions of the archetypes (e.g. chemistry, friction),
- The structural configuration of the archetypes
- The *assembly function*  $A$ , which includes material/structure processing
- Write a design theory with uncertainty quantification to wrap around the above

Greene, M., Y. Li, W. Chen, and W.K. Liu. The **archetype-genome exemplar** in molecular dynamics and continuum mechanics. *Computational Mechanics*, 2014.

KI Elkhodary, MS Greene, S Tang, T Belytschko, WK Liu. **Archetype-blending continuum theory**. *Computer Methods in Applied Mechanics and Engineering*, 2013

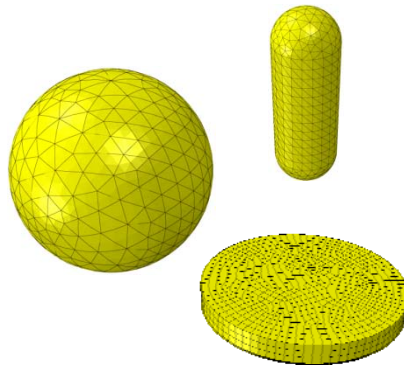
# Decomposition of systems



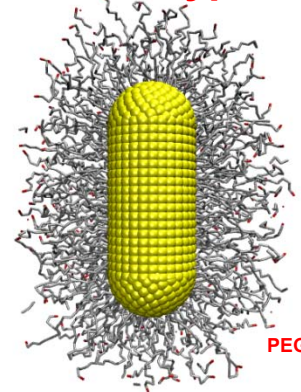
**Selection of archetypes via molecular simulation and from data base**

**Genome: targeted delivery of drugs**

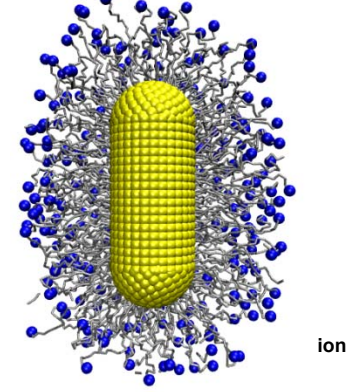
**First generation Archetypes**



**Second generation Archetypes**



**Third generation Archetypes**



**Nano-Materials**

- Material design
- Water solubility
- Biocompatibility

- Maximize delivery
- Stealth (passive)
- Active targeting

- Environment-response
- Dynamics properties
- Biological or external cues
- Theranostic abilities

**Biological challenges**

- Unstable
- Removal by MPS
- Poor tumor targeting

- Overreliance on EPR effect
- No “universal” antigen
- Active targeting is disappointing
- <10% dose in tumor

- No “universal” design principle

Evolution of nanoparticle design, highlighting the interplay between evolution of nanomaterial design and fundamental nano-bio studies.

Abbreviations: Ab, antibody; EPR, enhanced permeation and retention; MPS, mononuclear phagocyte system;

**PEG, poly(ethylene) glycol.**

**Bao, Liu et al. 2014, Journal of The Royal Society Interface 11 (97), 20140301**

## Northwestern Engineering

**(b)** Nanoparticles are segregated from red blood cells, increasing their interaction with the endothelium, leading to their removal from circulation.

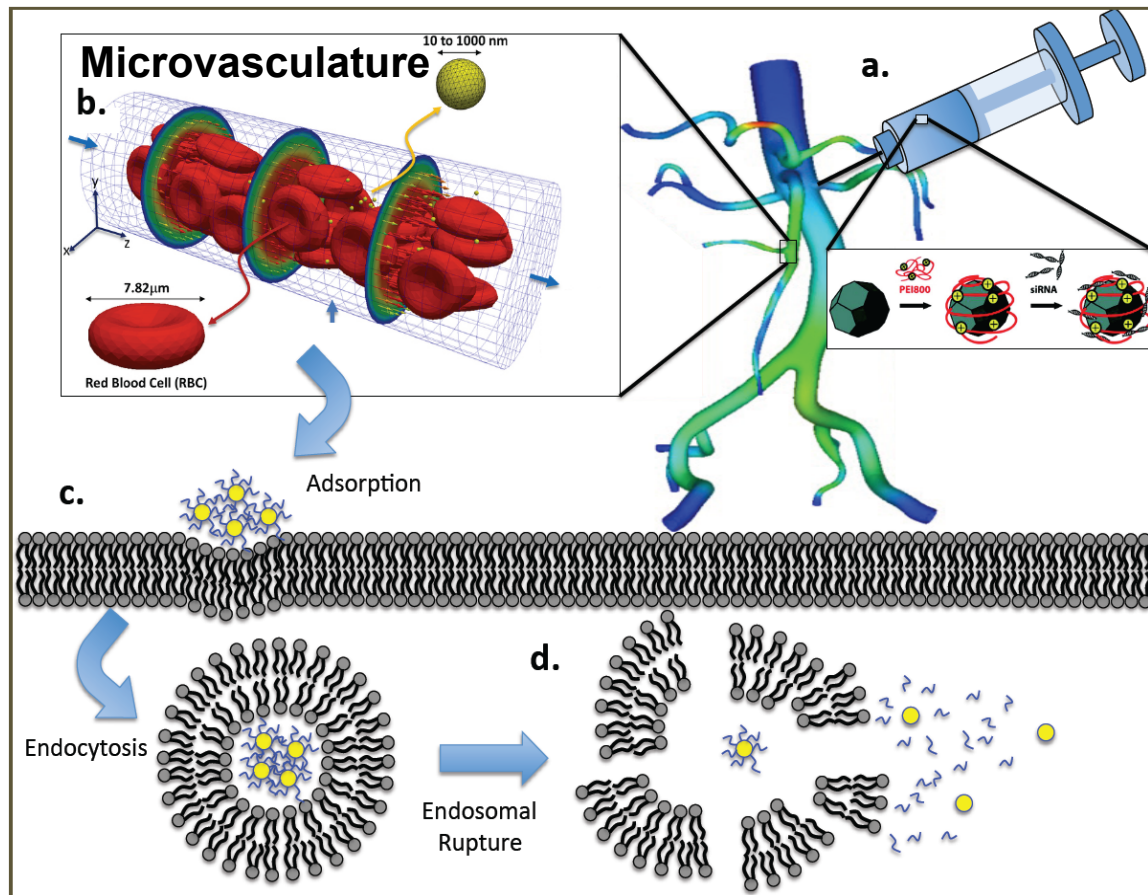
**(Modeling and Simulation)**

**(c)** Nanoparticles diffuse through the extracellular matrix;

adsorbing onto the surface of a target cell;

nanoparticles are then endocytosed from the lipid membrane.

**(Modeling and Simulation)**



**(a)** A solution containing nanoparticle delivery platforms is injected into a patient's circulatory system. **(Building Blocks or Archetypes)**

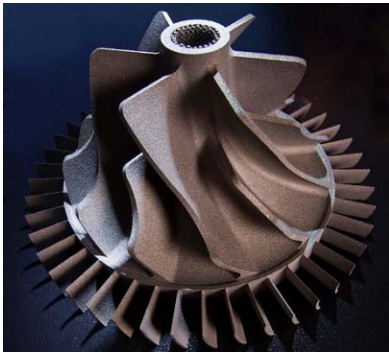
**(d)** The endosome containing the drug-delivery complex ruptures, releasing the therapeutic agents into the cytoplasm.

When released from the endosome, the nanoparticle cargo may be dissociated due to the pH environment change.

**(Modeling and Simulation)**  
**(\*Genome\*)**

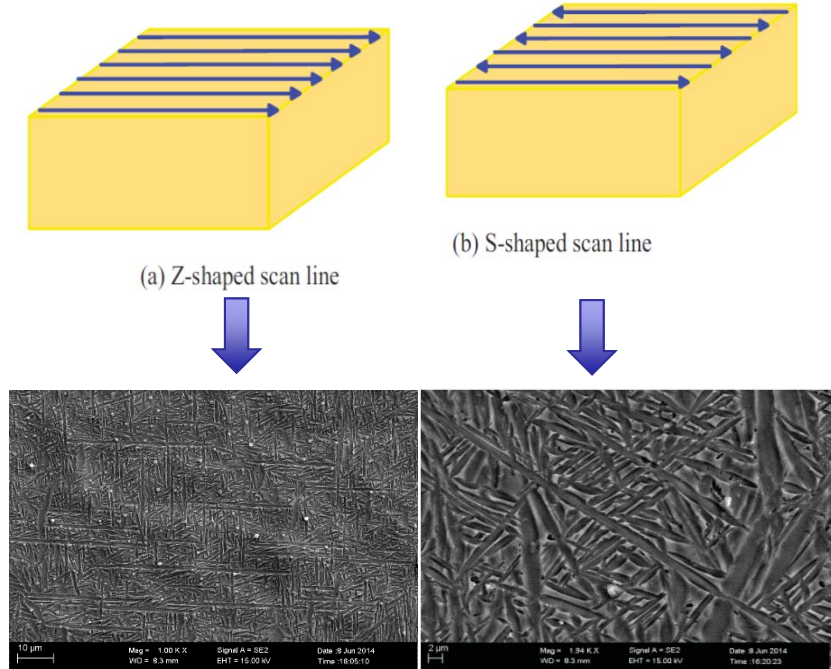
**Y. Li, W Stroberg, TR Lee, HS Kim, H, Man, D. Ho, P. Decuzzi, WK Liu, "Multiscale Modeling and Uncertainty Quantification in Nanoparticle mediated Drug/Gene Delivery," *Computational Mechanics on Nanomedicine*, (2014). TR Lee, AM Kopacz, WK Liu, P Decuzzi, "On the near-wall accumulation of injectable particles in the microcirculation: smaller is not better," *Scientific Reports*, 2013. TR Lee, WK Liu, et al., "Quantifying uncertainties in the microvascular transport of nanoparticles," *Biomechanics and Modeling in Mechanobiology*, 2014. Y Li, Y Lian, LT. Zhang, WK Liu, "Cell and Nanoparticle Transport in Tumor Microvasculature: the role of size, shape and surface functionality of nanoparticles," *Interface Focus*, 6 (1), 20150086, 2015.**

**1. Complex geometry**



**2. Control microstructure**

W Ge et al., 2014. SFF



**3. Design materials**



$\% \text{Powder \#1} + \% \text{Powder \#2} + \% \text{Powder \#3}$

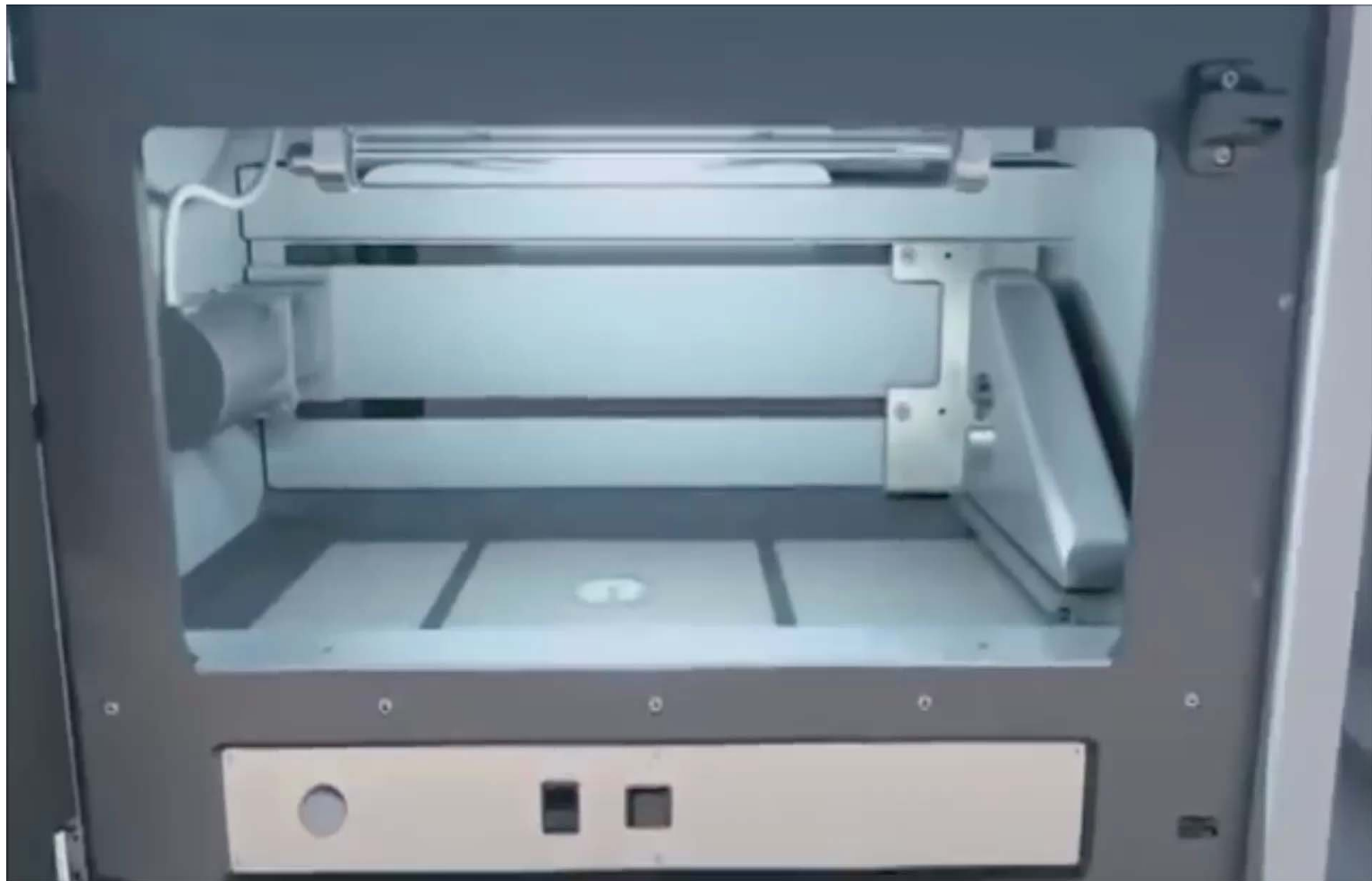


Unique Powder Combination

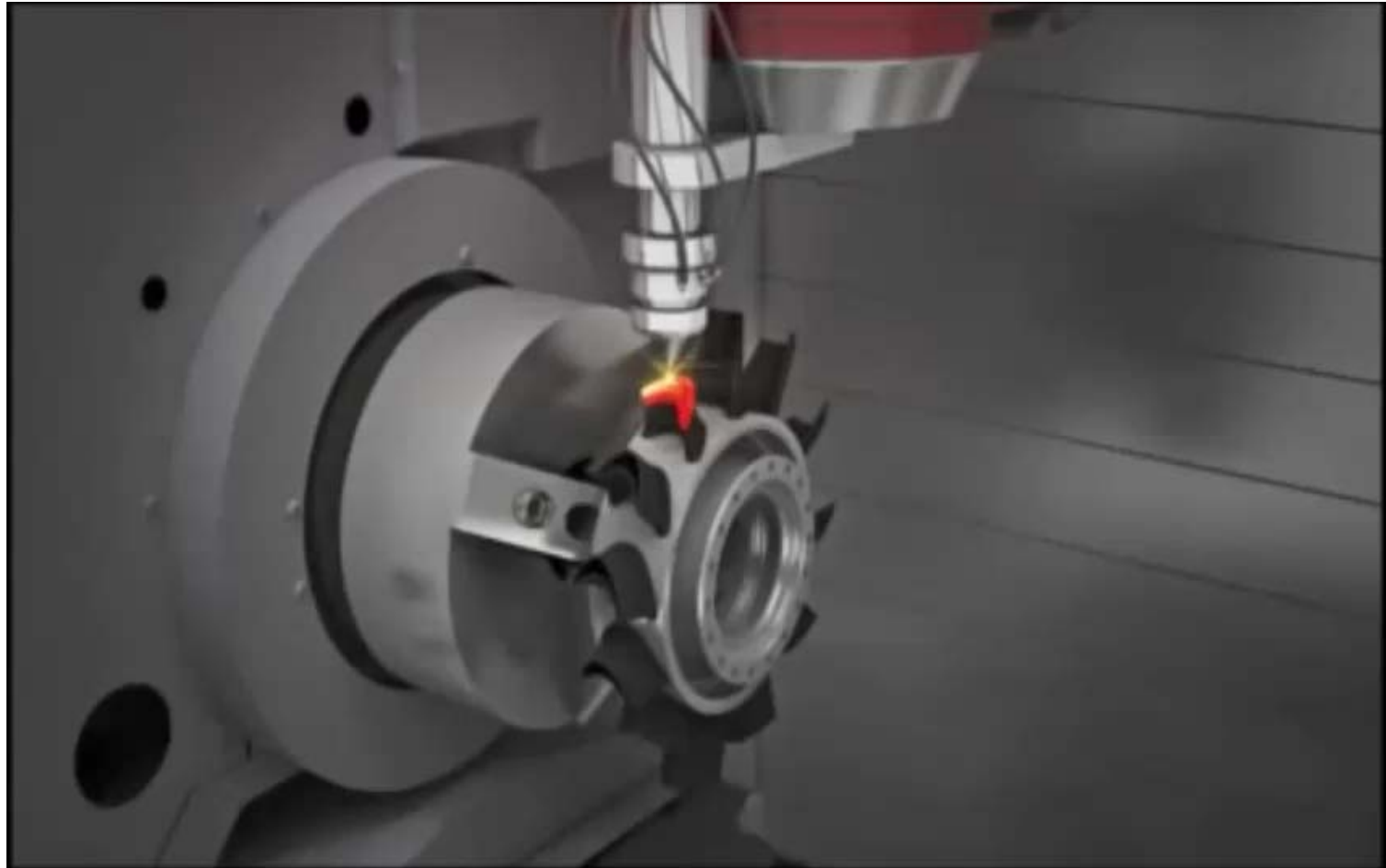
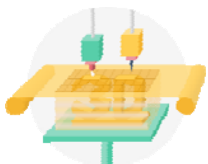
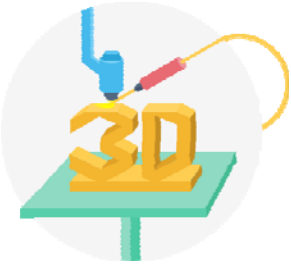
**Archetypes are the powders and chemistry**

**Genomes: metrology, properties and performance**





Walls, Sheraton. (2012, August 22). *Direct Metal Laser Sintering* [Video file]. Retrieved from <https://www.youtube.com/watch?v=cRE-PzI6uZA>



### Hybrid Additive and Subtractive Machining



Prototypes and small series production of complex lightweight and integral parts for:

- 1) **Die & Mold**
- 2) **Aerospace**
- 3) **Automotive**
- 4) **Medical**

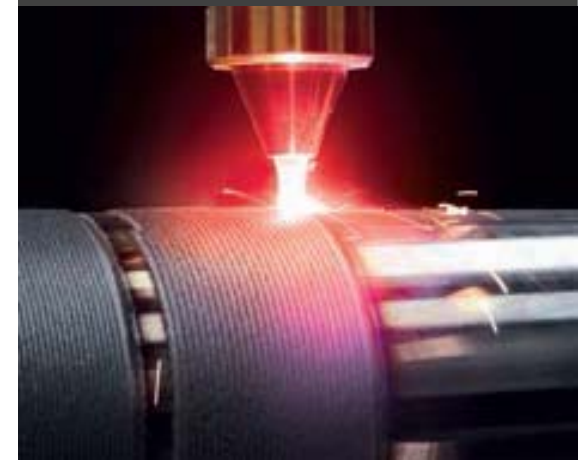
### Repair of Turbine and Die & Mold Components



Repair of damaged and worn components for:

- 1) **Medical**
- 2) **Die & Mold**
- 3) **Aerospace**  
(e.g. Blade Tip Repair)

### Corrosion and Wear Resistant Coatings



Partial coatings and complete part coatings (corrosion and wear resistant):

- 1) **Mould Making**
- 2) **Off Shore Drilling**
- 3) **Machine Tool**
- 4) **Medical**

## Under construction

### ARPI

Additive  
Rapid  
Prototyping  
Instrument at  
Northwestern  
University

- **Primary Additive Processing**

- Laser Engineered Net Shaping (LENS) Module
- Powder Bed Fusion (PBF) Module
- CW Laser 1 kW

- **Secondary Surface Operation**

- Electric Field Module
- Magnetic Field Module
- Pulsed Laser

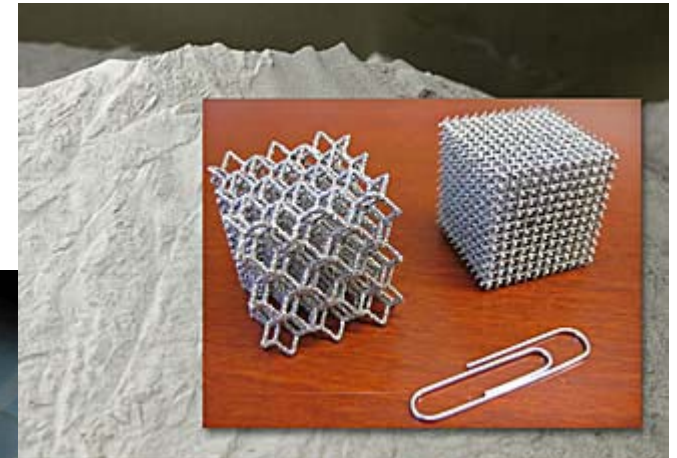
- **In-Situ Metrology**

- Pulsed laser
- Interferometer
- IR Camera

Typical engineering applications incorporate multiscale phenomena

**EXAMPLE:** Additive Manufacturing

**Final part**

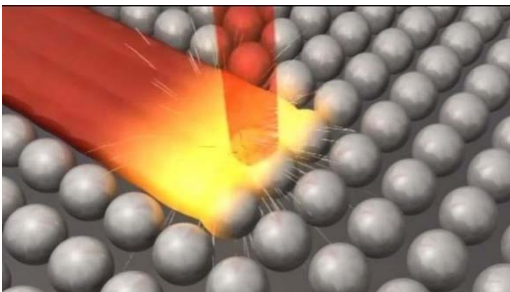


**Solidified layers**



**Structural property**

**Cyclic melting/re-melting on power scale**



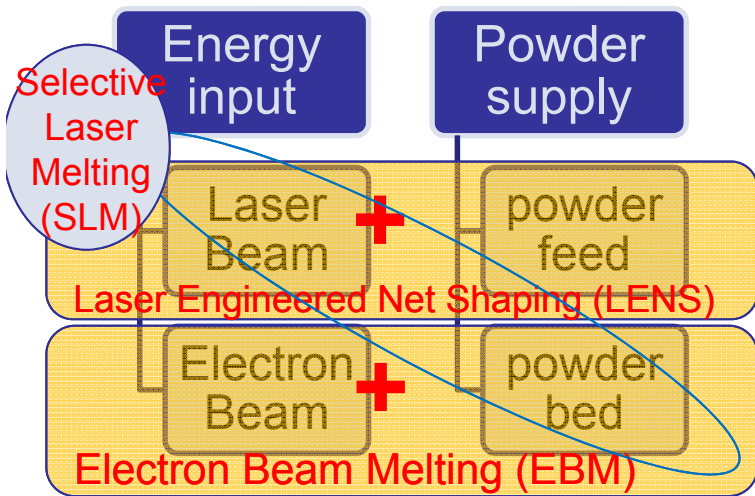
**Surface roughness**

**Microstructure evolution**

**Critical Problems (uncertainty source) for AM alloys**

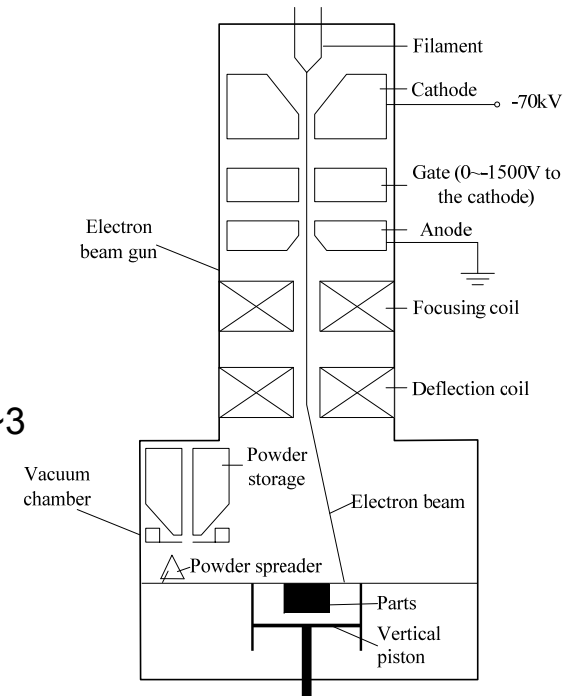
- ❖ Extremely fast heating and cooling rates
- ❖ Involving remelting and numerous low temperature reheating cycles
- ❖ Segregation & Phase distributions
- ❖ Long columnar grains along z-axis
- ❖ Impossible (at this time) to refine microstructure via deformation

### Additive manufacturing



### Electron Beam Melting

1. Spread powder bed
2. preheat: use defocused electron beam
3. melt: use focused electron beam
4. lower platform and repeat 1~3



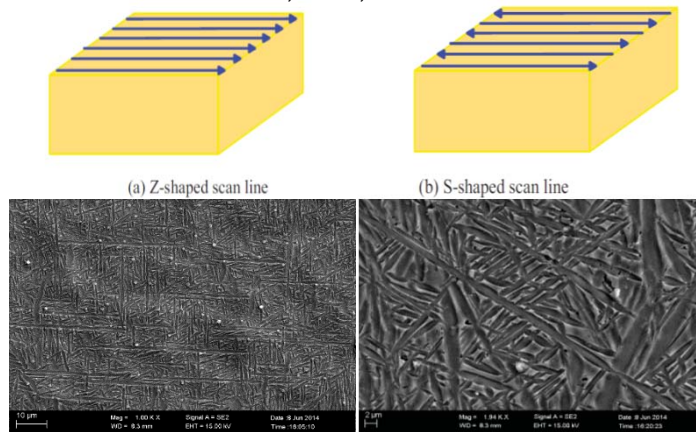
• The advantages

### 1. Complex geometry



### 2. control microstructure

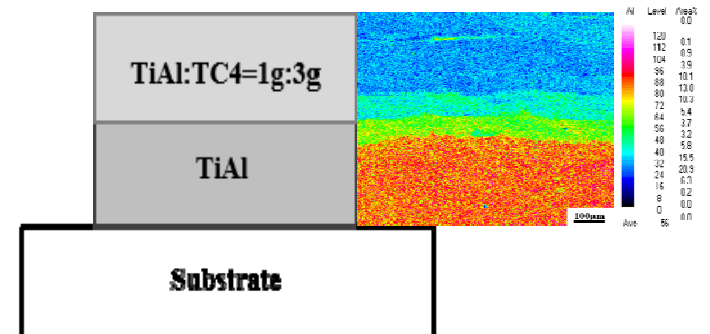
W Ge et al., SFF, 2014.



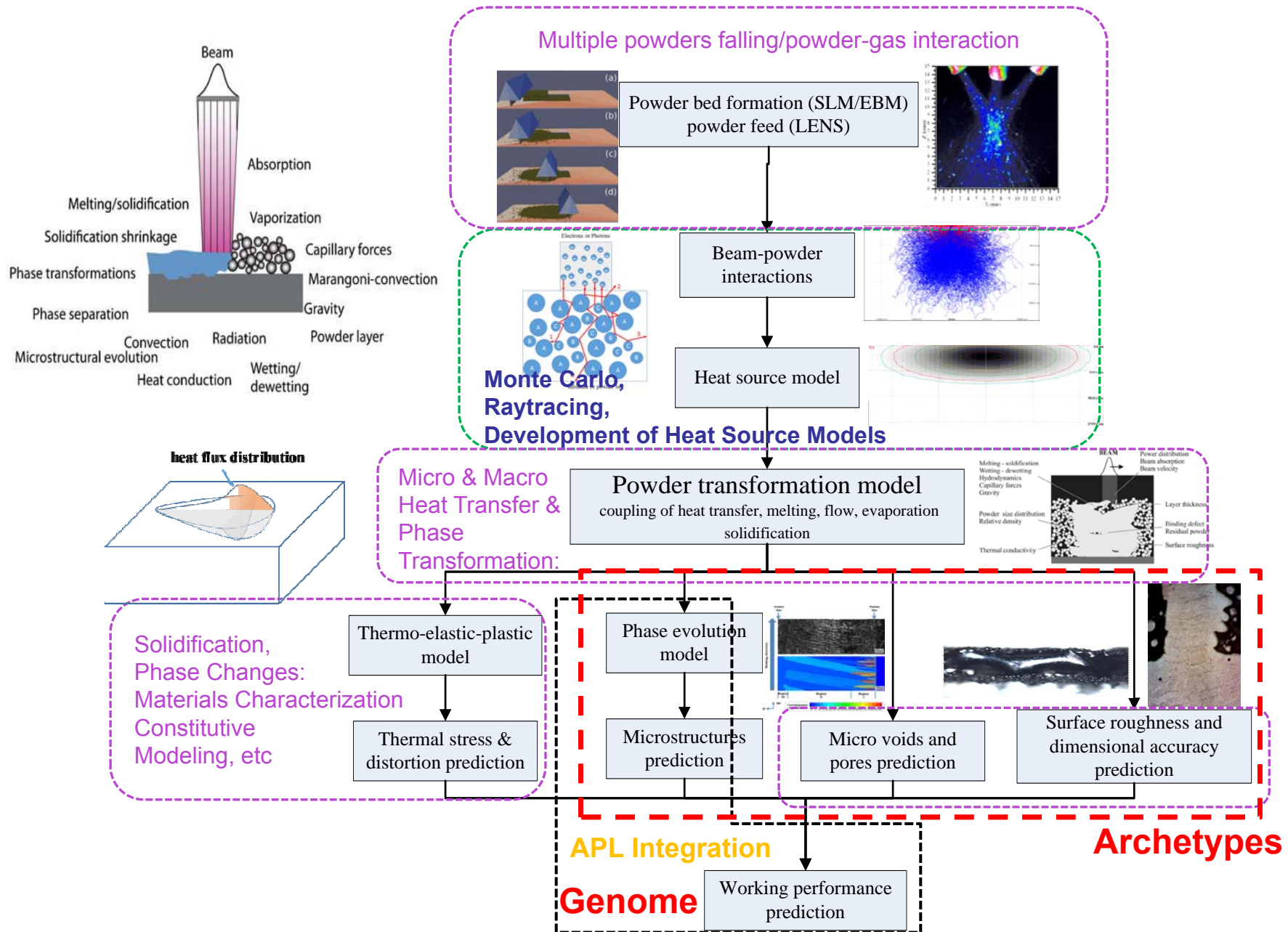
### 3. Design materials

#### Functional Gradient material

W Ge et al., SFF, 2015



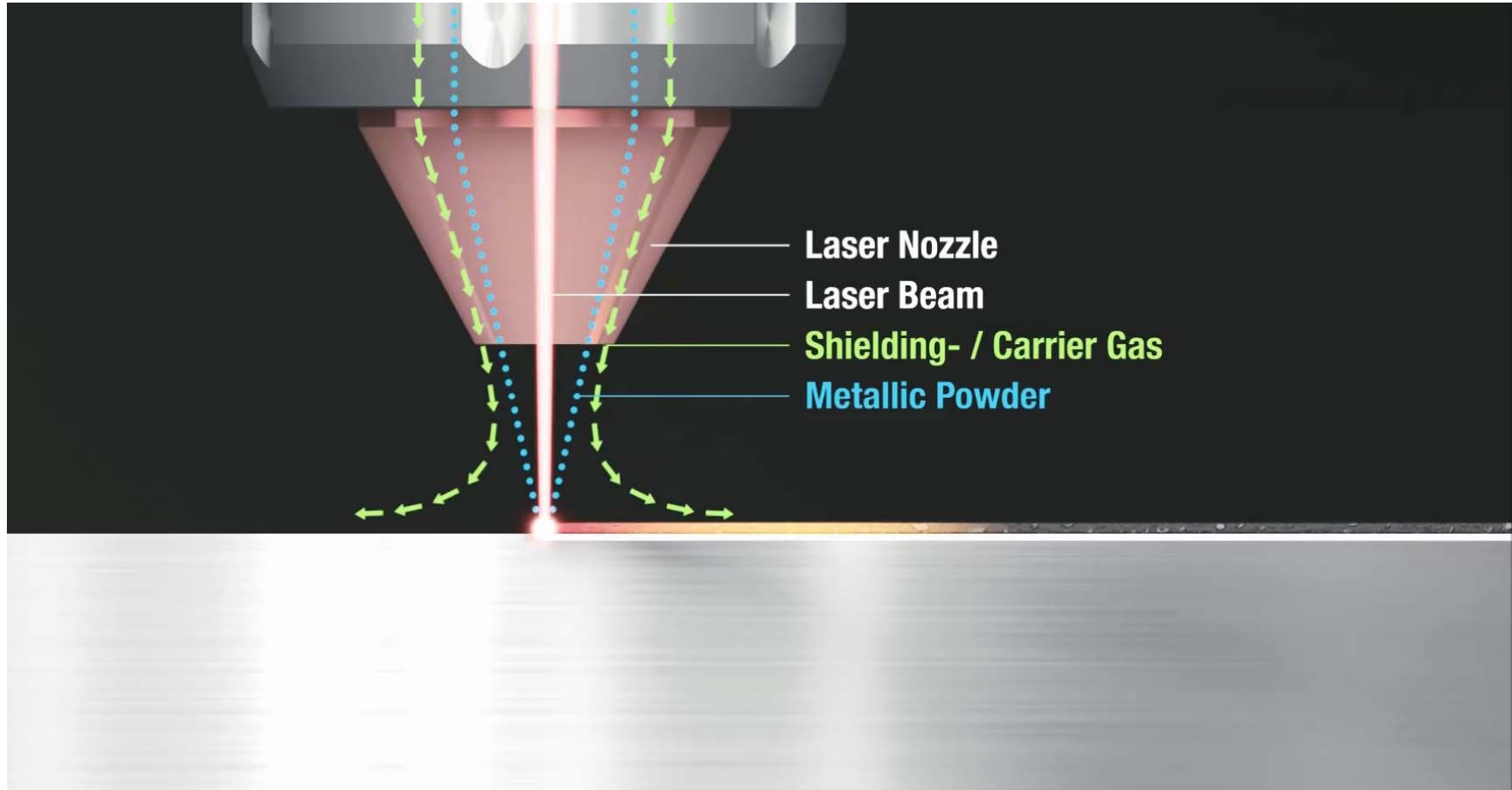
LENS: Laser Engineered Net Shaping



**McCormick**

Laser Engineered Net Shaping (LENS)

Northwestern Engineering

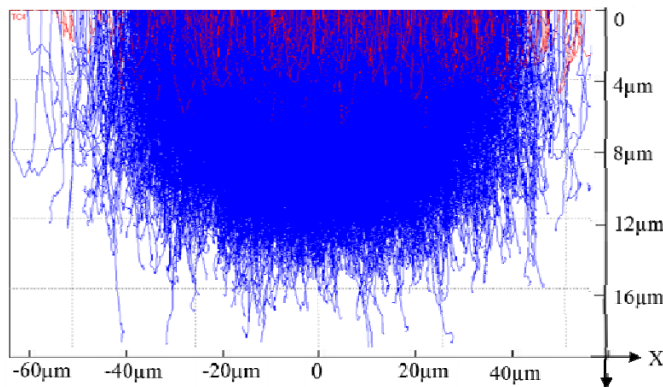


Movie; Used with permission from DMG Mori

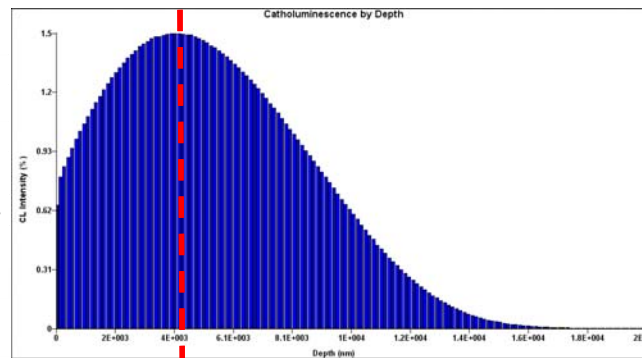


- **Metal-Based Processes**
  - Accumulation and Energy Input (**HEAT SOURCE**) Methods
  - Computational Process Modeling for **Microstructures Nucleation and Evolution (To make life easier or harder: Uncertainty Propagation)**
    - Micro heat source modeling
    - Macro heat source modeling and its microstructure evolutions
- **Experimental (**Statistical**) Materials Characterization**
  - The Role of Microstructure
- **Informatics-Driven (**with UQ**) Design Methodologies: Linking of Process-Structure-Property**
  - Image-Based Data Collection
  - Reduced Order Microstructural Modeling
  - Image-based Mechanistic Plasticity
  - Multiscale Fatigue Modeling
  - Image-Based materials behavior modeling (Constitutive Law Development)

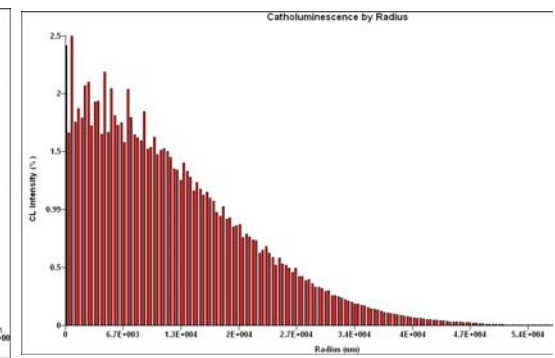
### New heat source model established



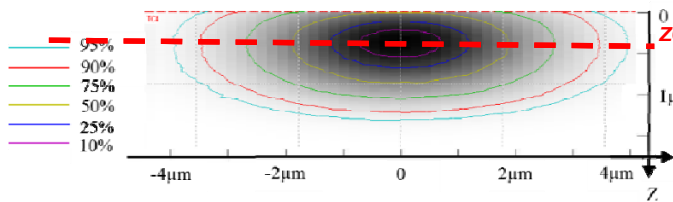
Trajectories



Energy Distribution in Z

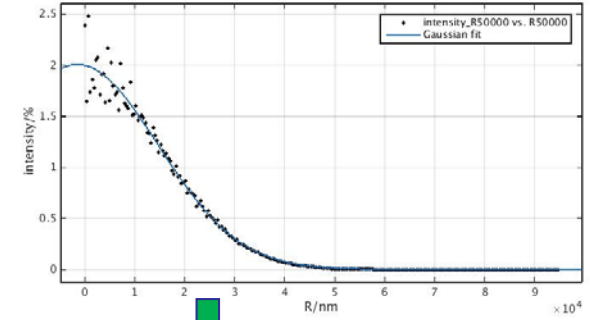
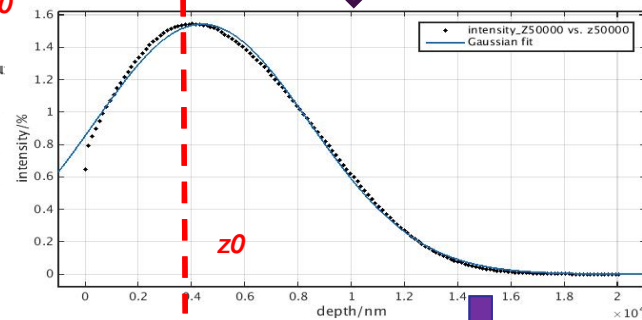


Energy Distribution in R



Absorbed energy distribution in XZ plane

Curve fitting



### New heat source model

$Z_0$ : depth with highest energy density

$\delta$ : characteristic depth

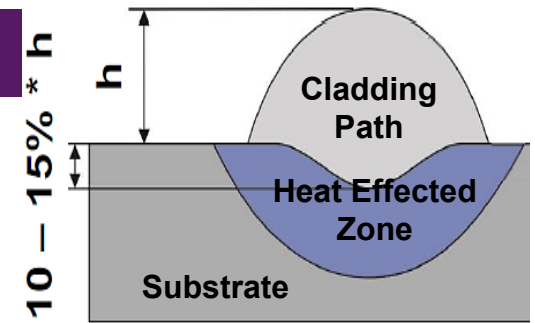
$$q(x, y, z) = Q * \left[ \frac{1}{\delta \cdot \int_{z_0}^{+\infty} \exp(-t^2) dt} \exp\left(-\frac{(z - z_0)^2}{\delta^2}\right) \right] * \left[ \frac{N}{\pi R_b^2} \exp\left(-N \cdot \frac{(x - x_s)^2 + (y - y_s)^2}{R_b^2}\right) \right]$$

Energy distributed through depth determined by the speed of the electron and the material

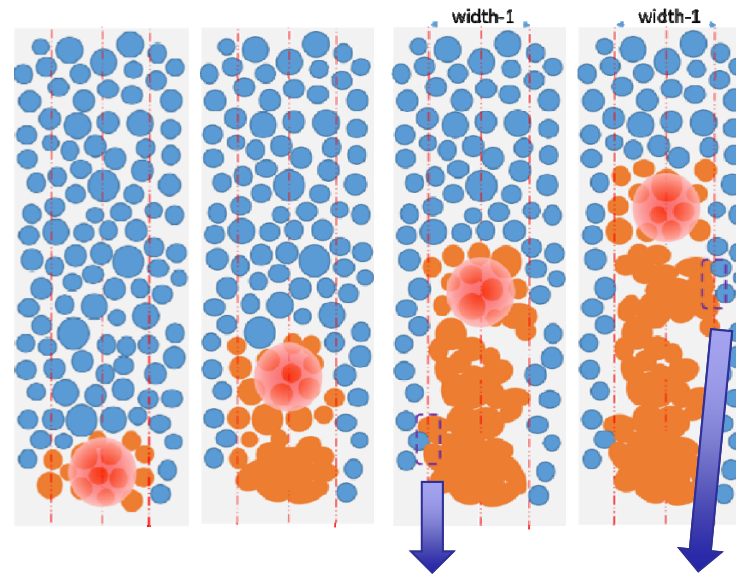
Energy distributed across cross section determined by the electron distribution

**Single track formation process**

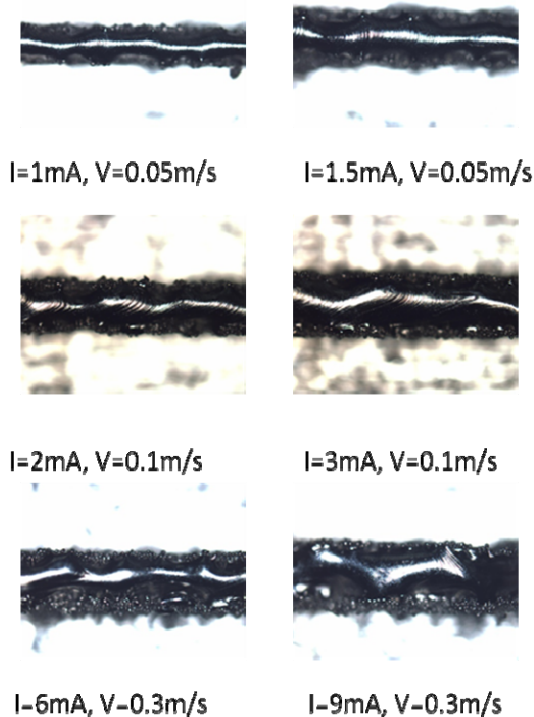
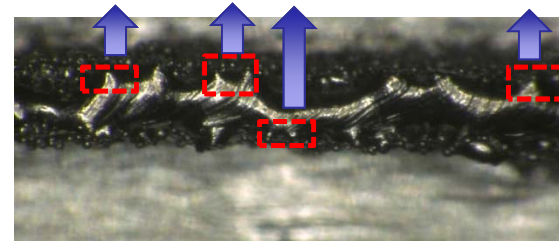
Experiments by Electron Beam Melting  
 Electron beam scans straightly, but the solidified tracks are not straight.



Mechanism view



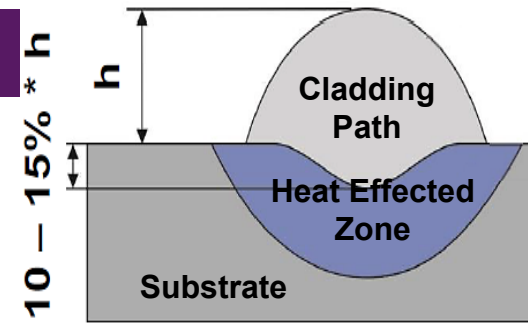
Random arrangement of powder bed



$v \uparrow$ , quality  $\downarrow$



How to predict?

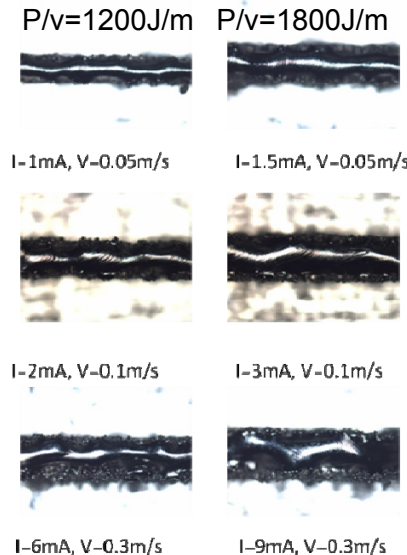


Comparison of experimental and simulated results

width-1 (μm) [experiments/**simulations**]

P/v	1200J/m	1800J/m
0.05m/s	420/450	506/490
0.1m/s	463/480	622/570
0.3m/s	550/540	660/600

Define line power input  
 $P/v=UI/v$   
 P: power  
 v: velocity



width-2 (μm) [experiments/**simulations**]

P/v	1200J/m	1800J/m
0.05m/s	287/310	421/420
0.1m/s	326/360	466/480
0.3m/s	383/420	502/490

- The differences are caused by the simplifications of the model, e.g. treating powder bed as continuum and neglecting the molten pool flow.
- However, the **simplified** model could act as a **useful** tool for the fabrication parameter selection.



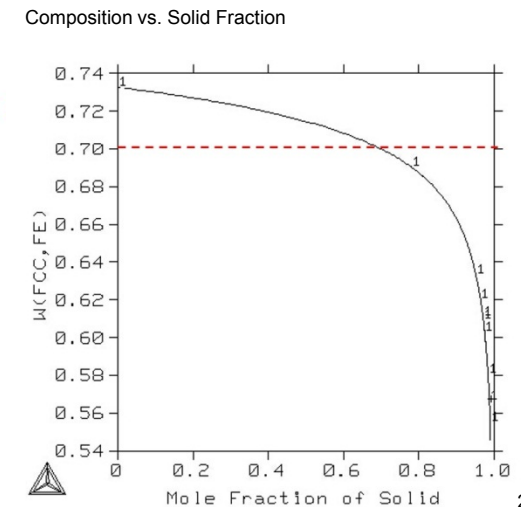
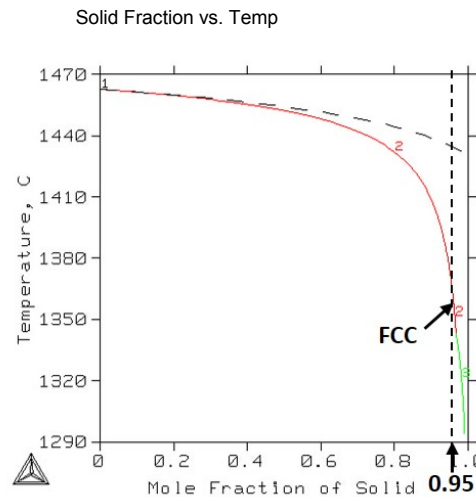
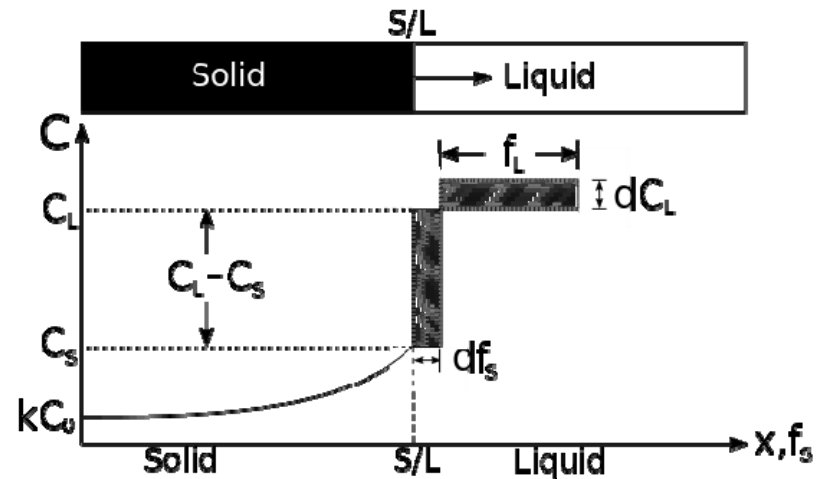
Thermo-Calc Software

❖ Powerful software package for a variety of thermodynamic calculations with composition and temperature as inputs including :

- ❑ Stable and meta-stable heterogeneous phase equilibria
- ❑ Amounts of phases and their compositions
- ❑ Thermochemical data such as enthalpies, heat capacity and activities
- ❑ Transformation temperatures, such as liquidus and solidus
- ❑ Driving force for phase transformations
- ❑ Phase diagrams (binary, ternary and multi-component)
- ❑ Solidification applying the Scheil-Gulliver model
- ❑ Thermodynamic properties of chemical reactions
- ❑ And much, much more...

### Solidification: Scheil Model

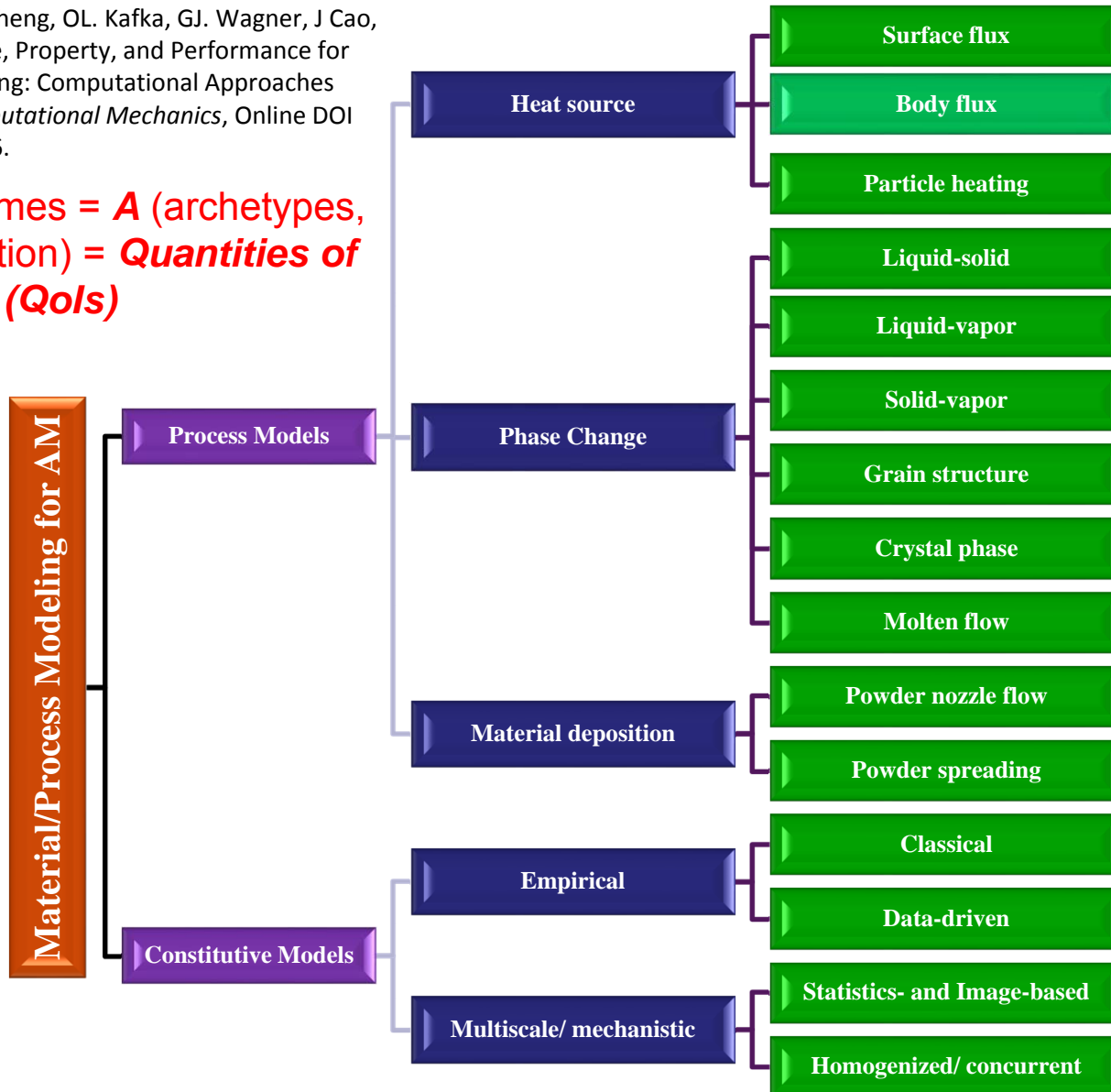
Solute redistribution by assuming local equilibrium at solid/liquid interface



J Smith, W Xiong, W Yan, S Lin, P Cheng, OL. Kafka, GJ. Wagner, J Cao, WK.Liu, "Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support," *Computational Mechanics*, Online DOI 10.1007/s00466-015-1240-4, 2016.

**Materials system genomes = A (archetypes, interactions, conformation) = Quantities of Interest (QoIs)**

- Various sources of uncertainties
- Quantification of uncertainties
- Uncertainties propagation
- Uncertainty quantification (UQ) is the quantifying of the uncertainty in predicted **QoIs**



**•Powder Deposition Parameters**

- Powder Flow Rate
- Shield Gas Flow Rate
- Powder Shape/Size/Type
- Nozzle Type

**•Laser Parameters**

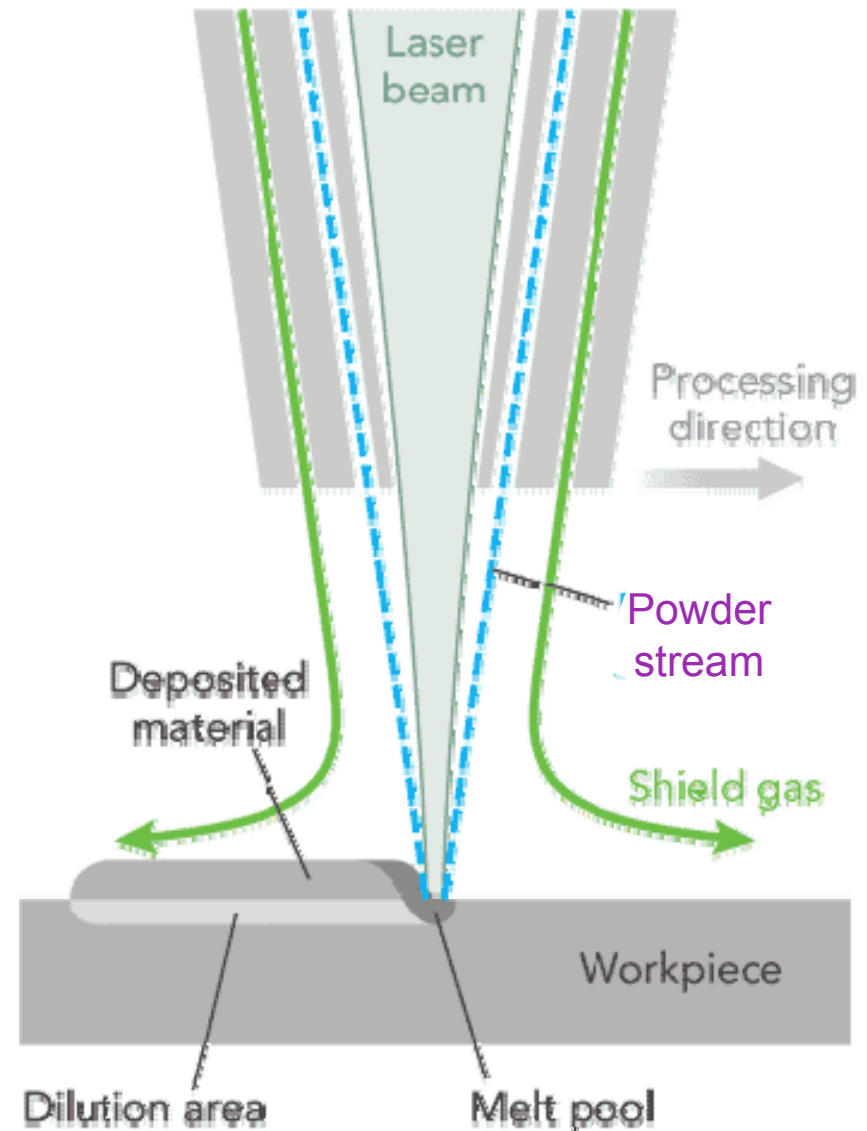
- Laser Spot Size
- Laser Scanning Speed
- Laser Power
- Laser Type

**•Geometric Parameters**

- Hatch Spacing
- Layer Height
- Build Geometry
- Build Strategy

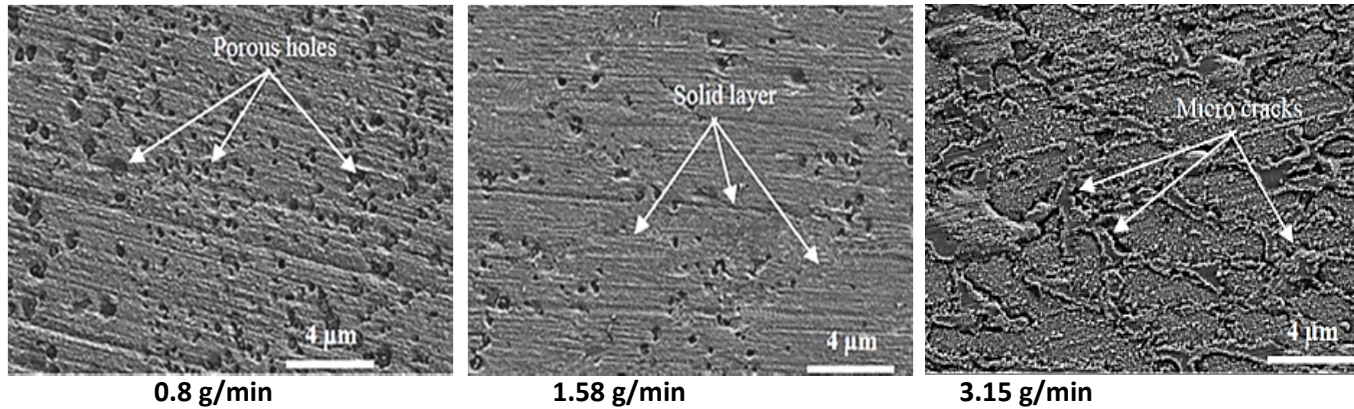
**•Substrate Parameters**

- Substrate Surface Condition
- Substrate Temperature
- Substrate Size



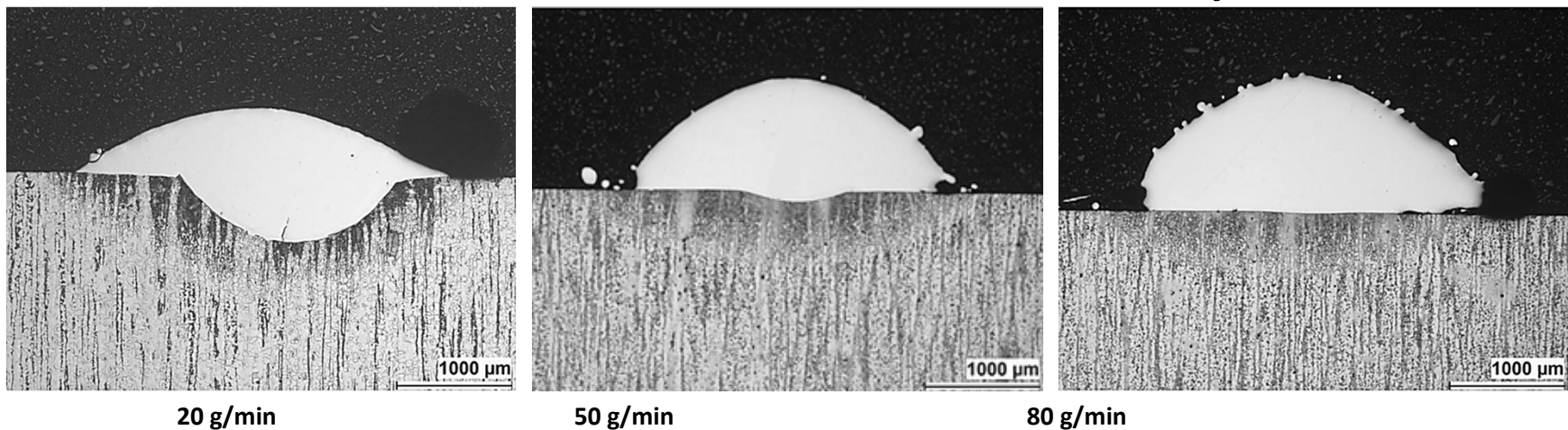
**Question: Materials system *genomes* = A(Archetypes, Interactions, Conformation)**

**Effect of Powder Mass Flow Rate on Microstructure<sup>[1]</sup>**



[2]

**Effect of Powder Mass Flow Rate on Clad Quality**



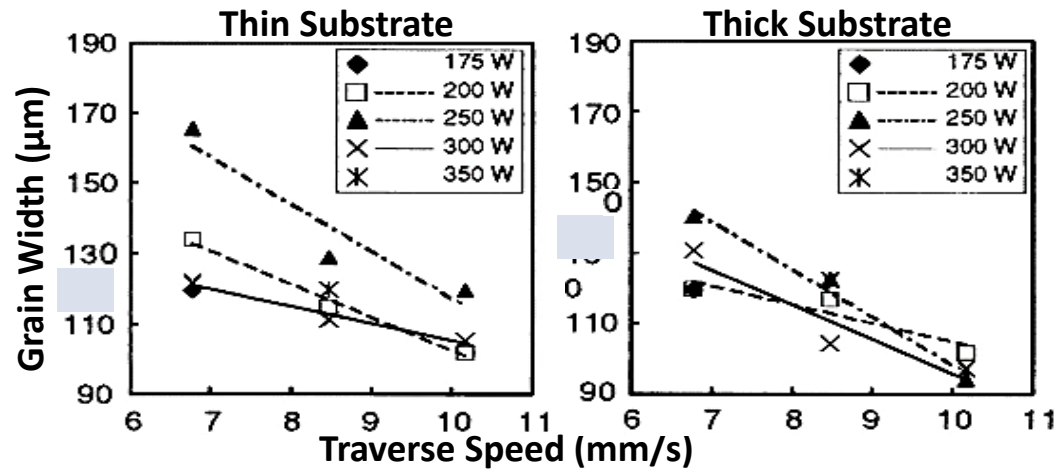
[1] Influence of Process Parameters in the DMD of H13 Tool Steel on Cu Alloy Substrate, Imran et al., Proceedings of the World Congress on Engineering Vol III, 2010

[2] Used with permission from DMG Mori

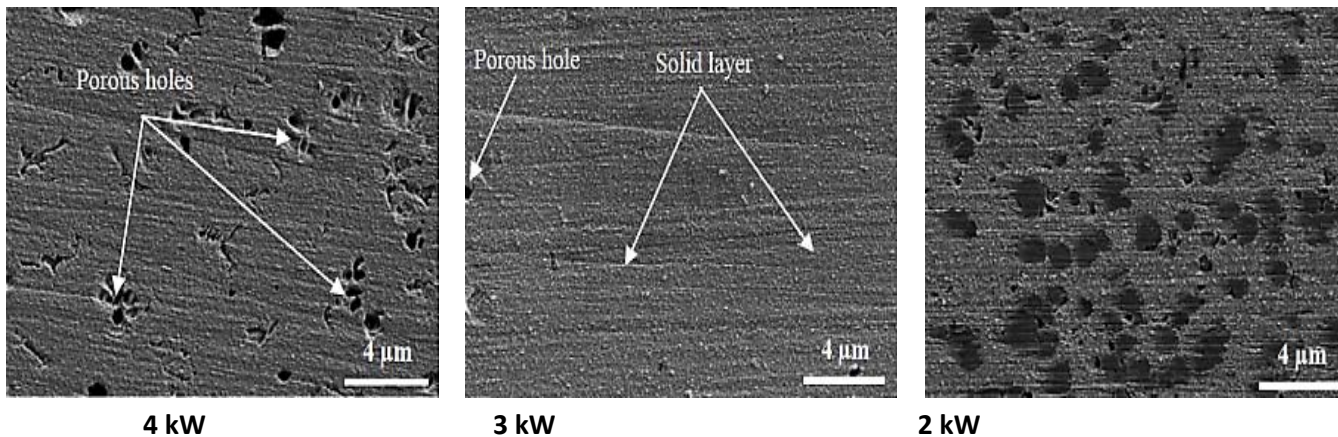


**Question: Materials system genomes = A(Archetypes, Interactions, Conformation)**

**Effect of Scan Speed and Laser Power on Ti-6Al-4V Build Microstructure**



**Effect of Laser Power on Microstructure** <sup>[2]</sup>

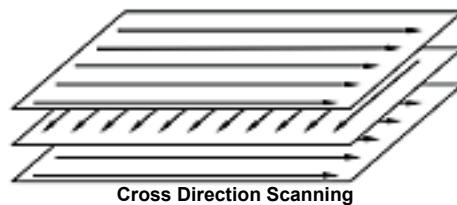
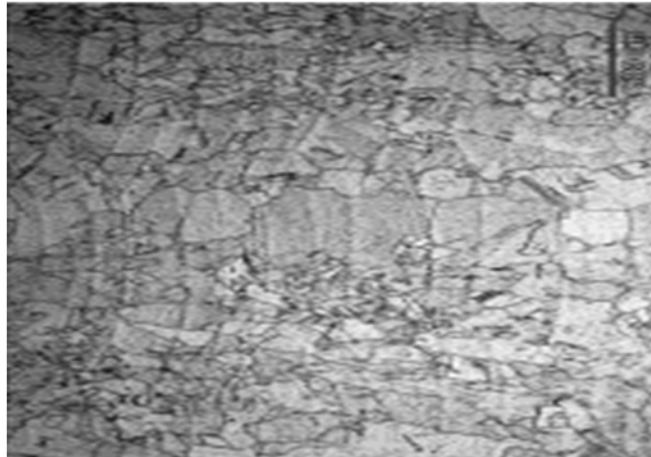
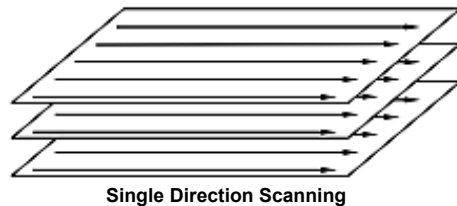


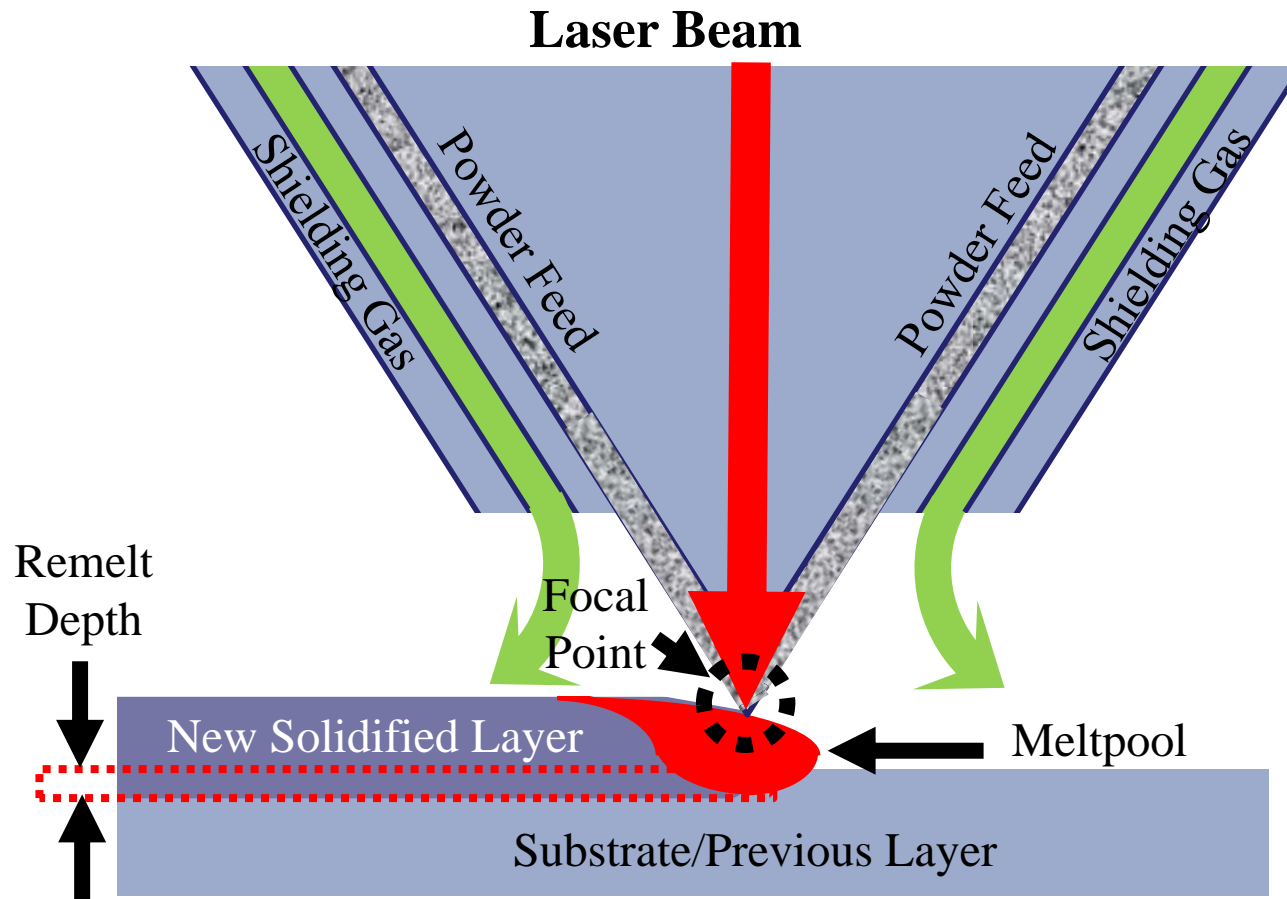
[1] The effect of laser power and traverse speed on microstructure, porosity and build height in laser-deposited Ti-6Al-4V, Kobryn, Scripta Materialia, 2000

[2] Influence of Process Parameters in the Direct Metal Deposition of H13 Tool Steel on Copper Alloy Substrate, Imran, Proceedings of the World Congress on Engineering, 2010

**Question: Materials system genomes = A(Archetypes, Interactions, Conformation)**

## Effect of Deposition Direction on Microstructure



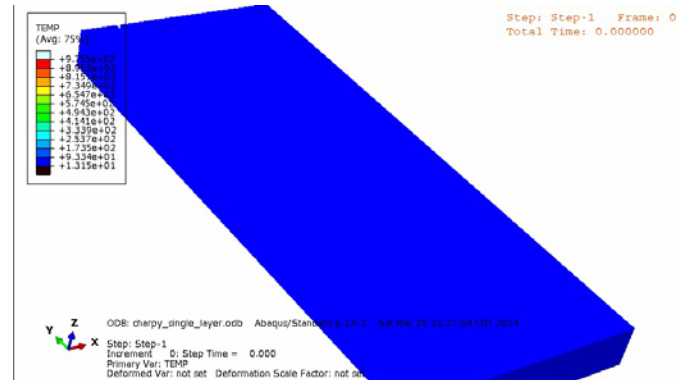


J Smith, W Xiong, W Yan, S Lin, P Cheng, OL. Kafka, GJ. Wagner, J Cao, WK.Liu, "Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support," *Computational Mechanics*, Online DOI 10.1007/s00466-015-1240-4, 2016.

Combining experimental toolpath with thermal analysis

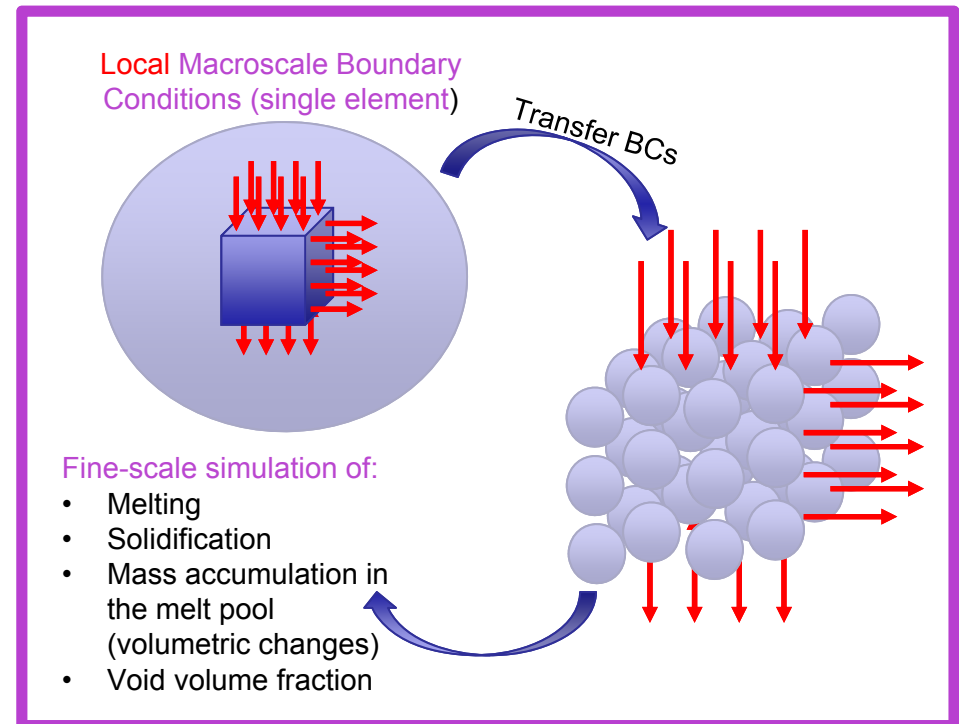
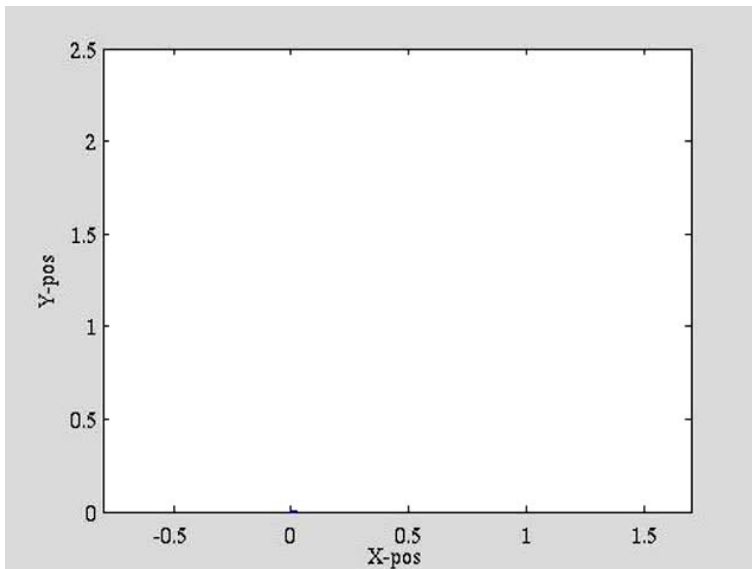
- Arbitrary toolpaths
- Better cooling rate prediction
- **Reduction of preprocessing time for simulations**

### Thermal Model w/ Experimental Toolpath

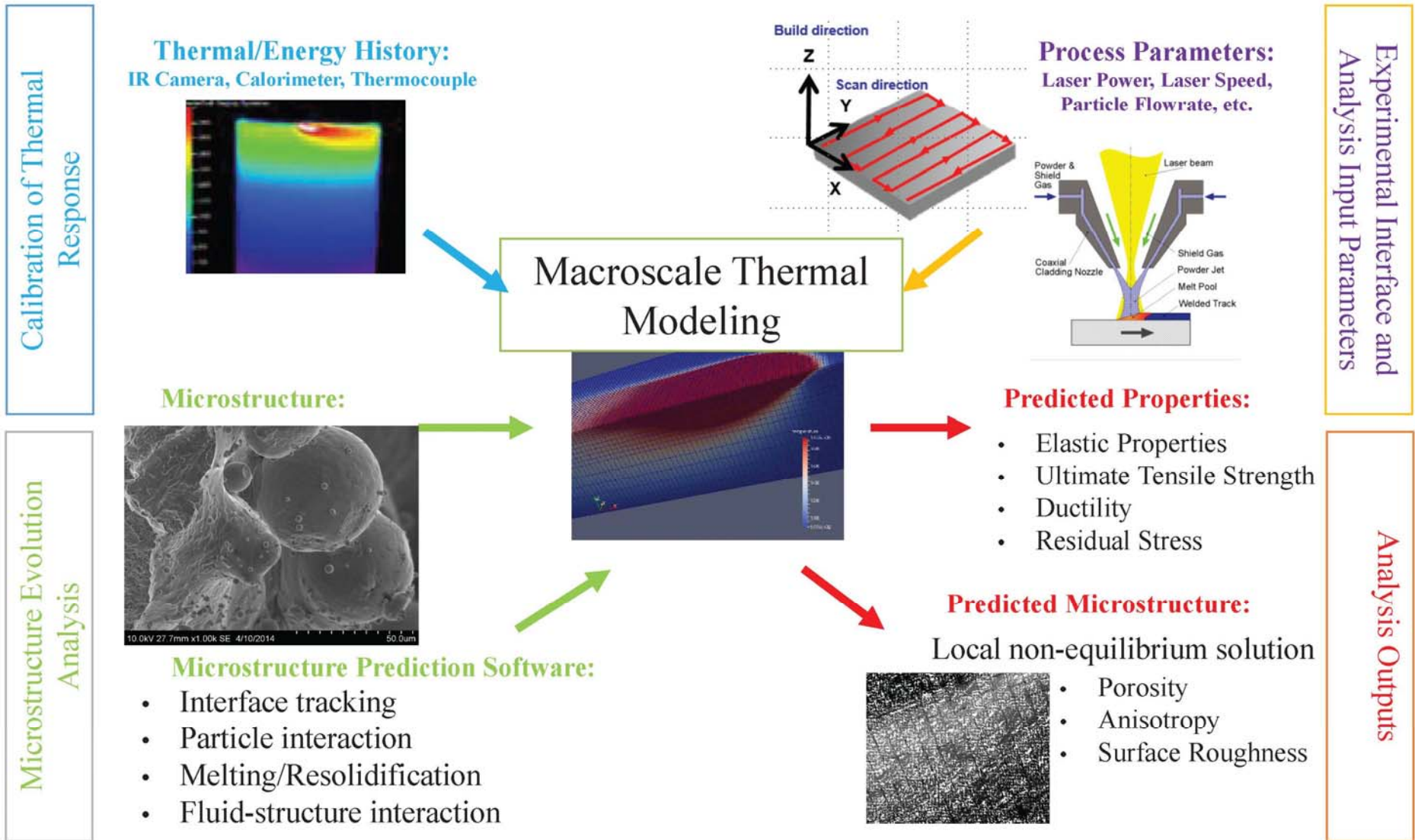


### Extracted Toolpath from LENS Machine Syntax

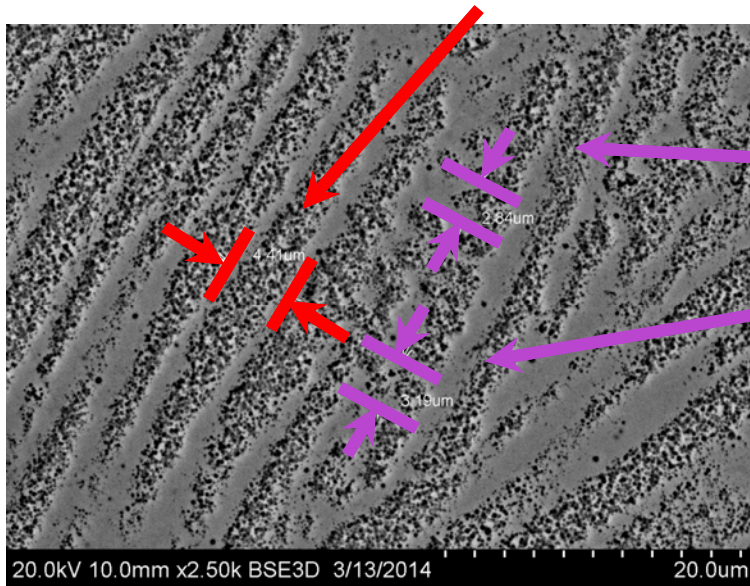
**Laser On**  
**Laser Off**



**Integrated computational toolset approach for understanding process-structure-property relations for AM processes.**



**Primary Dendrite Spacing (4.41um)**



**Secondary Dendrite Arm Spacing**

$$\lambda = 80 \dot{T}^{-0.33}$$

From thermal model

$$\lambda_1 = 2.84 \mu\text{m}$$

Cooling rate  $\sim 2.47 \times 10^4 \text{ K/s}$

$$\lambda_2 = 3.19 \mu\text{m}$$

Cooling rate  $\sim 1.74 \times 10^4 \text{ K/s}$

**Why 2nd Arm Dendrite Spacing?**

- Calculate cooling rate
- Gives sense of mechanical properties

**Now, Process Parameters Drive Microstructure and Material Behavior**

**Cooling Rate Calculation**

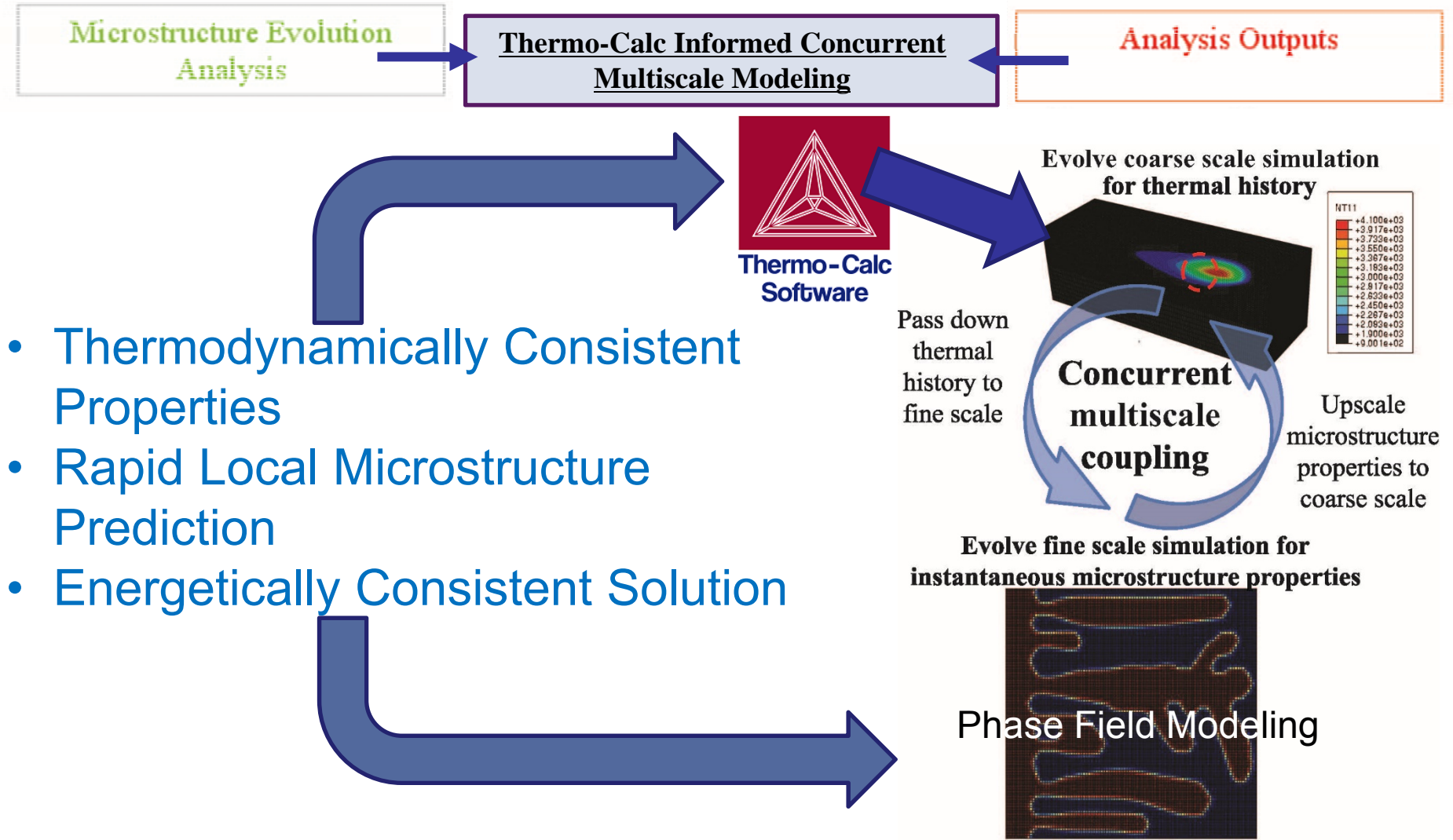
- Latent heat during solidification
- Input for solidification modeling

**Microstructure Control**

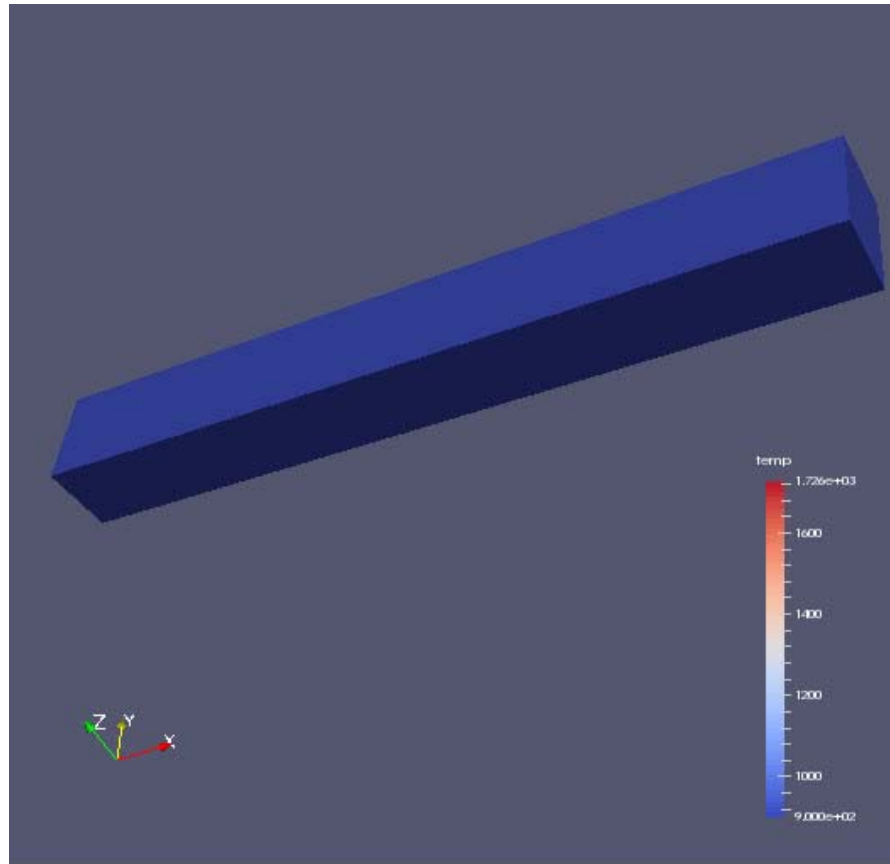
- Grain size
- Transfer columnar dendrites to equiaxed dendrites



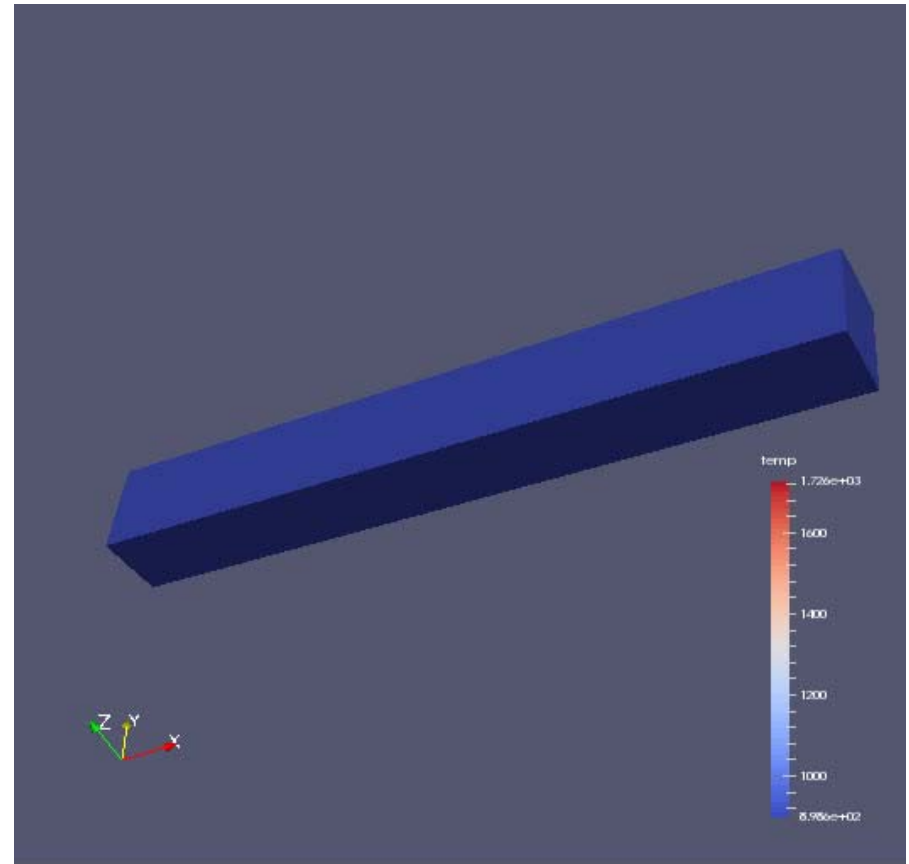
Smith, Xiong, Cao, and Liu, *“Thermodynamically Consistent Microstructure Prediction of Additively Manufactured Materials,” Computational Mechanics*, Online DOI 10.1007/s00466-015-1243-1, 2016.



### Traditional Experimentally Derived Properties



### ThermoCalc derived properties



Red = Melting Region  
Blue = Solid Region

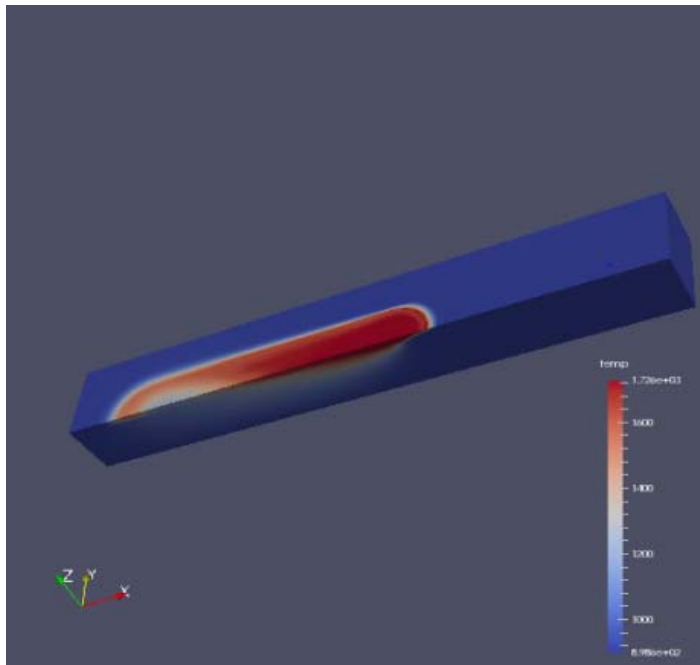


## Northwestern Engineering

Thermo-Calc provides thermodynamic property and phase fraction evolution laws

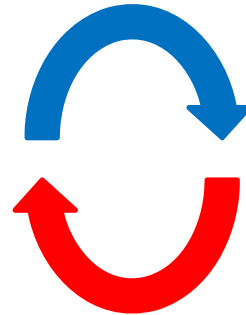
**Does NOT provide a image or “snapshot” of evolved microstructure**

**Goal:** Develop a concurrent multiscale model to capture high resolution microstructure evolution throughout AM build process

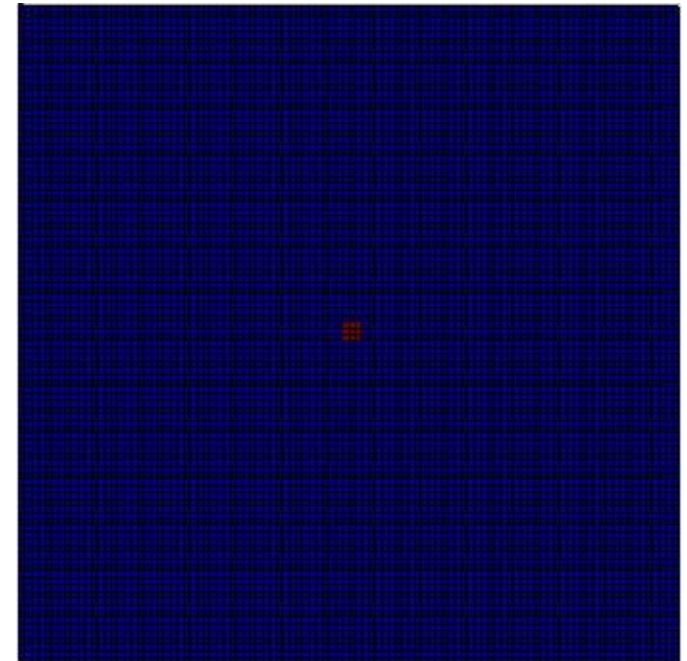


**Large Scale Thermal Modeling**

**Thermal Information:**  
Cooling rate,  
temperature gradient etc.

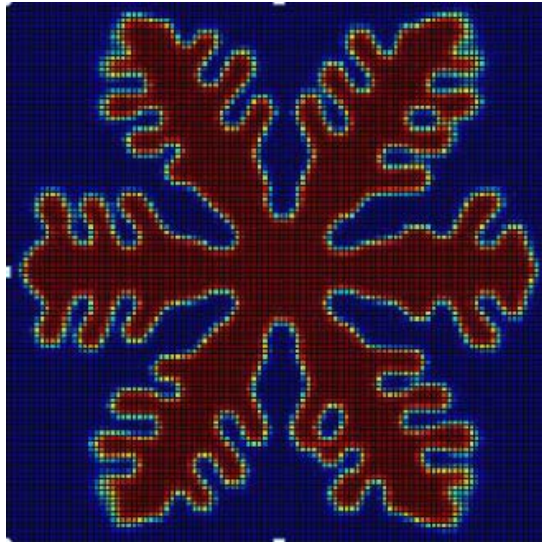


**Microstructure Properties**  
Conductivity, latent heat  
etc.



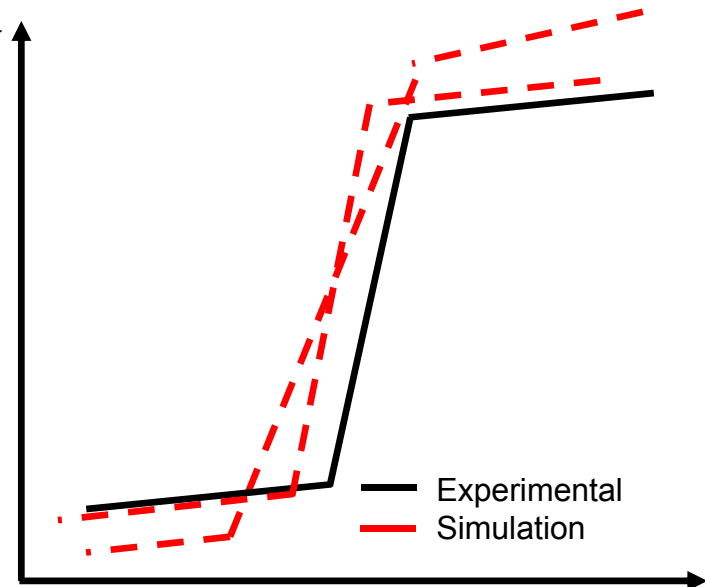
**Fine Scale Phase Field Computation**

Fine Scale Phase Field

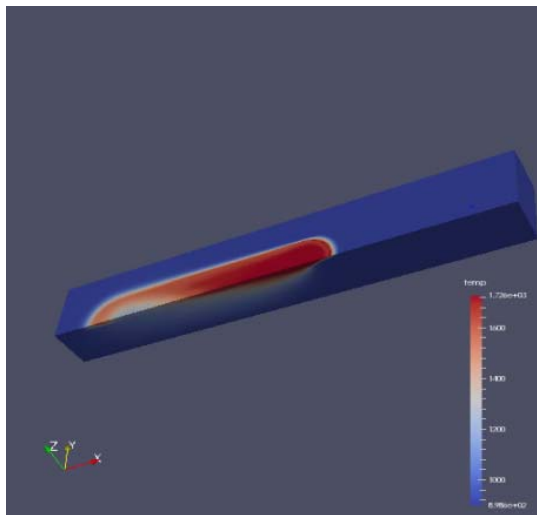


Calibrate with Thermo-Calc analysis

Enthalpy  $\Delta H$

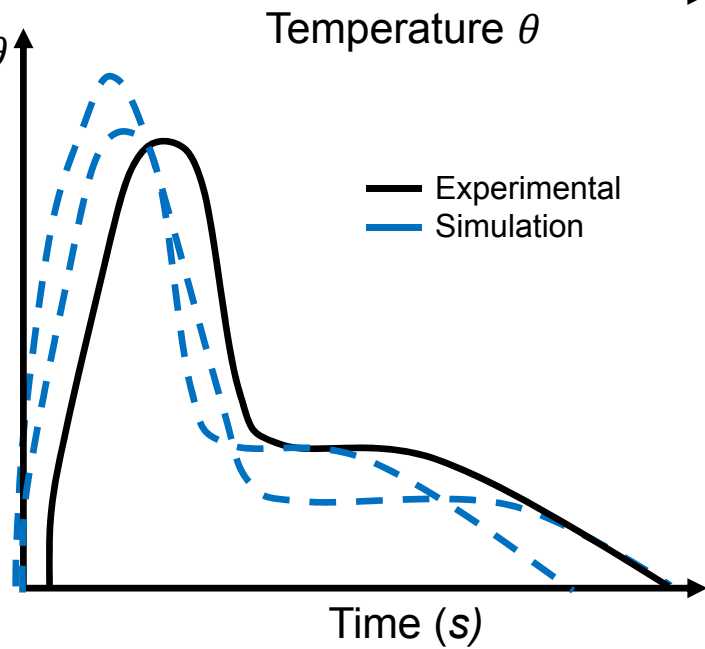


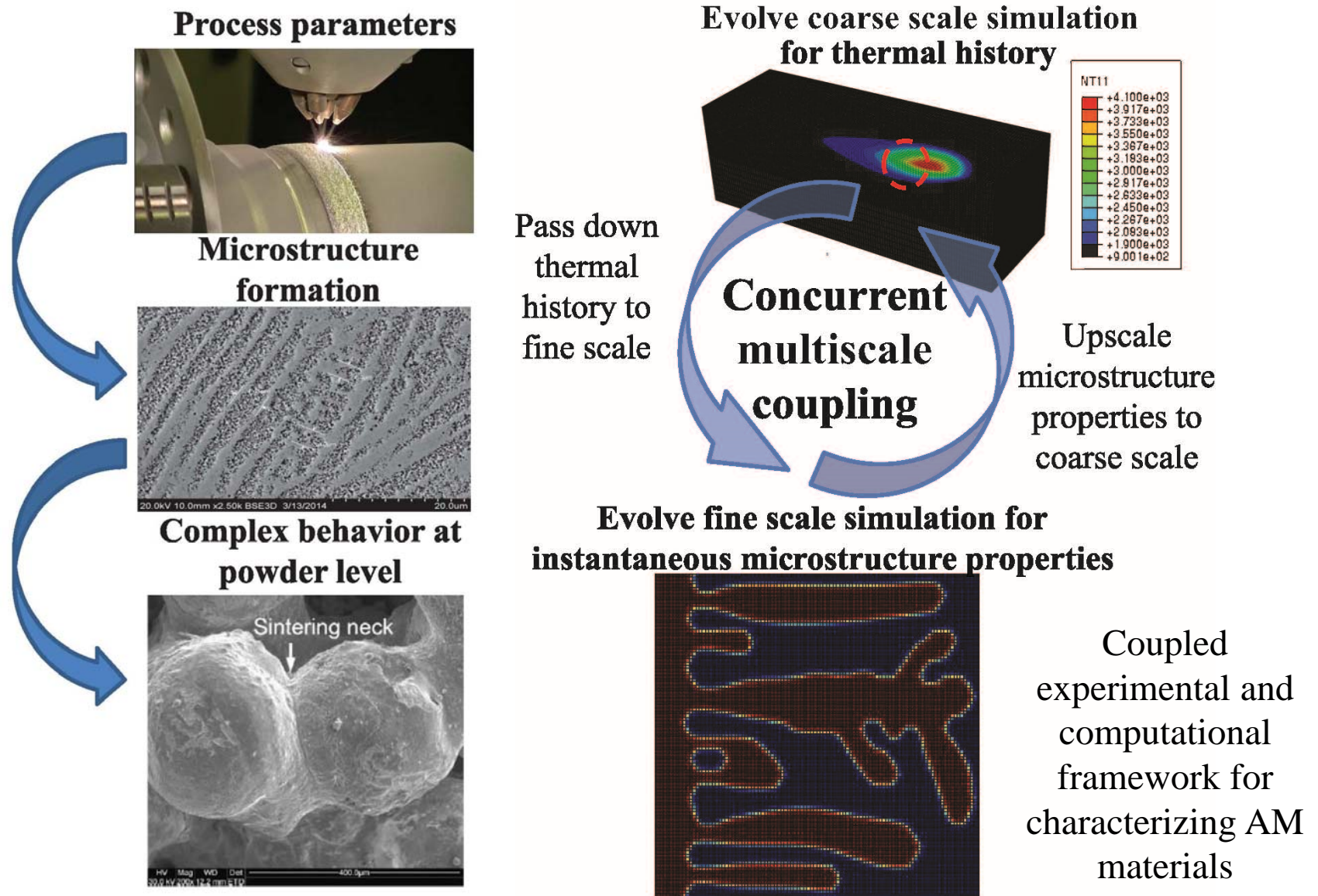
Large Scale Thermal Model

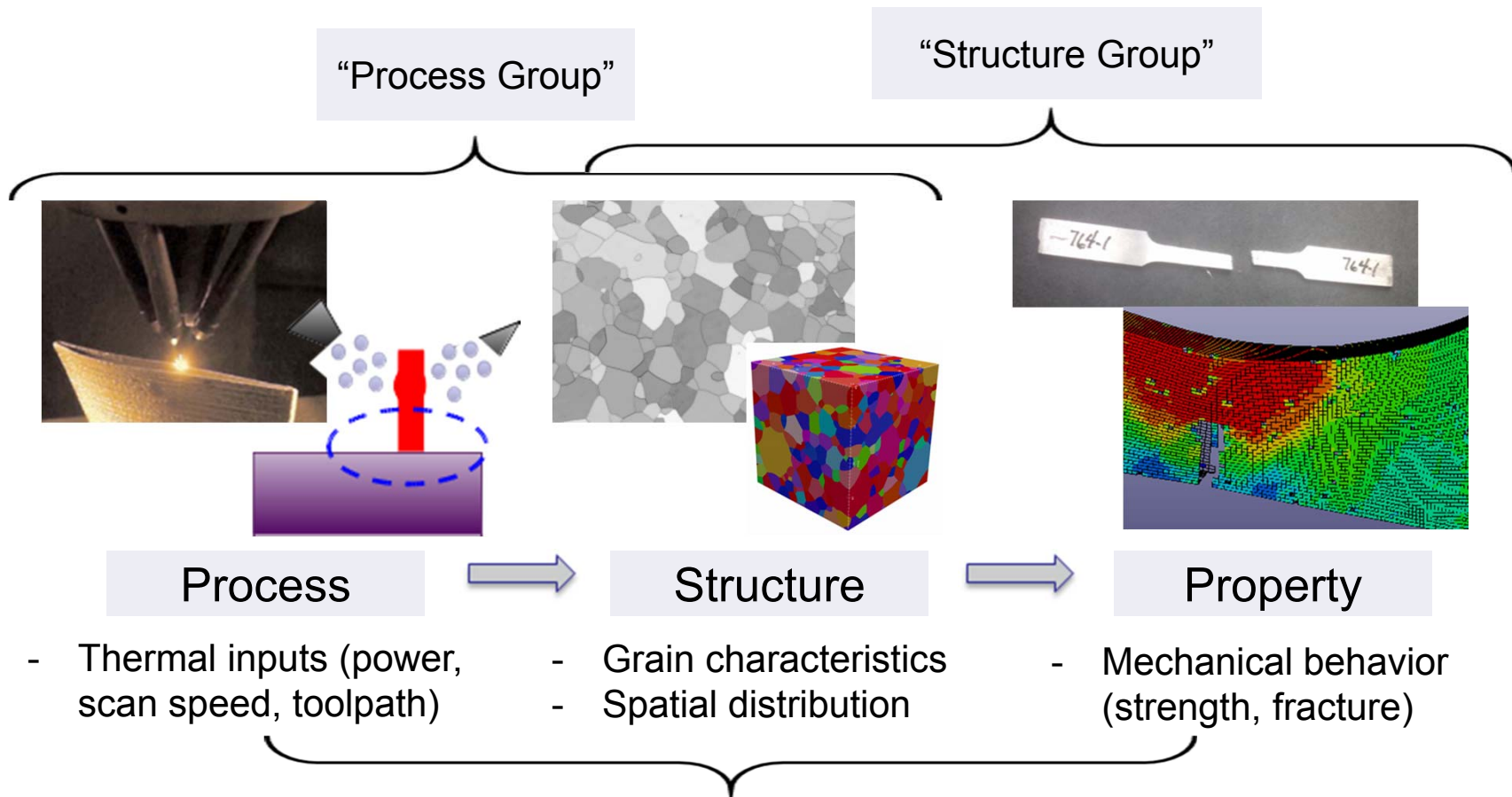


Calibrate with experimental cooling rate & thermal gradients

Temperature  $\theta$





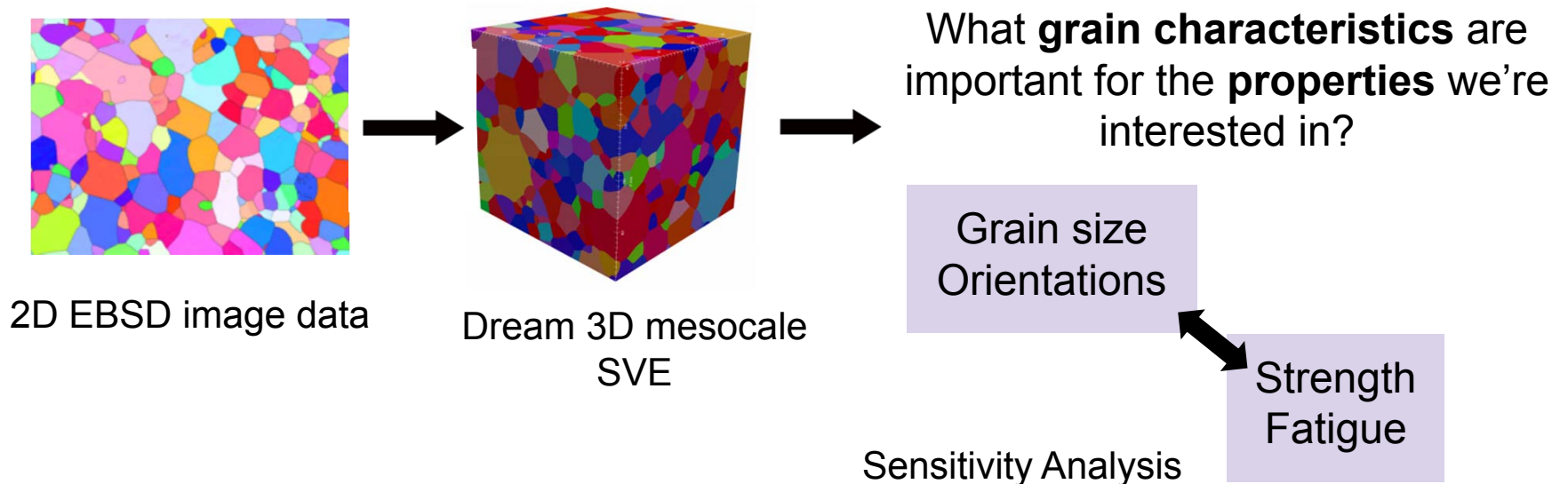


- |  |          |   |          |   |
|--|----------|---|----------|---|
| <p><b>Process</b></p> <ul style="list-style-type: none"> <li>- Thermal inputs (power, scan speed, toolpath)</li> </ul> | <p>→</p> | <p><b>Structure</b></p> <ul style="list-style-type: none"> <li>- Grain characteristics</li> <li>- Spatial distribution</li> </ul> | <p>→</p> | <p><b>Property</b></p> <ul style="list-style-type: none"> <li>- Mechanical behavior (strength, fracture)</li> </ul> |
|--|----------|---|----------|---|

**Design loop:** Determine optimal processing parameters for performance

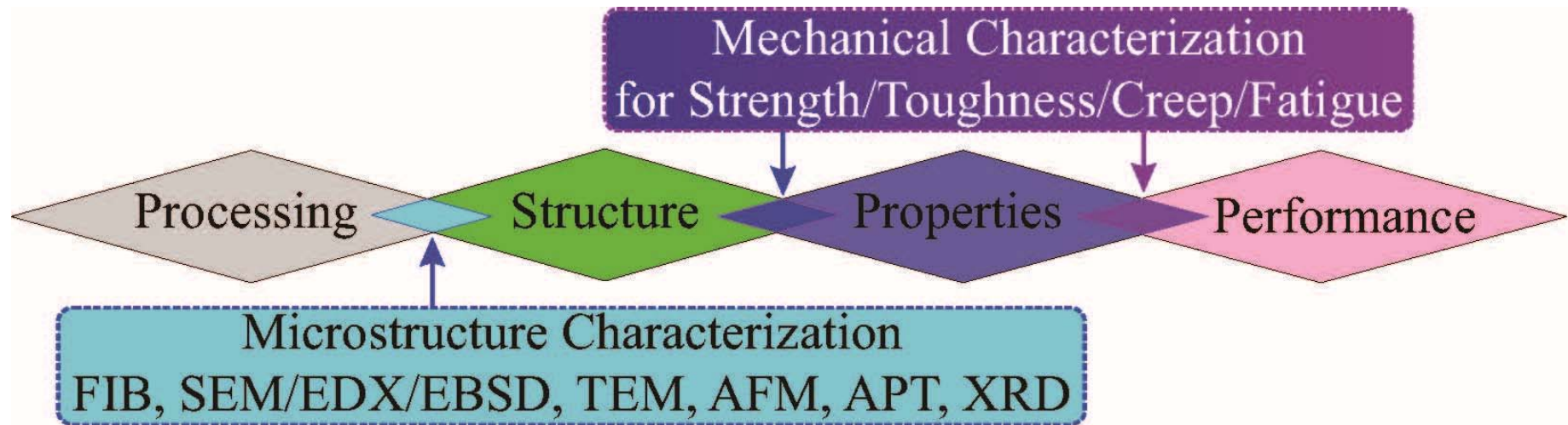
**Mesoscale SVE:** generate grains from images

- Construct ray of 3D SVEs from 2D images of grains
- Determine statistical relationships between **grain structure** and **mechanical properties** in SVEs through crystal plasticity



J Smith, W Xiong, W Yan, S Lin, P Cheng, OL. Kafka, GJ. Wagner, J Cao, WK.Liu, "Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support," *Computational Mechanics*, Online DOI 10.1007/s00466-015-1240-4, 2016.

Zeliang Liu, M.A. Bessa, Wing Kam Liu, "Self-consistent clustering analysis: an efficient multi-scale scheme for inelastic heterogeneous materials," Submitted



**FIB:** Focused Ion Beam,  
**SEM:** Scanning Electron Microscopy,  
**EDX:** Energy-Dispersive Xray spectroscopy,  
**EBSD:** Electron Backscatter Diffraction,  
**TEM:** Transmission Electron Microscopy,  
**AFM:** Atomic Force Microscopy,  
**APT:** Atom Probe Tomography,  
**XRD:** Xray Diffraction.

J Smith, W Xiong, W Yan, S Lin, P Cheng, OL Kafka, GJ. Wagner, J Cao, WK.Liu, "Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support," *Computational Mechanics*, Online DOI 10.1007/s00466-015-1240-4, 2016.

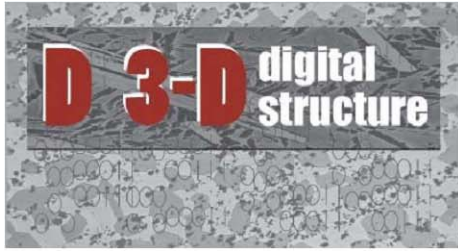
# Integration of Materials Design for Digital 3D Structures

**Wing Kam Liu, et al.**, “Complexity science of multiscale materials via stochastic computations,” *International Journal for Numerical Methods in Engineering*, Volume 80, Issue 6, 5 - 12 November 2009, Pages: 932-978, 2009.

**Shan Tang, Adrian M. Kopacz, Stephanie Chan, Gregory B. Olson, Wing Kam Liu**, “Concurrent Multiresolution Finite Element: Formulation and Algorithmic Aspects,” *Computational Mechanics*, 2013, 52:1265–1279.

**Shan Tang, Adrian M Kopacz, Stephanie Chan, Greg Olson, Wing Kam Liu**, “Three-dimensional Ductile Fracture Analysis with a Hybrid Multiresolution Approach and Microtomography,” *Journal of the Mechanics and Physics of Solids*, 2013, 2108–2124.

**S. O’Keeffe, S. Tang, AM Kopacz, J. Smith, DJ Rowenhorst, G. Spanos, WK Liu, GB Olson**, Multiscale Ductile Fracture Integrating Tomographic Characterization and 3D Simulation, *Acta Materialia*, 82, (2015), 503-510.



# Design Research Tools



# Design Research Tools Consortium

PI: G.B. Olson

Northwestern University & QuesTek

Co-PI: Wing Kam Liu

**Fracture Toughness Simulator**



**Georgia Tech**





**D 3-D** digital structure

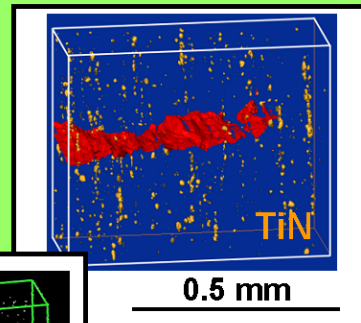


Design Research Tools



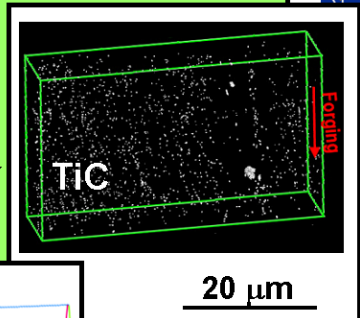
**matCAT** Characterization & Visualization Toolset

FSL/LOM Tomography  
[Pollock, Olson]  
Toughness, Fatigue Strength  
[Olson, Kern]



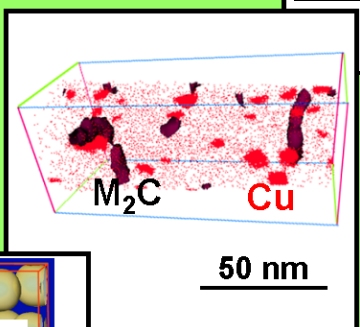
Ductile Fracture  
[Moran, Liu, Parks]  
Fatigue Nucleation  
[McDowell, Olson]

FSL/FIB Tomography  
[Pollock]  
Shear Instability  
[Olson, Kern]

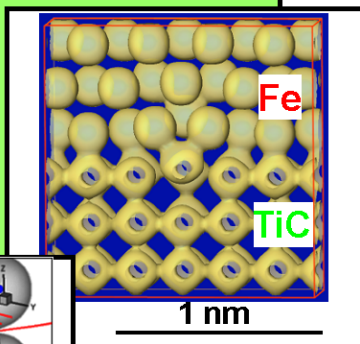


Microvoid Shear  
[Moran, Liu, Parks]  
Fatigue Propagation  
[McDowell]

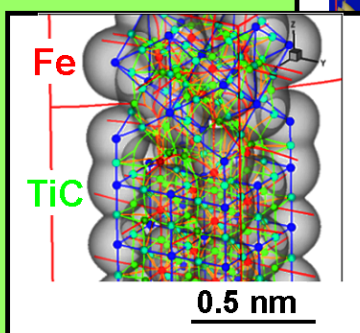
LEAP Tomography  
[Seidman]  
Yield Strength  
[Olson, Kern]



Transformation Toughening  
[Parks, Olson]  
Precipitation Strengthening  
[Voorhees, Wang, Jou]



Semicoherent IPB Adhesion  
[Freeman, Jerome, Wang]



Bond Topological S/P Relations  
[Eberhart]

TECD

FLAPW

PrecipiCalc-3D

DFrac-3D

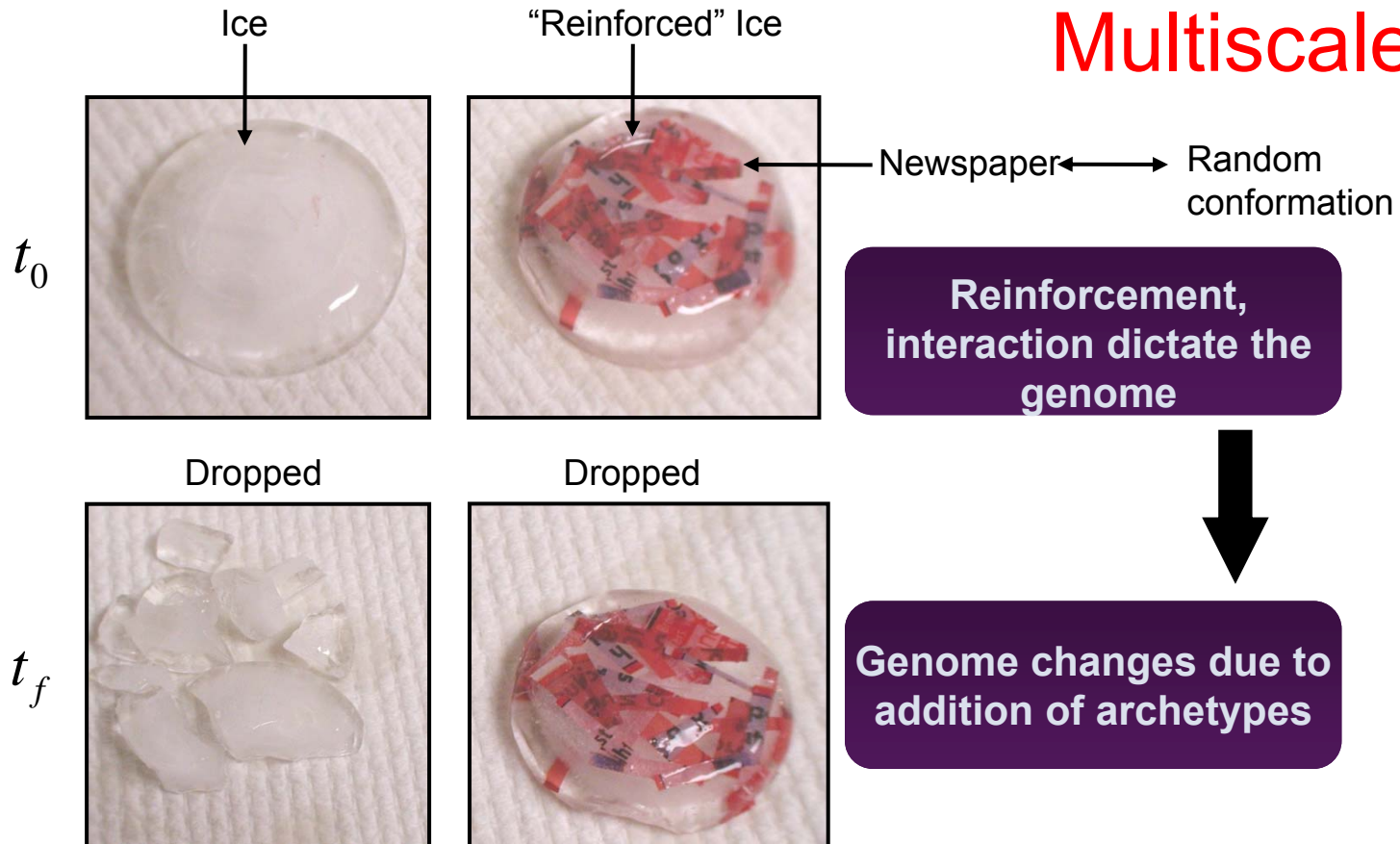
iSIGHT/CMD Integration

Why do we care?

**Genome:** Resistance to Breaking

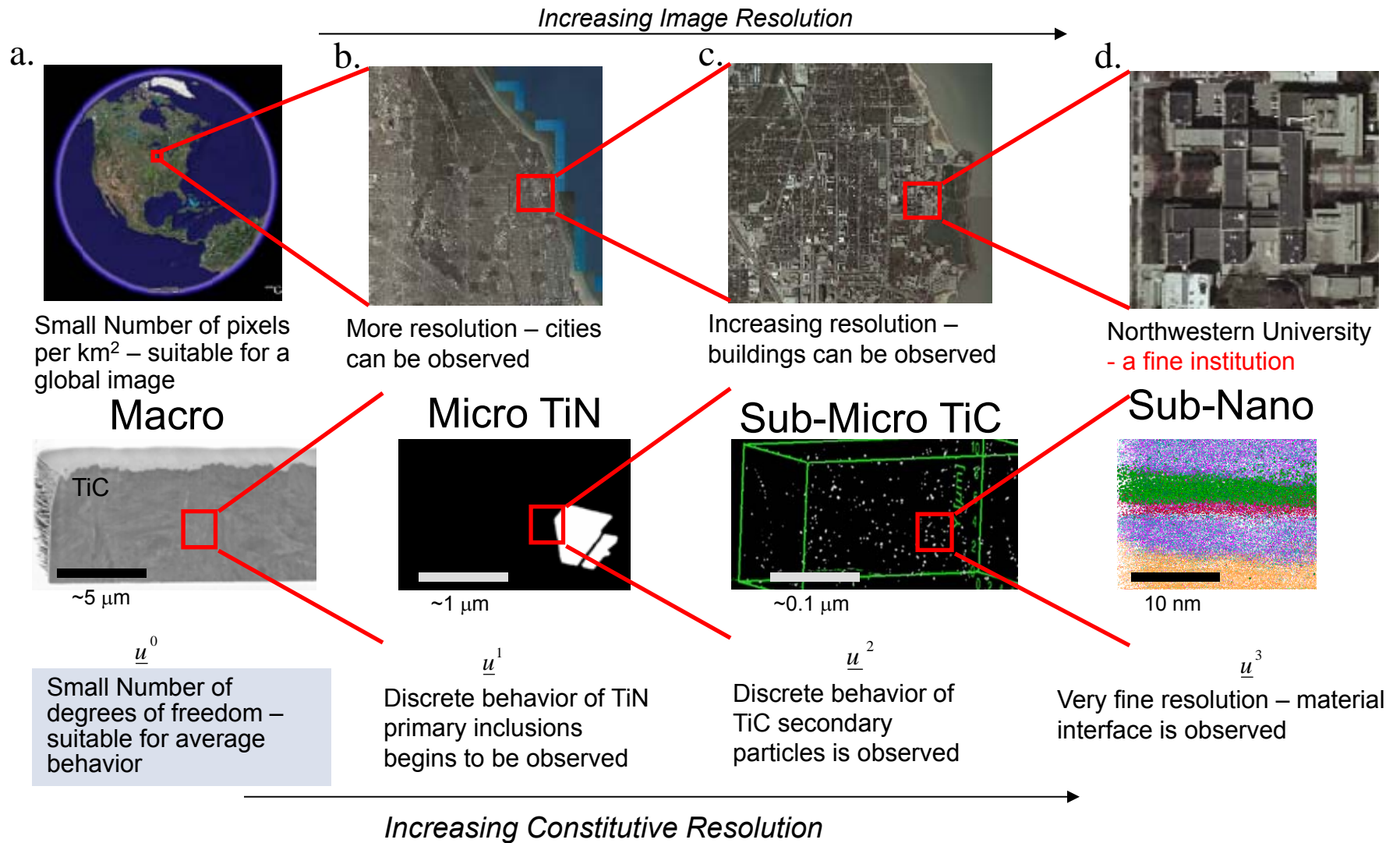
**Archetypes:** 1) ice 2) paper

A simple demonstration



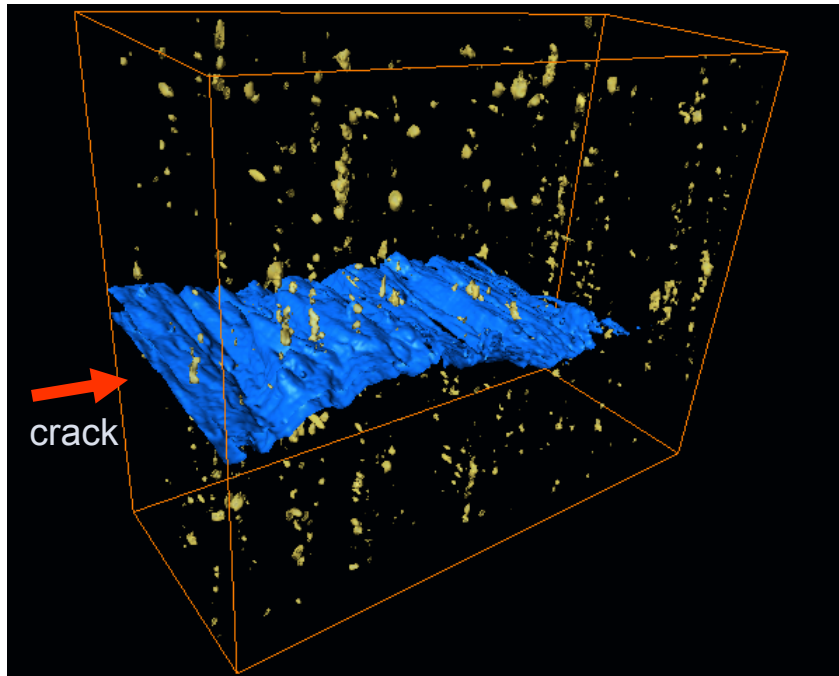
**Experiment was performed by Professor Yip Wah Chung, Northwestern, 2003**

SM. Greene, Y. Li, W. Chen, WK. Liu, "The archetype-genome exemplar in molecular dynamics and continuum mechanics," Computational Mechanics, 2013.

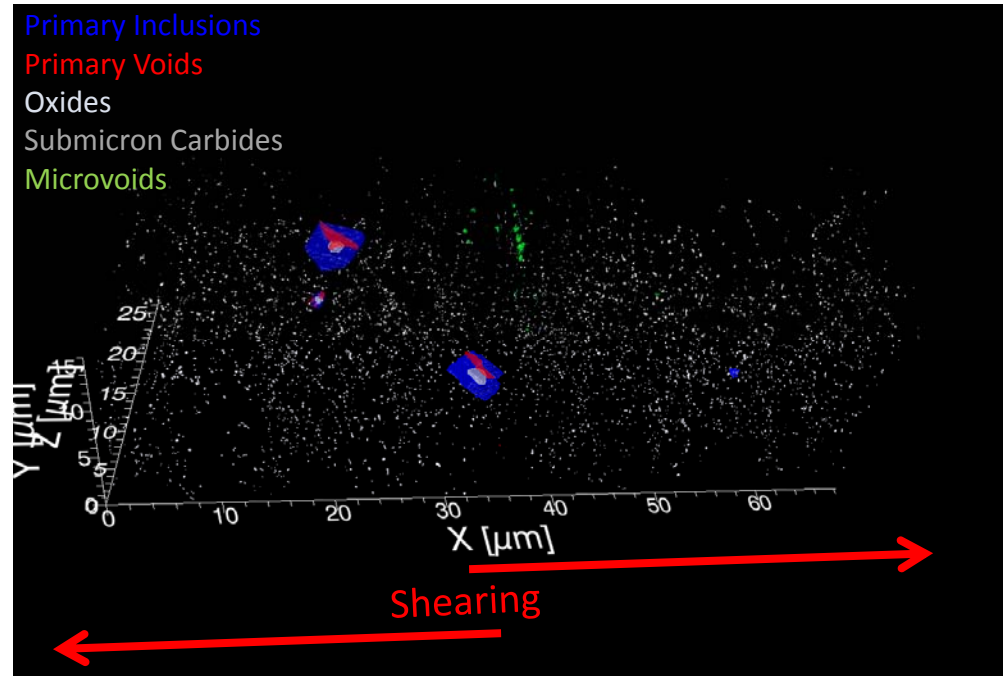


To & Liu et al., Materials integrity in microsystems: a framework for a petascale predictive-science-based multiscale modeling and simulation system, Computational Mechanics, 2008.

Liu et al., Complexity science of multiscale materials via stochastic computations,” International Journal for Numerical Methods in Engineering, 2009.



Mod4330 Crack tip specimen #1:  
 Primary particles (yellow) near crack tip  
 Reconstruction area: 633x516x259  $\mu\text{m}^3$   
 Averaged: 2.857  $\mu\text{m}$   
 Spacing: 16  $\mu\text{m}$   
 Volume fraction: 1.756%

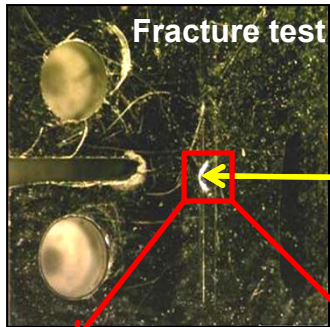
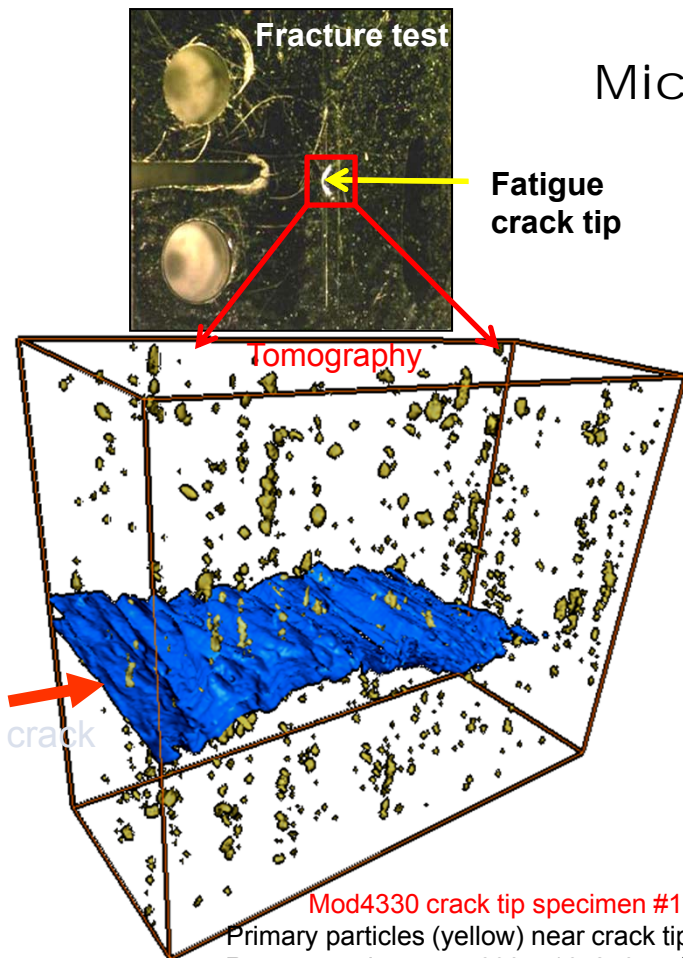


Mod4330 shear specimen:  
 Secondary particles (white dots) inside shear band  
 Reconstruction area: 70x15x28  $\mu\text{m}^3$   
 Averaged: 0.117035  $\mu\text{m}$   
 Spacing: 2  $\mu\text{m}$   
 Volume fraction: 0.0384%

Courtesy of Stephanie Chan (Olson's group), and HJ Jou (QuesTek)

Vernervey, Moran and Liu. "Multiscale Micromorphic Theory for Hierarchical Materials, *JMPS*, 2603-2651, 2007  
 McVeigh & Liu, "Linking microstructure and properties through a predictive multiresolution continuum," *CMAME*, 2008  
 McVeigh & Liu, Multiresolution modeling of ductile reinforced brittle composites. *J. Mech. Phys. Solids*, 2009.  
 Liu et. al., Complexity science of multiscale materials via stochastic computations, *IJNME*, 2009.

Microstructures of Ultra High Strength Alloys



Fatigue crack tip

Tomography

crack

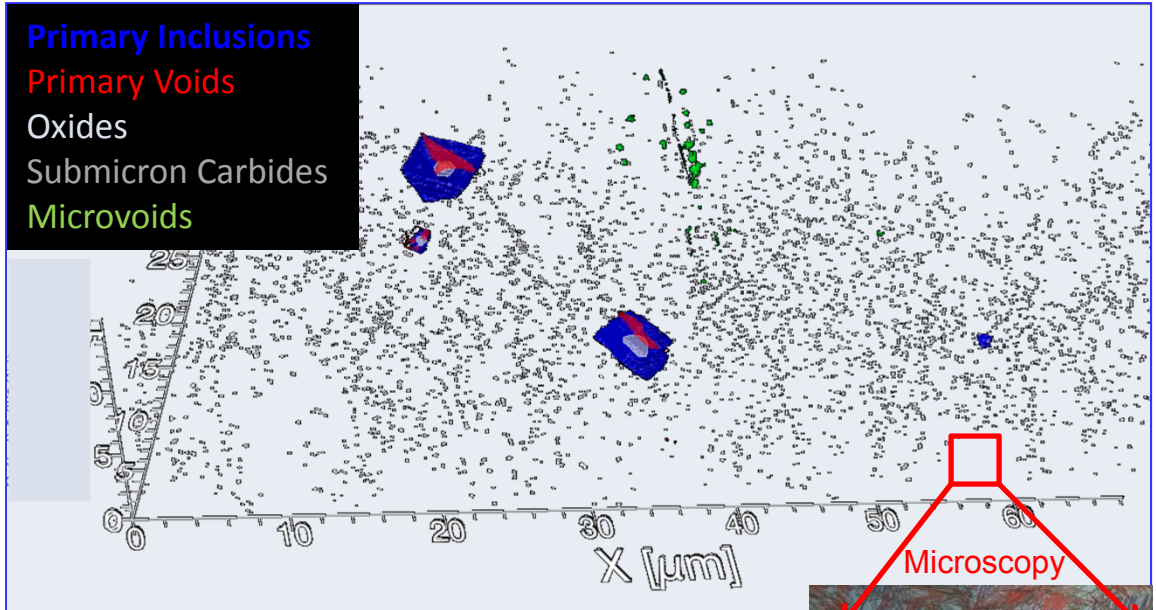
Mod4330 crack tip specimen #1:

Primary particles (yellow) near crack tip  
Reconstruction area: 633x516x259  $\mu\text{m}^3$

Averaged: 4.857  $\mu\text{m}$

Spacing: 16  $\mu\text{m}$

Volume fraction: 1.756%



Primary Inclusions  
Primary Voids  
Oxides  
Submicron Carbides  
Microvoids

Microscopy



Lath martensite

Mod4330 specimen #1:

Secondary particles (white dots) inside shear band

Reconstruction area: 70x15x28  $\mu\text{m}^3$

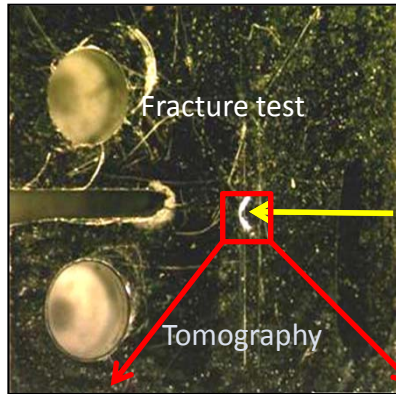
Averaged: 0.117035  $\mu\text{m}$

Spacing: 2  $\mu\text{m}$

Volume fraction: 0.0384%

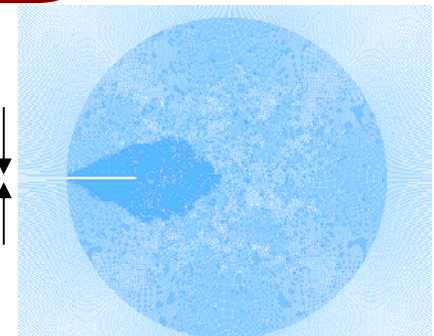
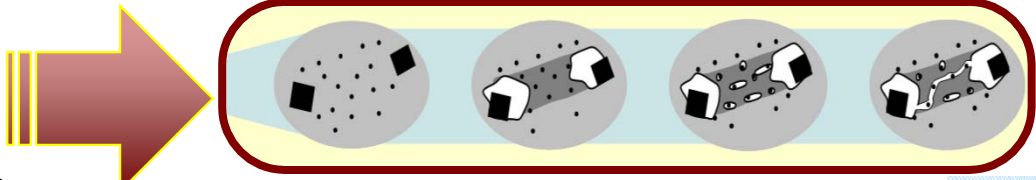
**Multiscale microstructures:** within one grain we see

– primary particles, secondary particles, laths (too many to model explicitly)

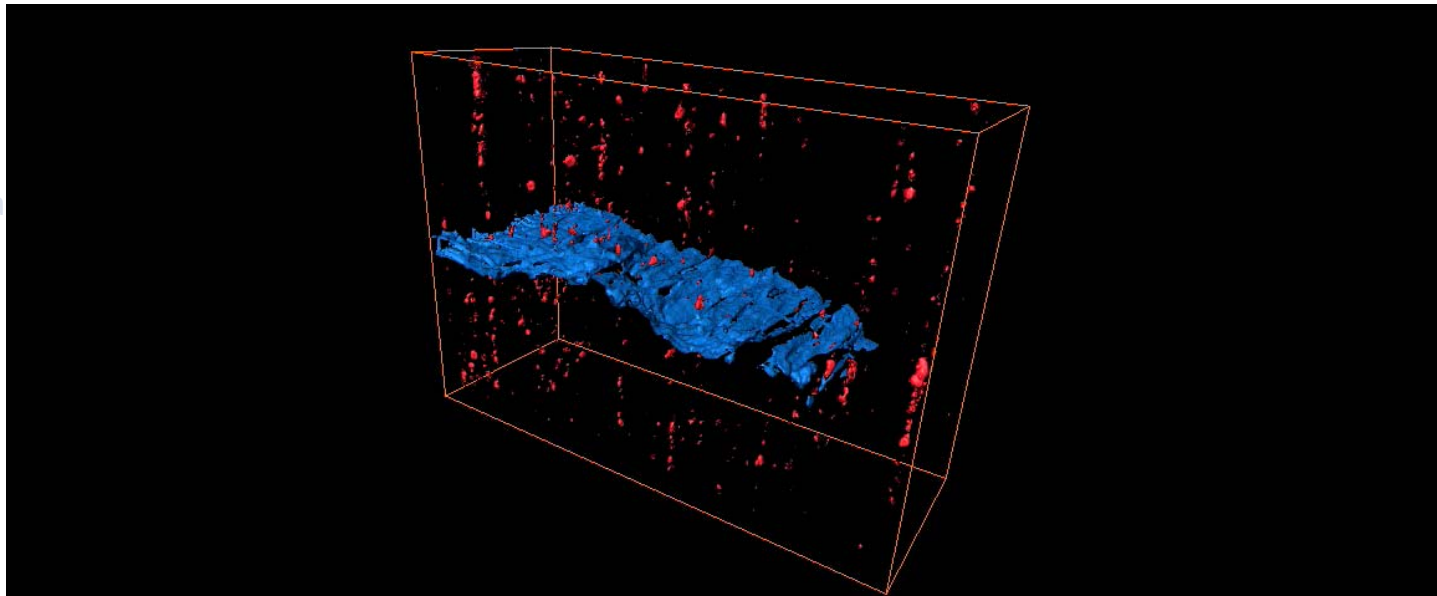
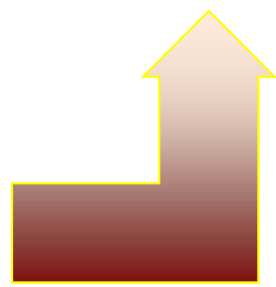


Fatigue crack tip

**Mod4330 crack tip specimen #1:**  
Primary particles (yellow) near crack tip  
Reconstruction area: 633x516x259  $\mu\text{m}^3$   
Averaged: 4.857  $\mu\text{m}$   
Spacing: 16  $\mu\text{m}$   
Volume fraction: 1.756%



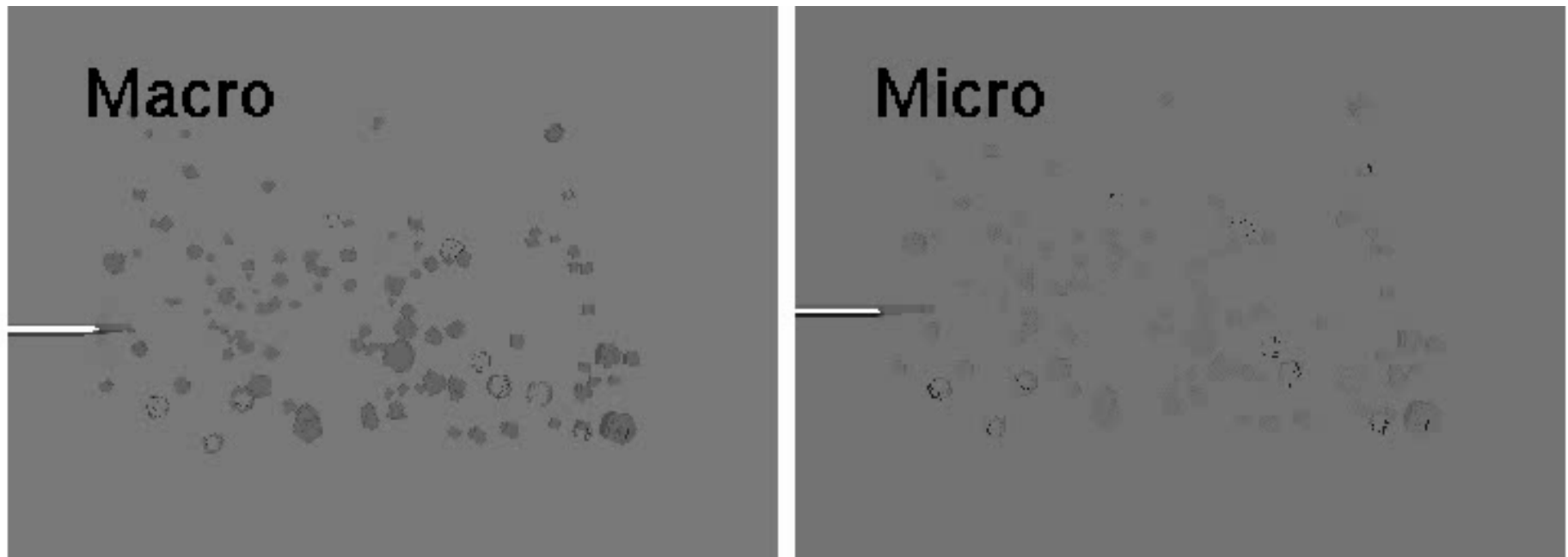
Degrees of Freedom:  
**30 million**  
**(132 particles)**

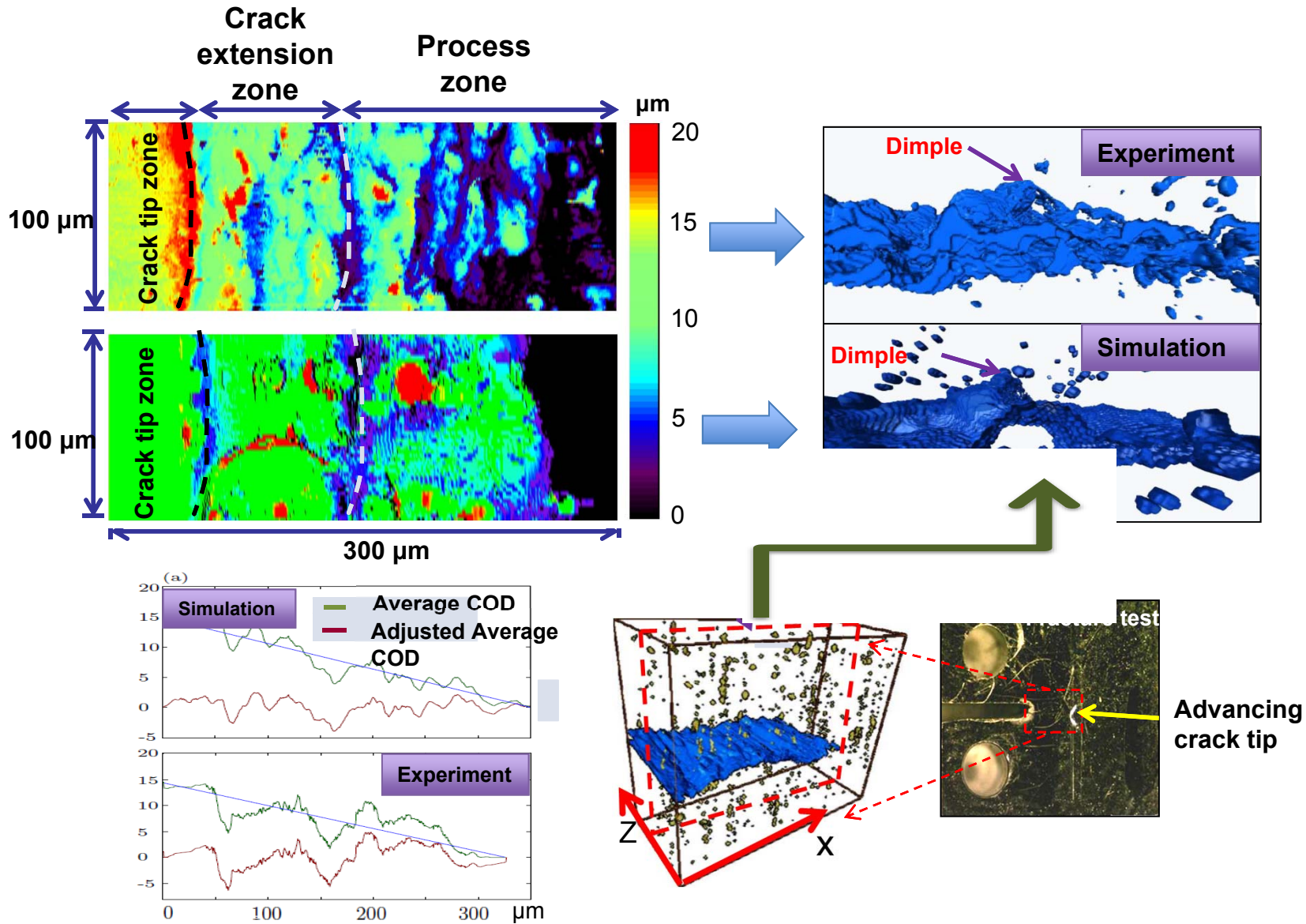


Initial Fatigue Crack Opening is about 3 microns, a load is applied gradually until the material reaches the initial and then final fracture toughness strengths followed by unloading to the final state of deformation

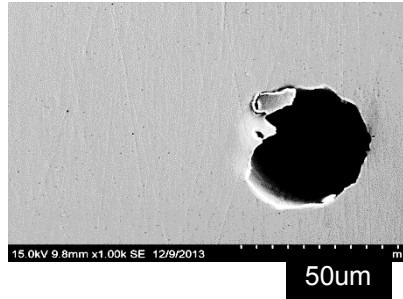
Total experimental time is one minute

The below **MOVIE** shows the **CONCURRENT** interaction of macro and micro effective strains due to submicron and micron voids growth, interaction, coalescence to form Micro and macro defects (mini-cracks) that eventually define the fracture process zone

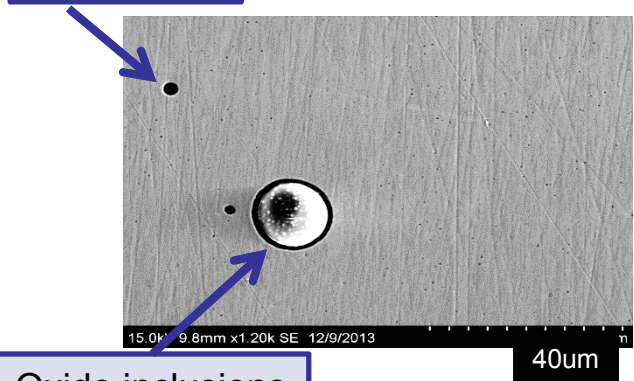






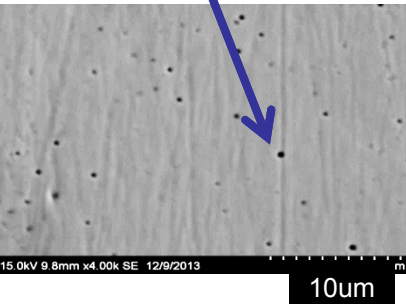


Micro-voids



Oxide inclusions

Submicron voids



**Capturing constituencies**, e.g.

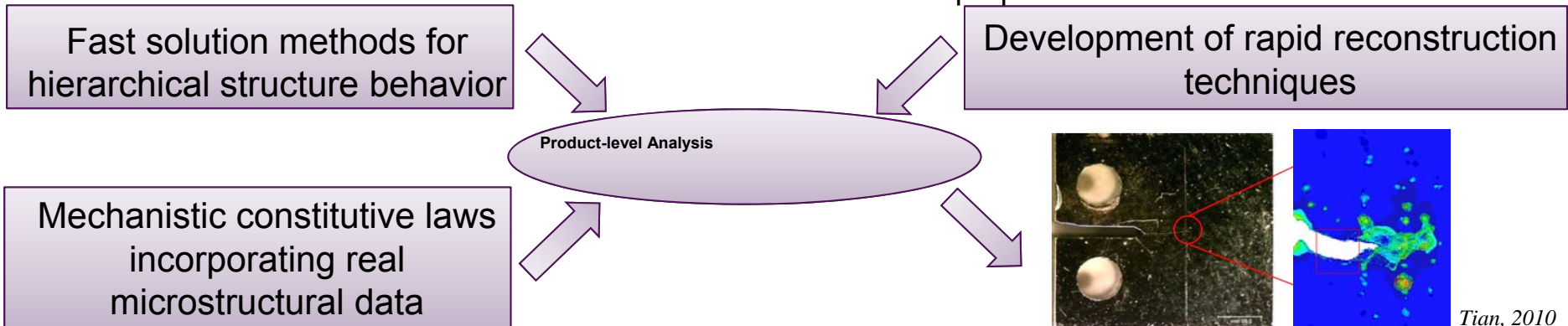
- Strength
- Toughness
- Ductility
- Fatigue life

(GENOME)

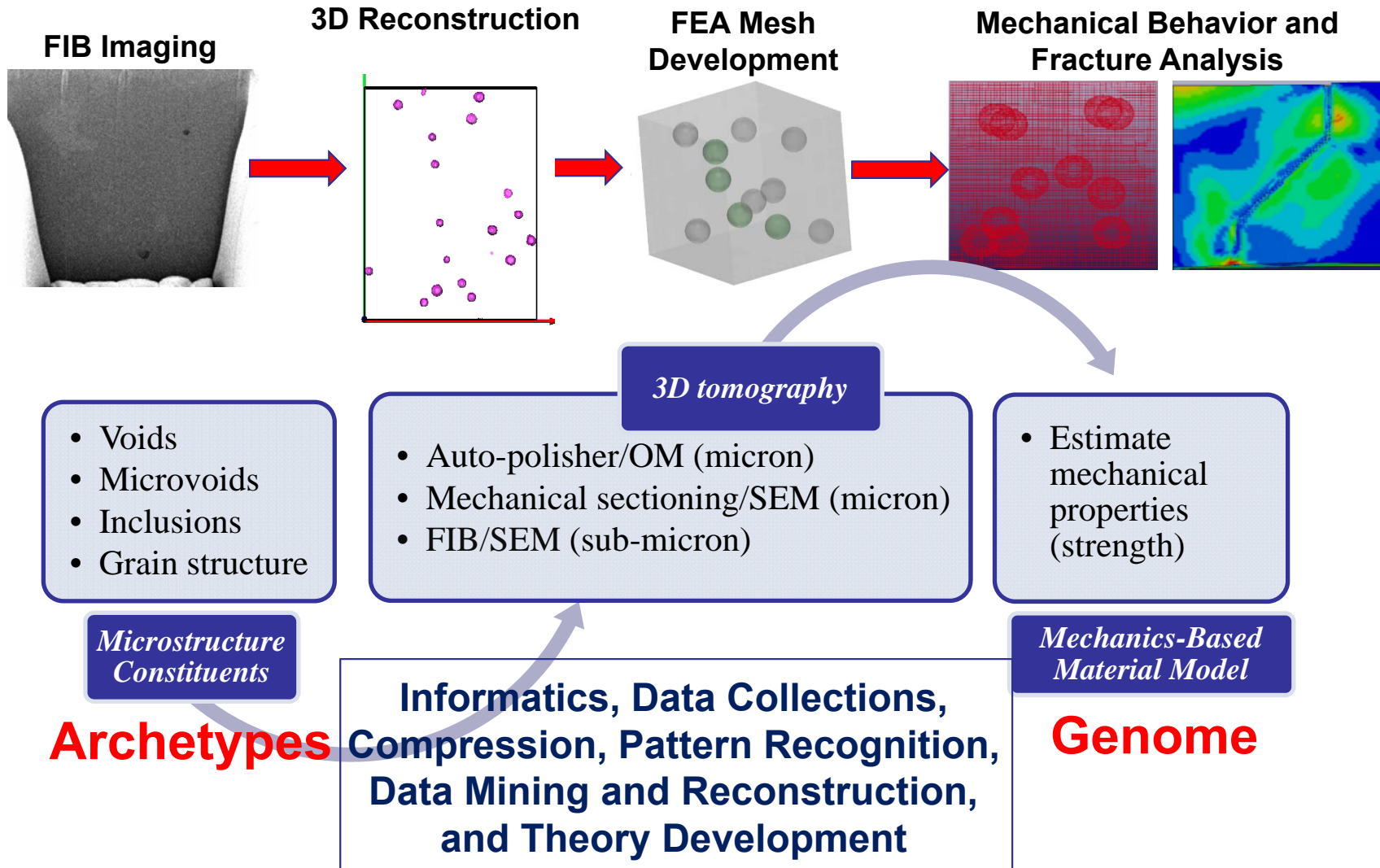
**Requires information** (i.e. microstructure and conformation), e.g.

- Voids
- Inclusions
- Interfaces
- Surface properties

(ARCHETYPES)



**From microstructure (Archetypes) to mechanical property (Genomes) for as-built alloys**



Northwestern Engineering

Information collection, storage, processing and knowledge ordering

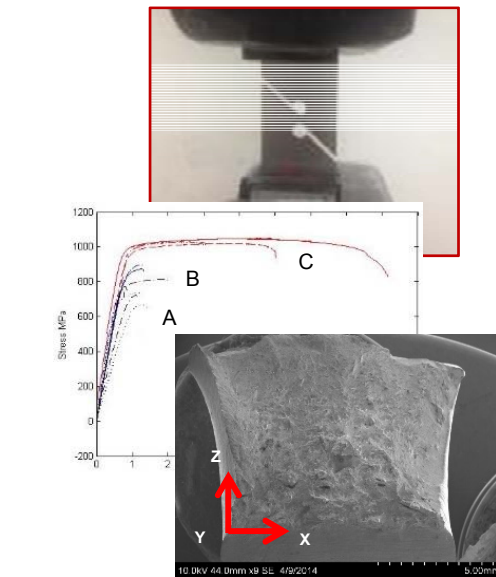
Data Collection

Design

Data Storage

Data Processing

Theory Development

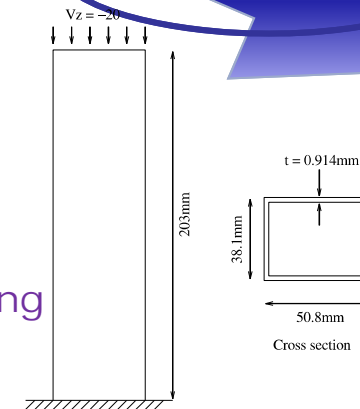


Microstructural and property characterization



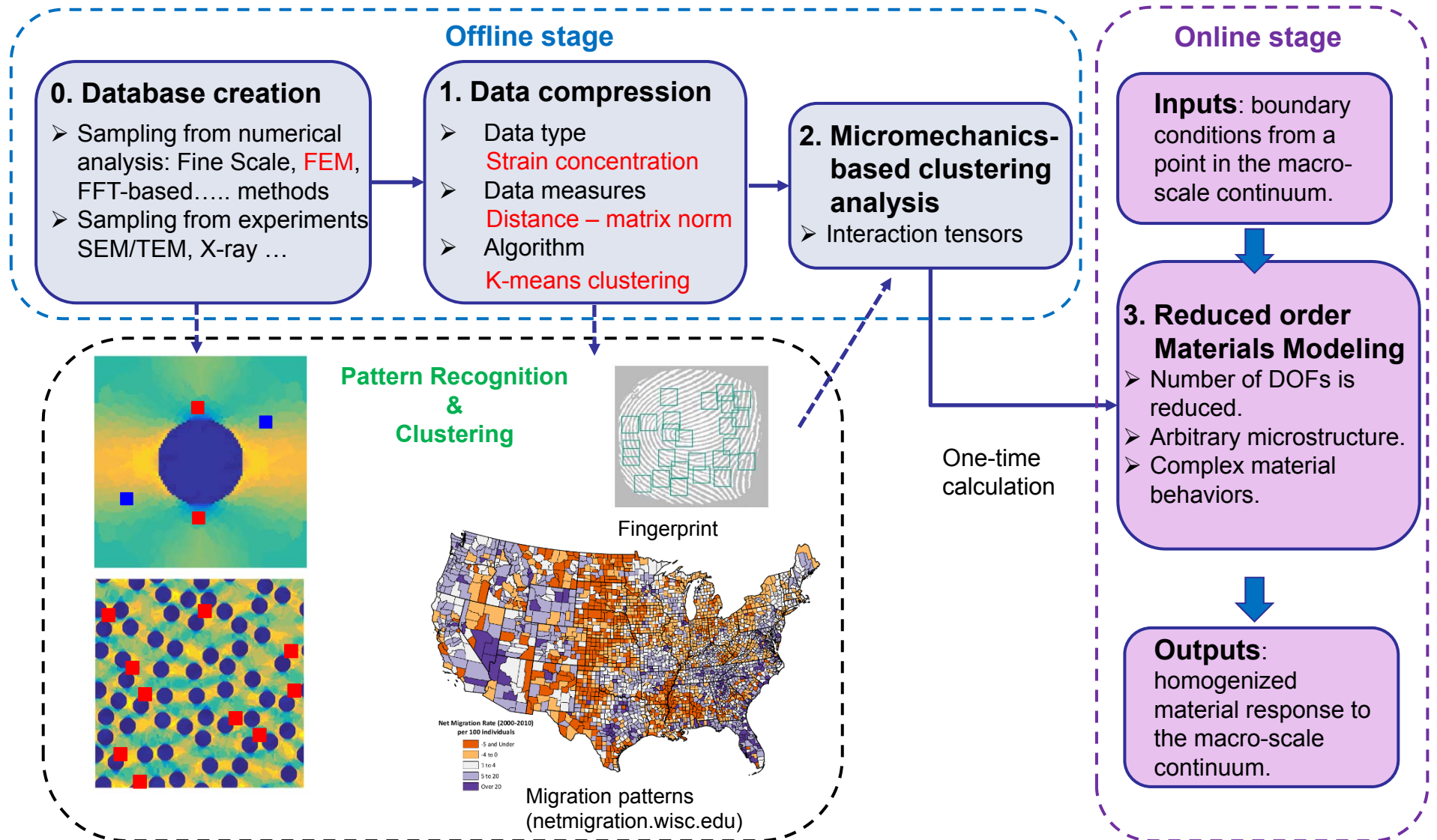
pattern  
information  
search  
behavior  
assess  
relationship  
evaluate  
impact  
analysis  
discovery

Advanced material modeling

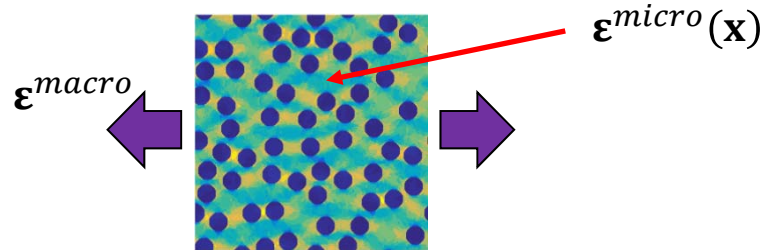


## Northwestern Engineering

- S. Chan O'Keefe, S. Tang, AM Kopacz, J Smith, DJ Rowenhorst, G Spanos, WK Liu, GB Olson, Multiscale Ductile Fracture Integrating Tomographic Characterization and 3D Simulation, *Acta Materialia*, 82, (2015).
- TR Lee, MS Greene, Z Jiang, AM Kopacz, P Decuzzi, W Chen, WK Liu, "Quantifying uncertainties in the microvascular transport of nanoparticles", *Biomech. Model. Mechanobiol.*, 2014, 13, 515-526.
- Steven Greene, Ying Li, Wei Chen, Wing Kam Liu, "The archetype-genome exemplar in molecular dynamics and continuum mechanics," *Computational Mechanics*, Volume 53, Issue 4 (2014), Page 687-737.
- Y Li, W Stroberg, TR Lee, HS Kim, H Man, D Ho, P Decuzzi, WK Liu, "Multiscale Modeling and Uncertainty Quantification in Nanoparticle mediated Drug/Gene Delivery," *Computational Mechanics*, (2014) 53:511–537.
- Khalil I Elkhodary; Michael S Greene; Shan Tang; Ted Belytschko; Wing K Liu, "Archetype-blending continuum theory," *Comput. Methods Appl. Mech. Engrg.* 254 (2013) 309–333.
- Yu Liu, M. Steven Greene, Wei Chen, Dmitriy A. Dikin, Wing Kam Liu, "Computational microstructure characterization and reconstruction for stochastic multiscale material design," *Computer-Aided Design*, 45, 2013.
- MS. Greene, H. Xu, S. Tang, W. Chen, WK Liu, "A generalized uncertainty propagation criterion from benchmark studies of microstructured material systems," *Comput. Methods Appl. Mech. Engrg.*, 254, 2013, Pages 271–291.
- H Xu, H Deng, C Brinson, D Dikin, WK Liu, W Chen, MS Greene, C. Burkhart, G Papakonstantopoulos, M Poldneff, "STOCHASTIC REASSEMBLY FOR MANAGING THE INFORMATION COMPLEXITY IN MULTILEVEL ANALYSIS OF HETEROGENEOUS MATERIALS," *Proceedings of ASME 2012 International Design Engineering Technical Conferences & Computers and Information in Engineering Conference*, DETC2012-70668, 2012.
- Greene M.S., Liu, Y., Chen, W., Liu, W.K., "Computational Uncertainty Analysis in Multiresolution Materials via Stochastic Constitutive Theory", *Computer Methods in Applied Mechanics and Engineering*, (2011), **200**.
- W. K. Liu, T. Belytschko and A. Mani, "Random Field Finite Elements," *Int J for Numl Methods in Eng*, 23, 1986.
- W. K. Liu, T. Belytschko and A. Mani, "Probabilistic Finite Elements for Nonlinear Structural Dynamics," *CMAME*, 56, 1986.



- **Data type:** strain concentration tensor  $A(\mathbf{x})$  in the RVE for linear elastic material.



For 2D plane strain material,  $A(\mathbf{x})$  has **9 independent components**, determined by *a priori* simulations under **3 orthogonal loading conditions**.

- **Data format:**

EIndex	$A_{11}$	$A_{22}$	$A_{33}$	$A_{12}$	$A_{21}$	$A_{23}$	$A_{32}$	$A_{13}$	$A_{31}$
1	-	-	-	-	-	-	-	-	-
2	-	-	-	-	-	-	-	-	-
⋮			⋮			⋮			⋮
$N$	-	-	-	-	-	-	-	-	-

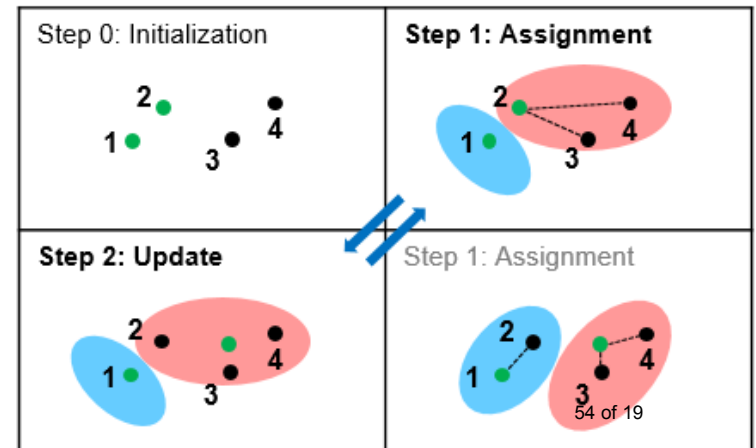
\*  $N$ : total number of elements (observations) in the RVE

$\epsilon^{micro}(\mathbf{x}) = A(\mathbf{x}) : \epsilon^{macro}$   
 strain concentration tensor  $A(\mathbf{x})$   
 microscopic strain  $\epsilon^{micro}(\mathbf{x})$   
 macroscopic strain  $\epsilon^{macro}$

$$\begin{bmatrix} \epsilon_1^{local} \\ \epsilon_2^{local} \\ \epsilon_3^{local} \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{bmatrix} \begin{bmatrix} \epsilon_1^{macro} \\ \epsilon_2^{macro} \\ \epsilon_3^{macro} \end{bmatrix}$$

- **Compression algorithm:**

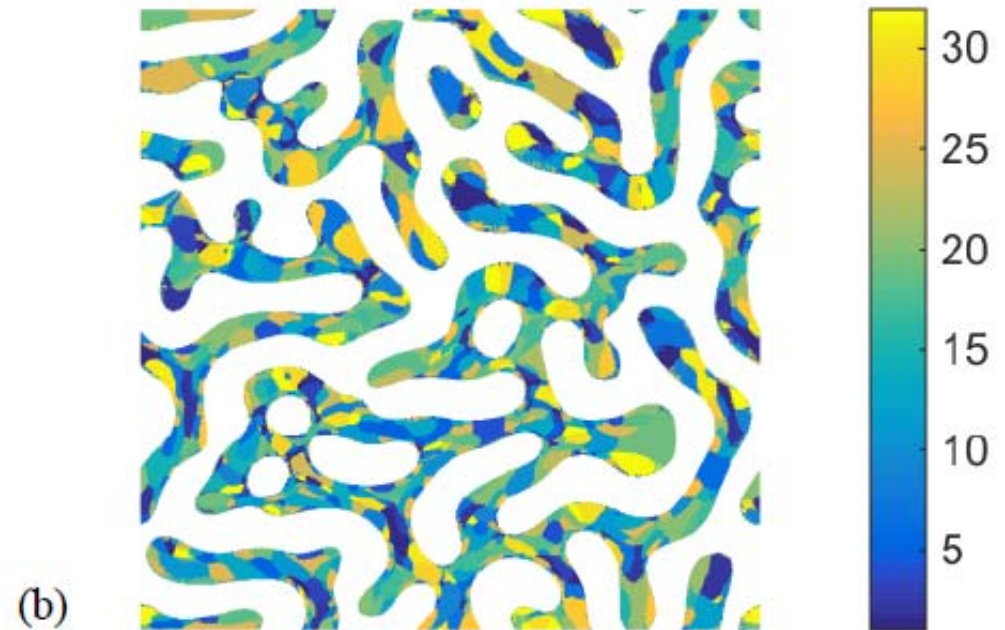
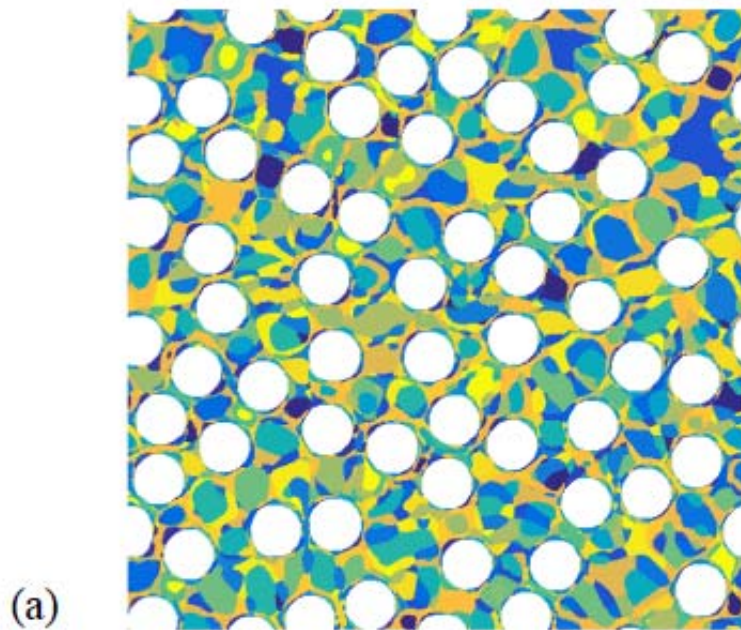
k-means clustering



**K-means clustering – results**

Fiber-reinforced composite ( $\nu_f = 30\%$ )

Phase-field structure ( $\nu_f = 50\%$ )



DNS:  $600 \times 600$

DNS:  $600 \times 600$

Proposed method – offline stage

We omit the details as the paper is not published yet



**Reduced order constitutive modeling**

(1)

(2)

By substituting (2) into (1), we obtained

(3)

(4)

We omit the details as the paper is not published yet

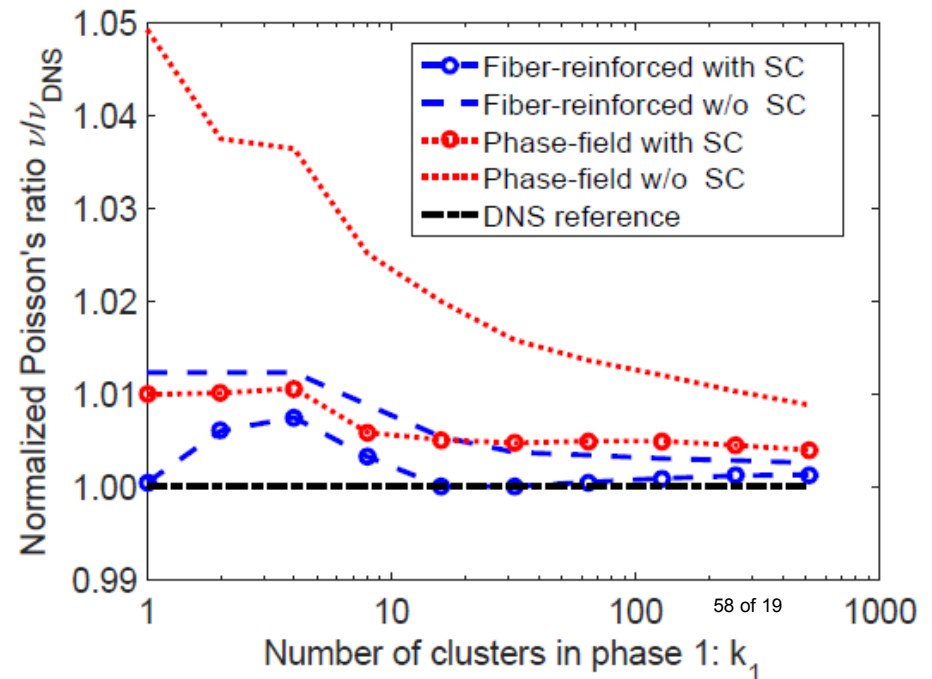
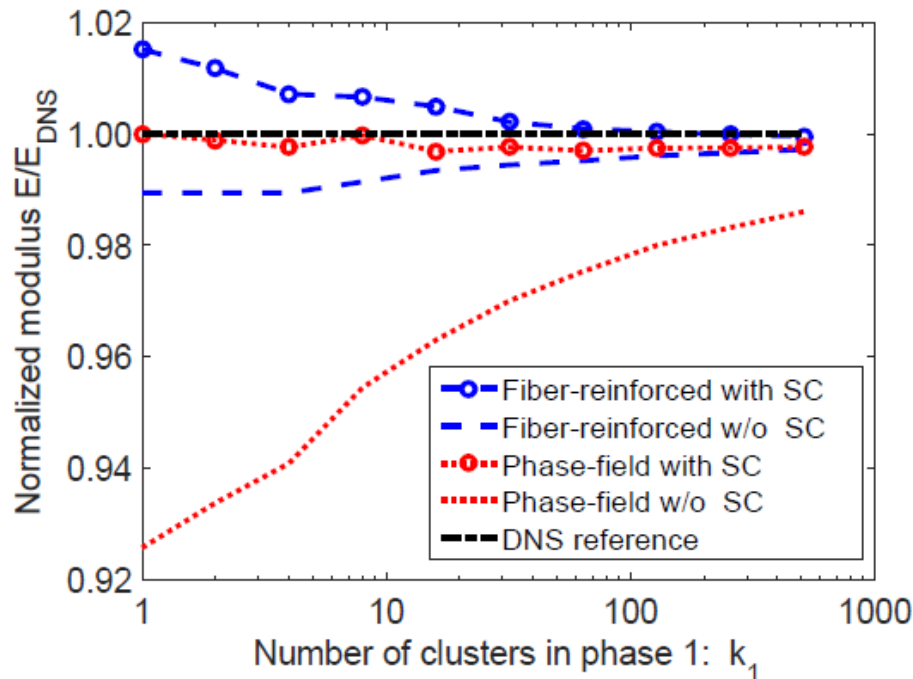
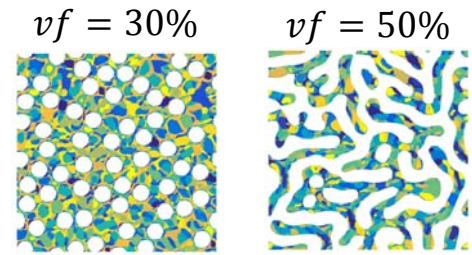
Elastic Material – The effect of number of clusters

$E_1 = 100 \text{ MPa}, \nu_1 = 0.3;$  Matrix  
 $E_2 = 500 \text{ MPa}, \nu_2 = 0.19.$  Inclusion

same as the ones we used for building the database

- DNS results from FE analysis with  $600 \times 600$  mesh.

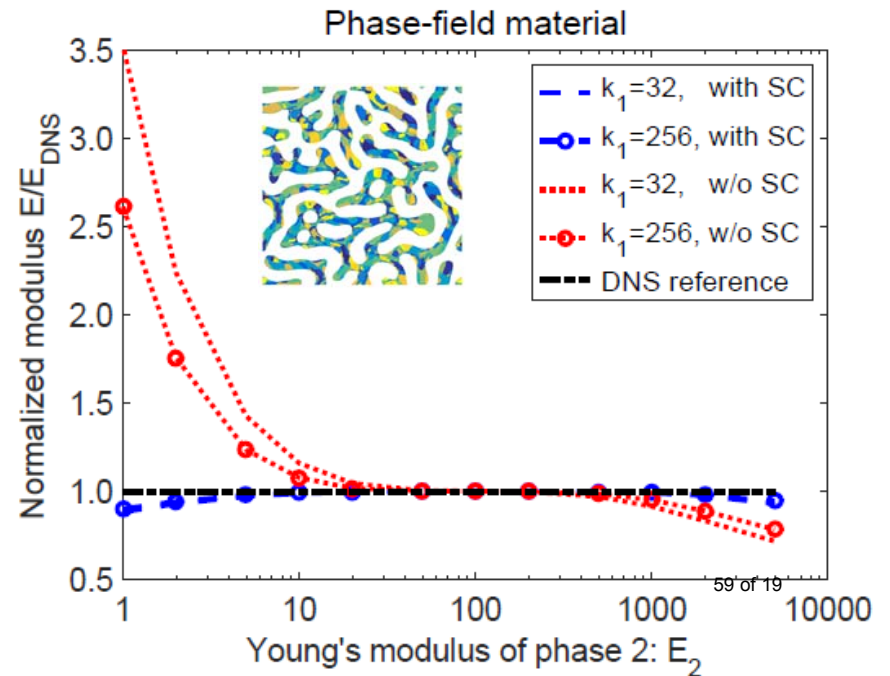
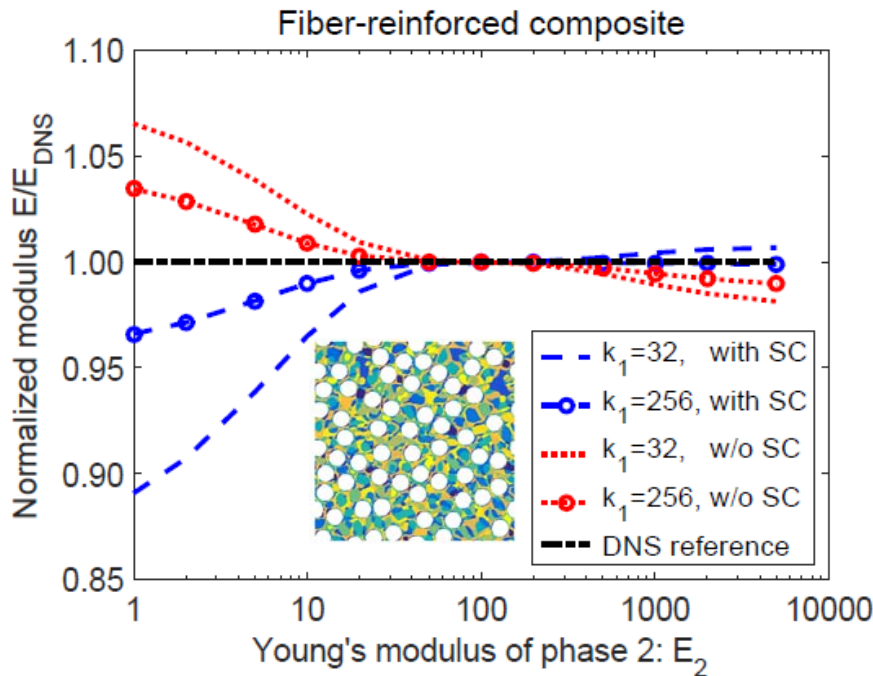
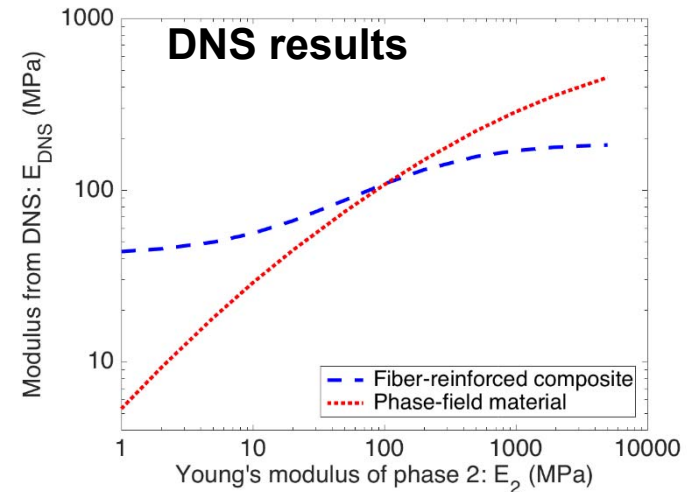
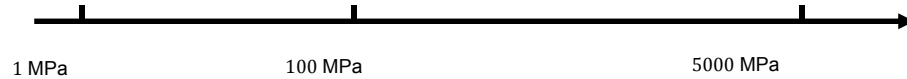
- Fiber-reinforced composite:  $E_{\text{DNS}} = 156.43 \text{ MPa}, \nu_{\text{DNS}} = 0.391.$
- Phase-field material:  $E_{\text{DNS}} = 220.79 \text{ MPa}, \nu_{\text{DNS}} = 0.350.$



**Elastic Material – the effect of phase modulus**

$$E_1 = 100 \text{ MPa}, \nu_1 = 0.3; \quad \nu_2 = 0.19.$$

Change  $E_2$  (inclusion)



**Elasto-plastic Material – The importance of the self-consistent (SC) method**

- Elastic domain

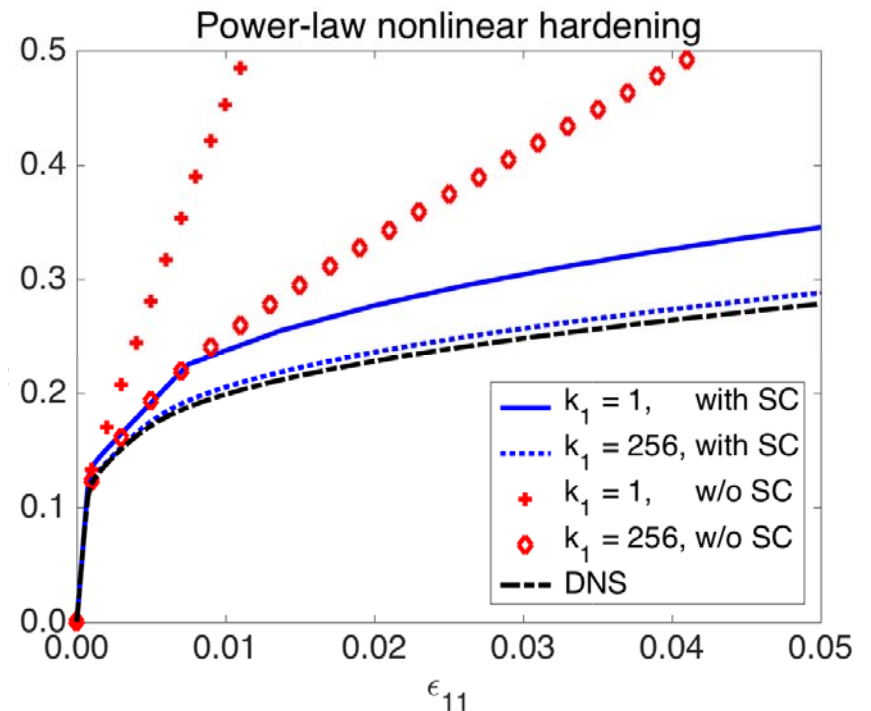
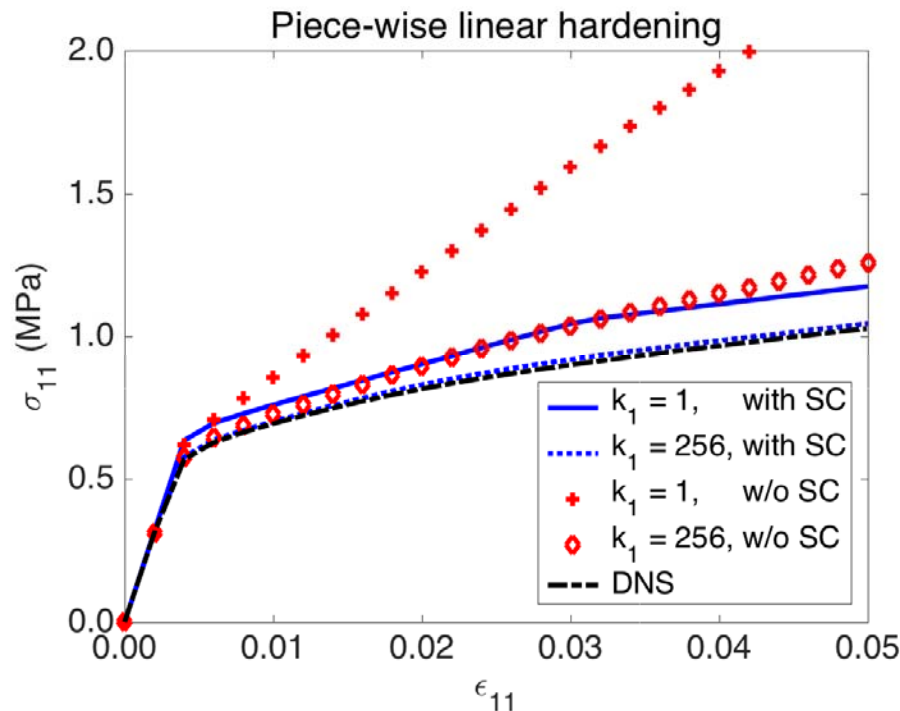
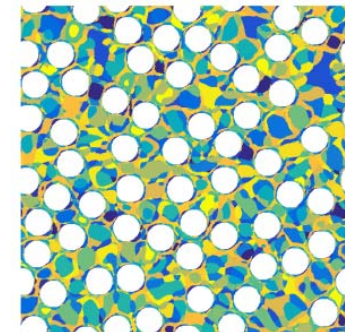
$$E_1 = 100 \text{ MPa}, \nu_1 = 0.3; \quad E_2 = 500 \text{ MPa}, \nu_2 = 0.19.$$

- Plastic domain: J-2 plasticity

$$f = \bar{\sigma} - \sigma_Y(\bar{\varepsilon}) \leq 0, \quad \sigma_Y(\bar{\varepsilon}) = \begin{cases} 0.5 + 5\bar{\varepsilon} & \bar{\varepsilon} \in [0, 0.04) \\ 0.7 + 2\bar{\varepsilon} & \bar{\varepsilon} \in [0.04, \infty) \end{cases} \text{ MPa}$$

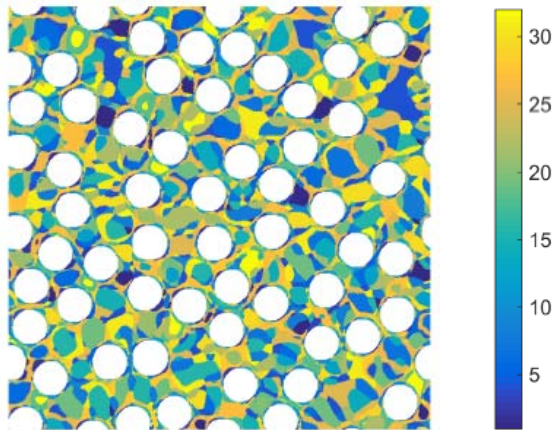
$$\sigma_Y(\bar{\varepsilon}) = 0.1 + 0.3\bar{\varepsilon}^{0.4} \text{ MPa.}$$

Fiber-reinforced composite



Importance of the raw data type

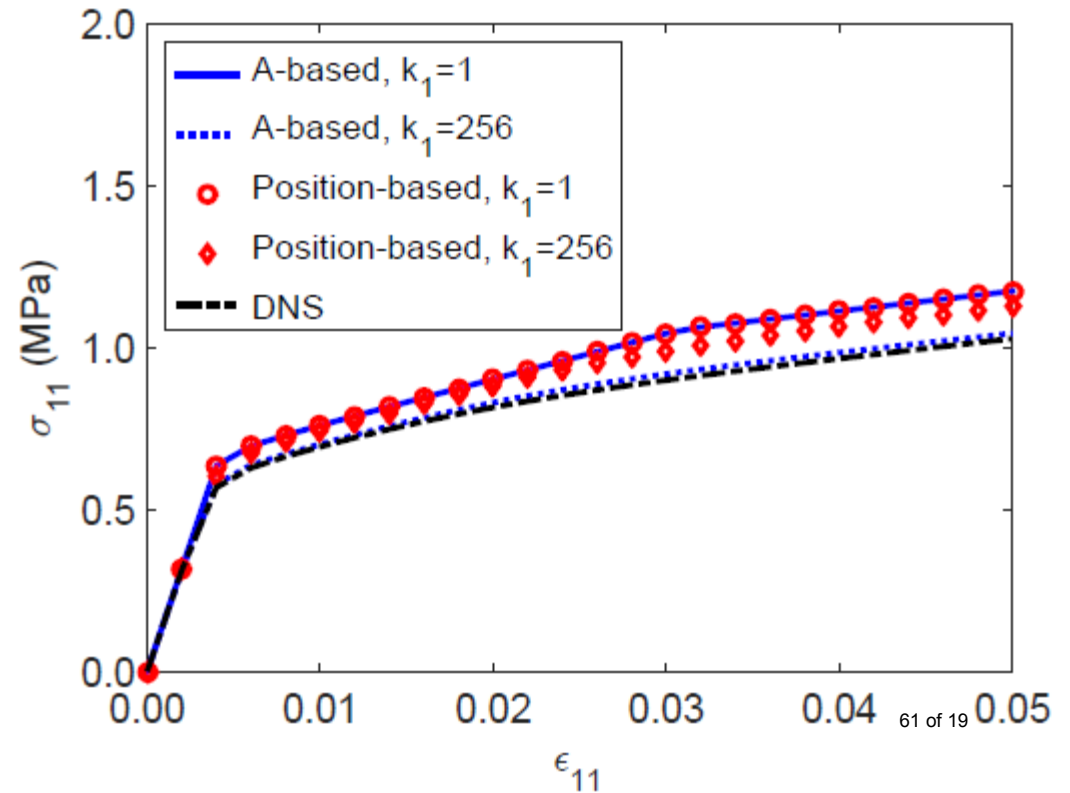
Strain concentration tensor:  $A(\mathbf{x})$



Spatial coordinates / Position:  $\mathbf{x}$



- We use  $A(\mathbf{x})$  in order to capture the mechanical behaviors. Differently, the clustering can be also purely based on the **spatial coordinates  $\mathbf{x}$**  of the data points, similar to the meshing in FEM...

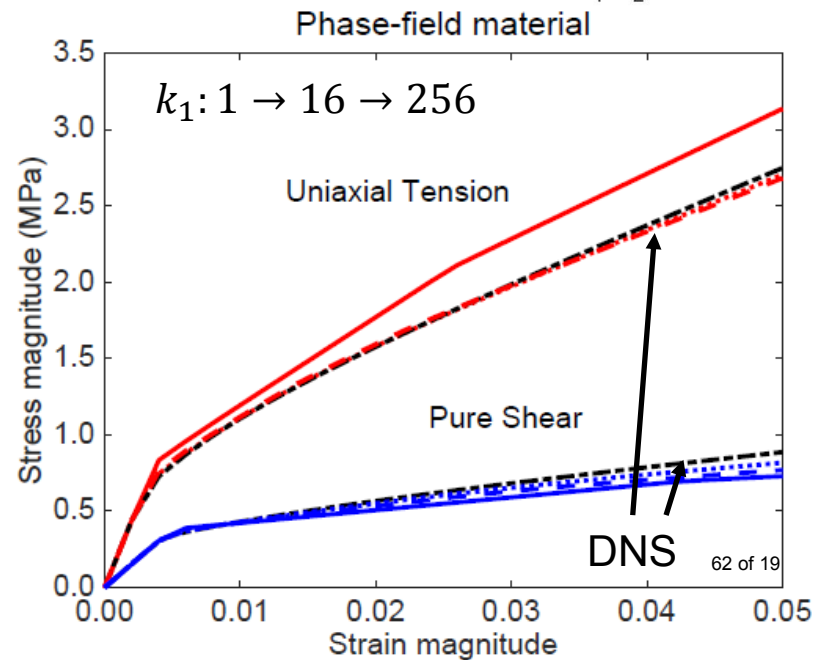
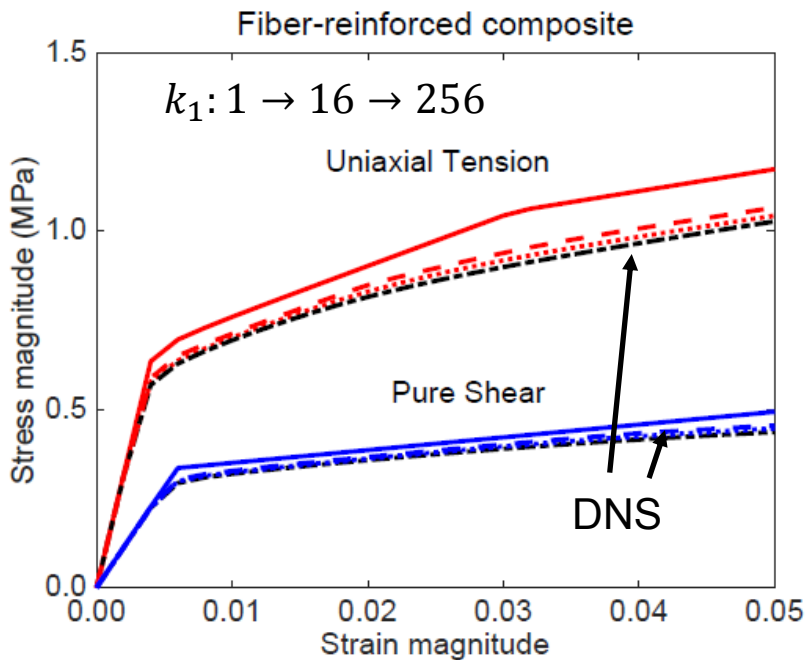
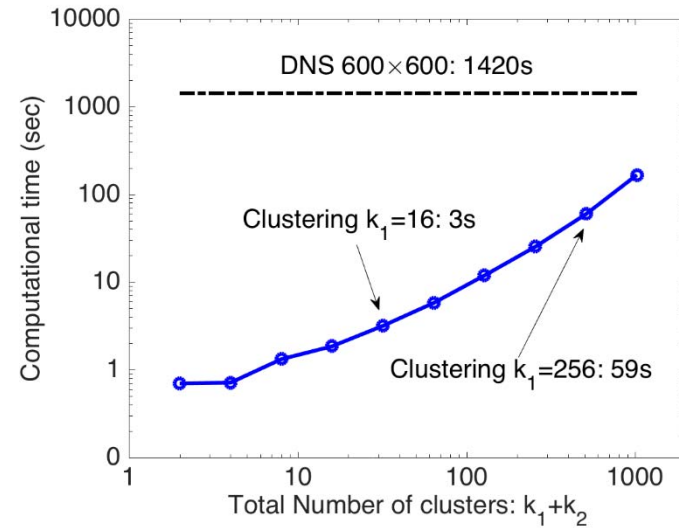


**Computational time**

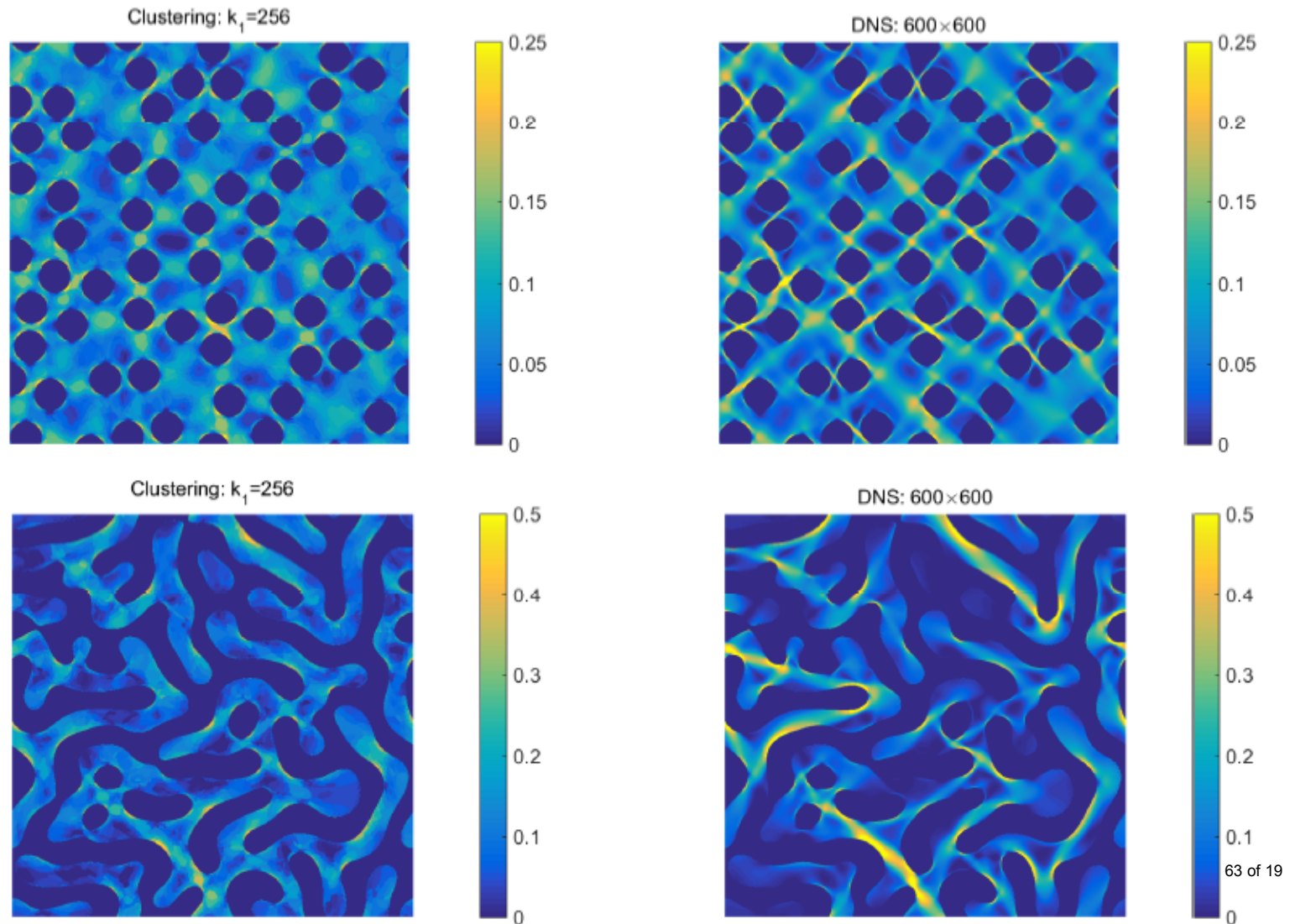
- Implicit elasto-plastic simulations with **25 incremental steps**.
- Performed on one Inter® Core i7-3632QM

DNS  $600 \times 600$ : **Abaqus standard**

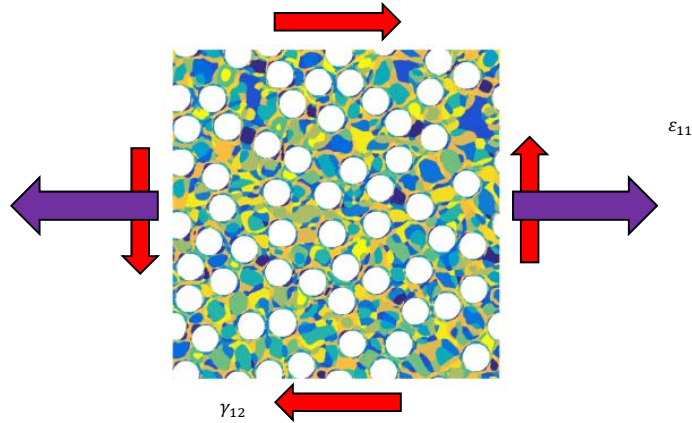
Proposed reduced order model: **Matlab**



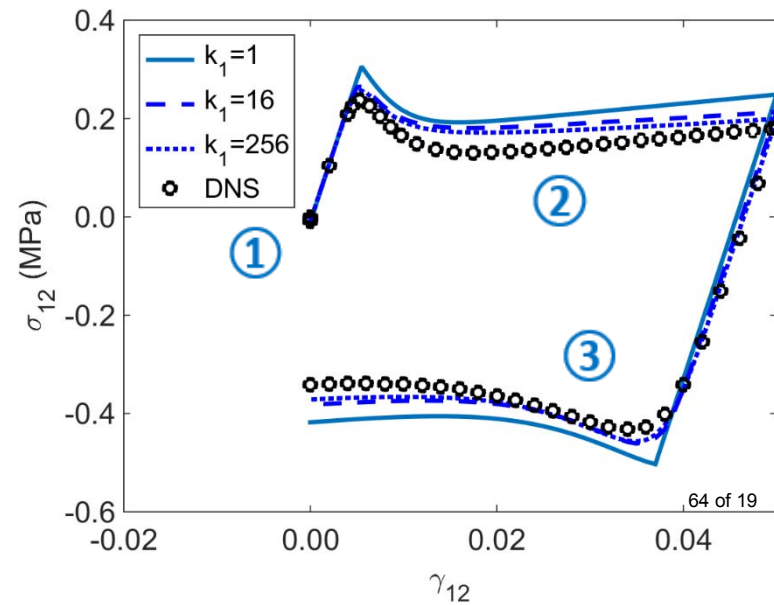
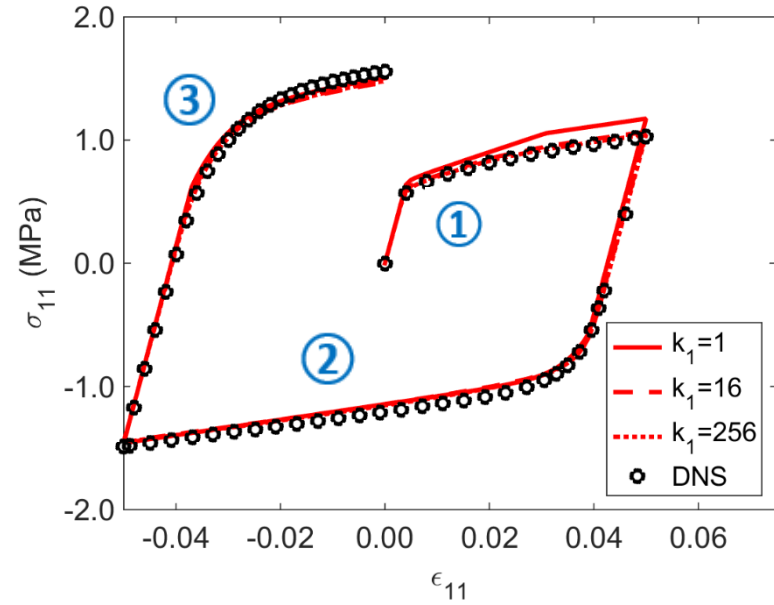
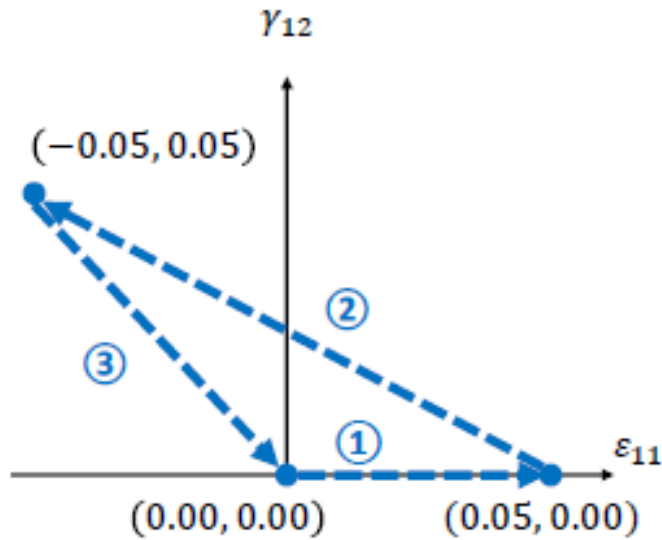
## Comparison of the effective plastic strain field



A complex loading path in 2D

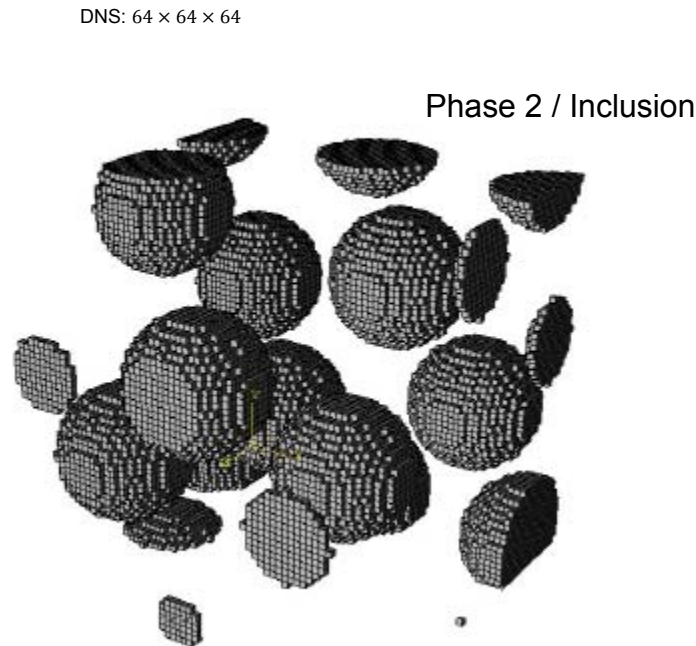


- No constraint on  $\epsilon_{22}$





3D results and the computational time



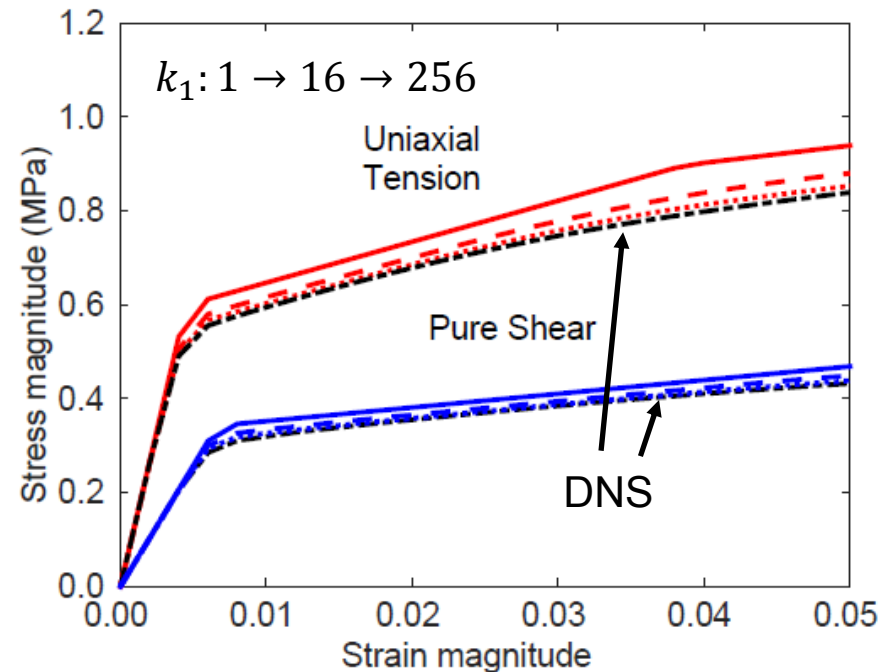
- Elastic domain

$$E_1 = 100 \text{ MPa}, \nu_1 = 0.3;$$

$$E_2 = 500 \text{ MPa}, \nu_2 = 0.19.$$

- Plastic domain: J-2 plasticity

$$\sigma_Y(\bar{\epsilon}) = \begin{cases} 0.5 + 5\bar{\epsilon} & \bar{\epsilon} \in [0, 0.04) \\ 0.7 + 2\bar{\epsilon} & \bar{\epsilon} \in [0.04, \infty) \end{cases} \text{ MPa}$$

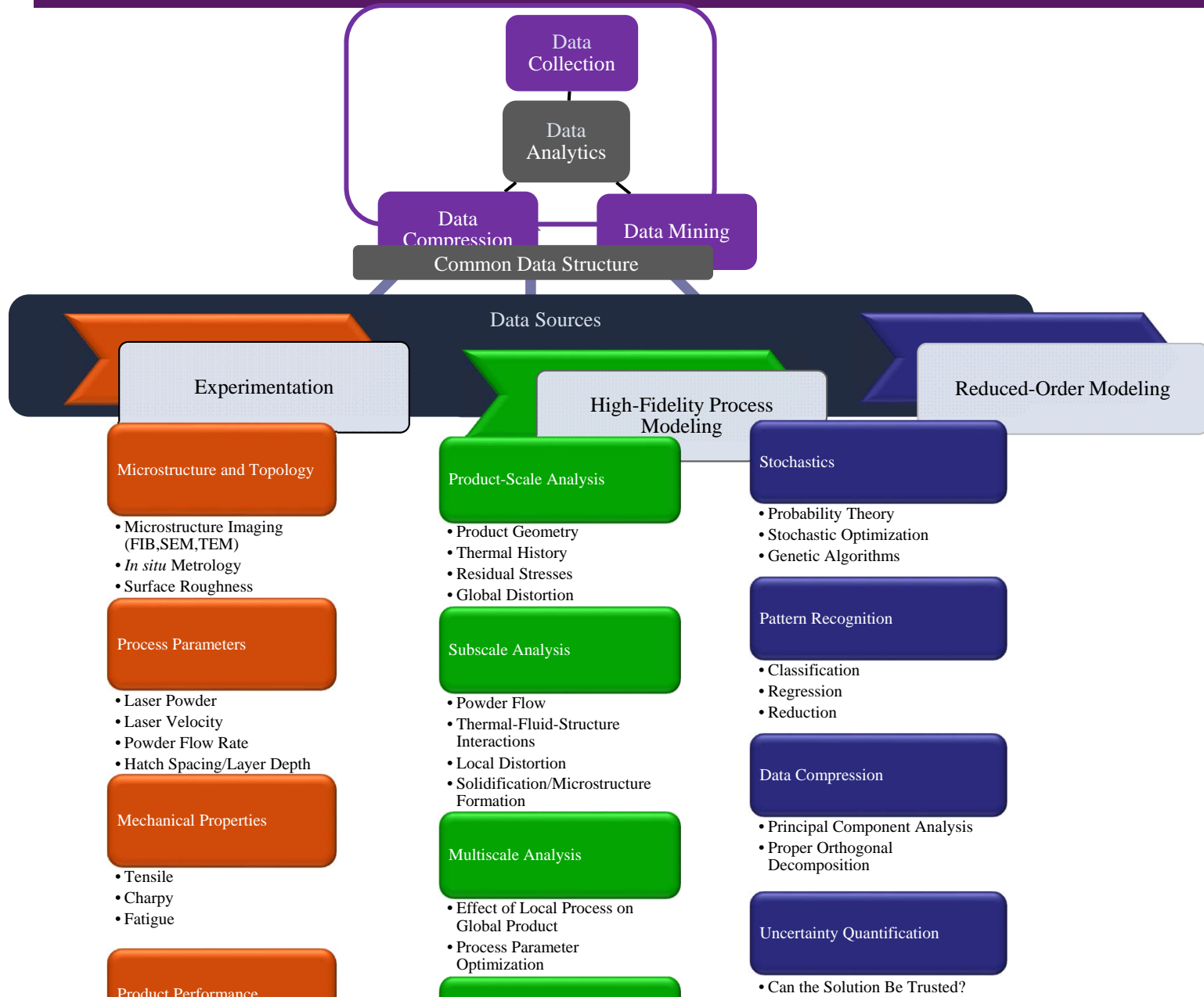


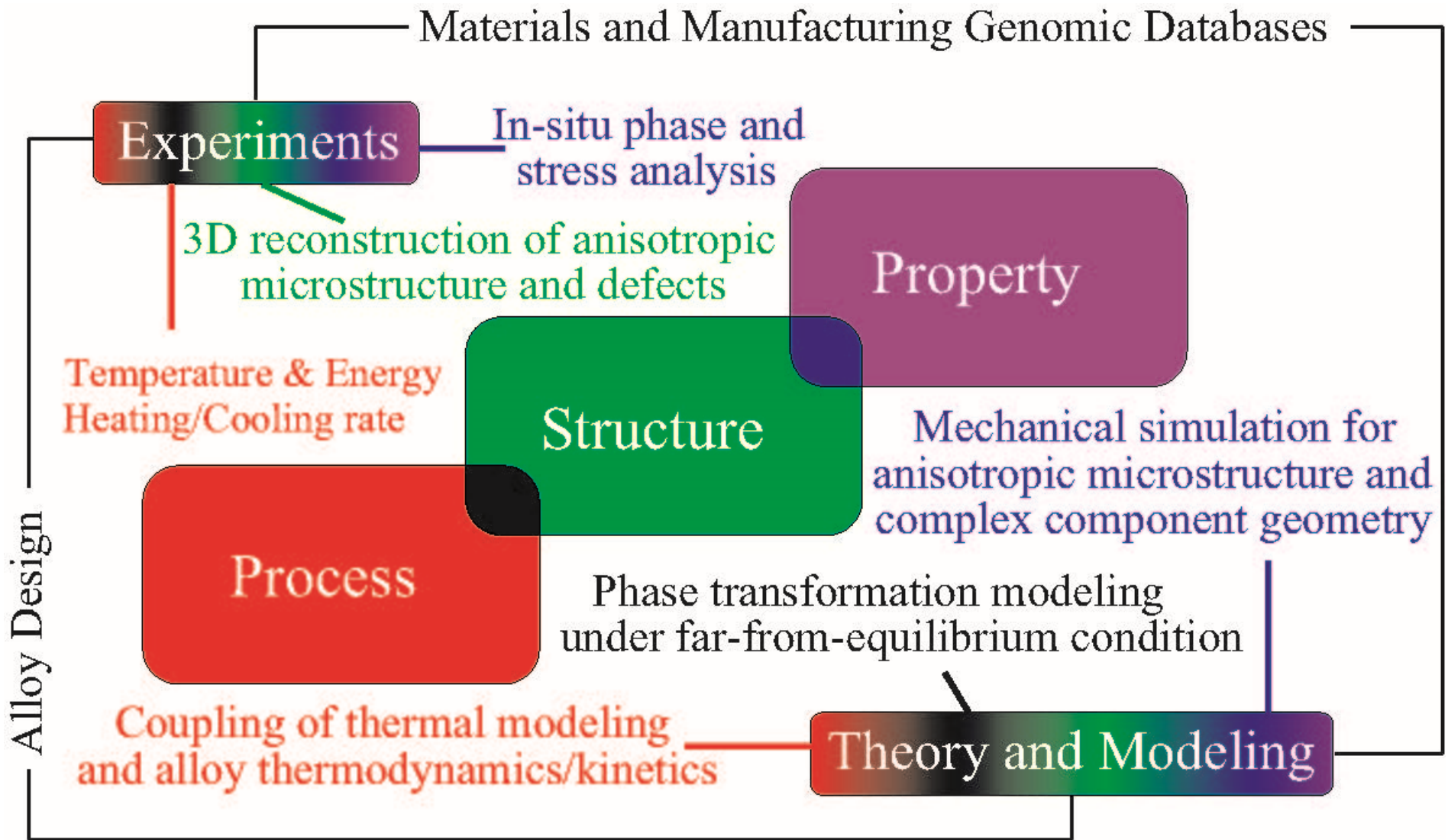
- Implicit elasto-plastic simulations with **25 incremental steps**.

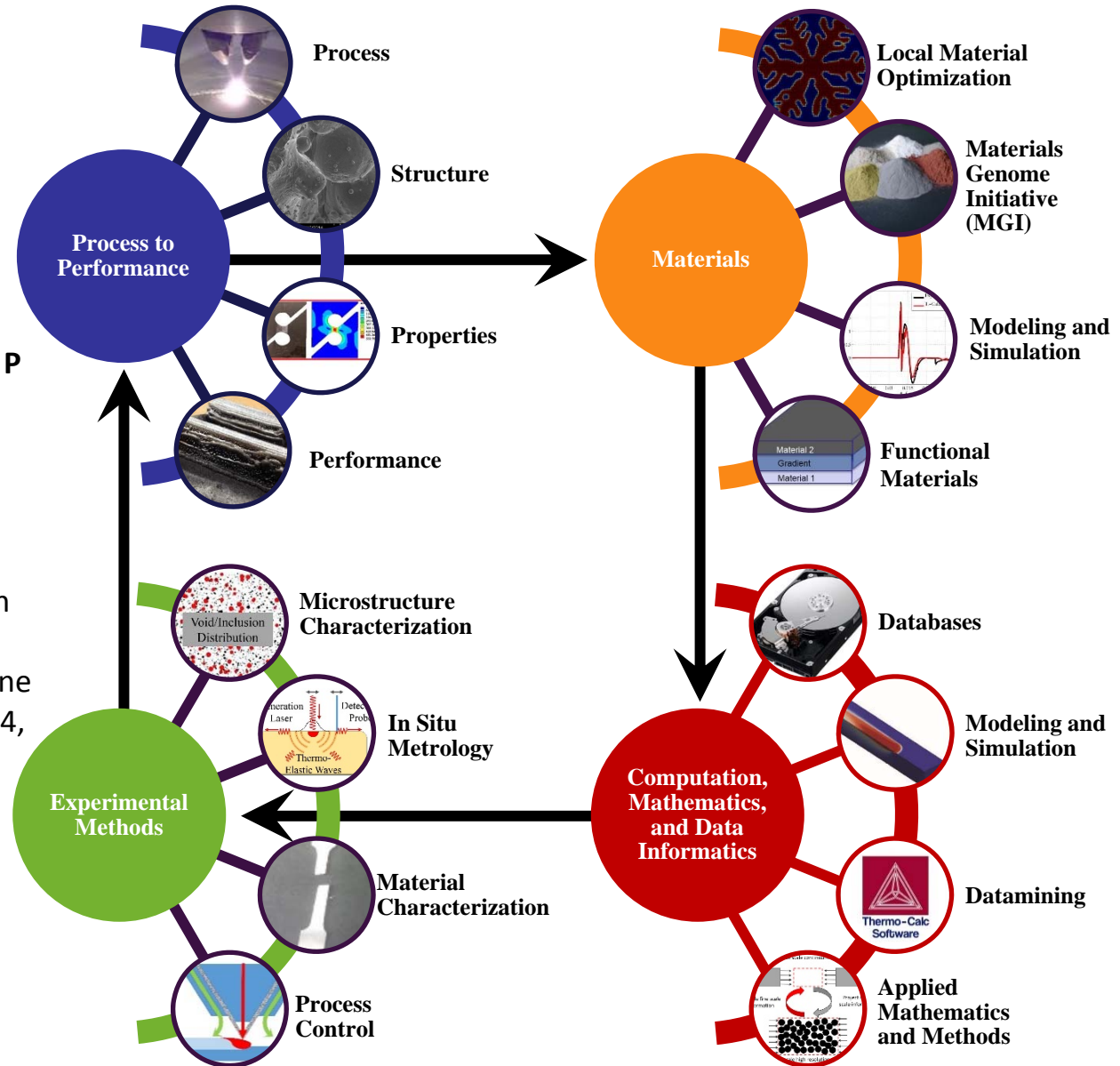
DNS: **Abaqus standard** on Hercules (32 Intel Westmere X5650 processors)  
12 hours

Proposed reduced order method: **Matlab**  
on one Inter® Core i7-3632QM 65 of 19  
5 sec ( $k_1 = 16$ ); 214 sec ( $k_2 = 256$ )

## Northwestern Engineering

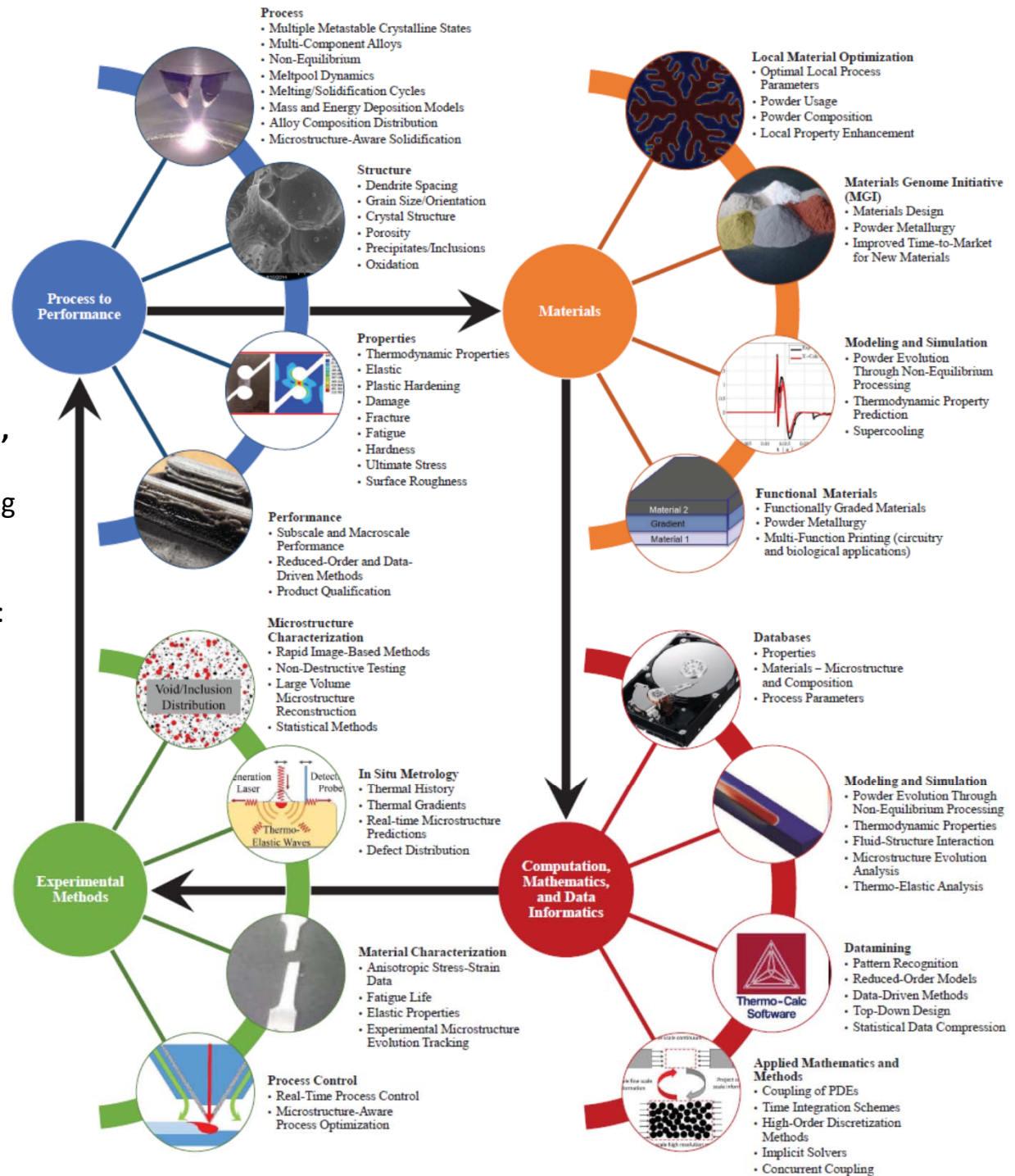






J Smith, W Xiong, W Yan, S Lin, P Cheng, OL Kafka, GJ. Wagner, J Cao, WK.Liu, "Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support," *Computational Mechanics*, Online DOI 10.1007/s00466-015-1240-4, 2016.

J Smith, W Xiong, W Yan, S Lin, P Cheng, OL Kafka, GJ. Wagner, J Cao, WK.Liu, "Linking Process, Structure, Property, and Performance for Metal-based Additive Manufacturing: Computational Approaches with Experimental Support," *Computational Mechanics*, Online DOI 10.1007/s00466-015-1240-4, 2016.



## Materials Genome for Multiscale Modeling and Simulation with Experimental Support for Additive Manufacturing

- **Archetype-Genome exemplar:** the apparent properties of a system depend on the building blocks (archetypes) that comprise it; and apparent system properties create the system genome.
- **Three important entities:** design of **archetype** properties, **conformation** of archetypes (as a result of processing), and **interactions** activated by that conformation. (The combination of these entities into the system genome is called **assembly**.)
- **Integrated design theory/framework (i.e. assembly)** to bridge the gap between computational methods and scales for a well defined genome for particular application(s)
- **AM has a natural application in this framework: Archetype conformation and interactions are apparent with a cursory inspection of the technology**  
The question is, can we develop detailed *material databases, conformation and interaction (statistical descriptions with uncertainty quantification)* to produce a desired genome with AM techniques?