

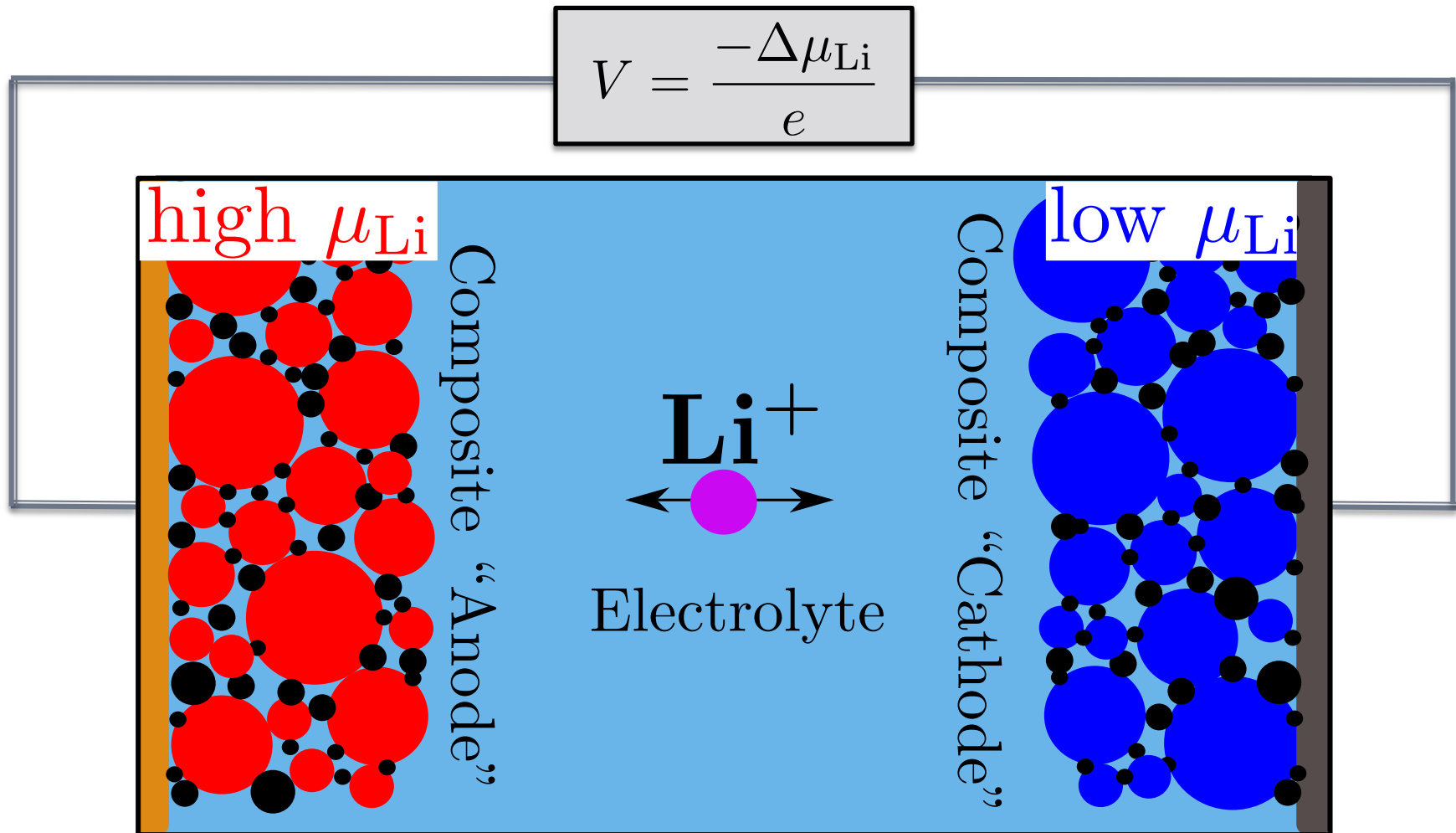
# Electrochemical Shock in Polycrystalline Lithium Storage Materials

William H. Woodford, Yet-Ming Chiang, and W. Craig Carter  
Department of Materials Science and Engineering, MIT

“Whiskers, Wires, and Walls” Workshop – NIST  
30 September 2010

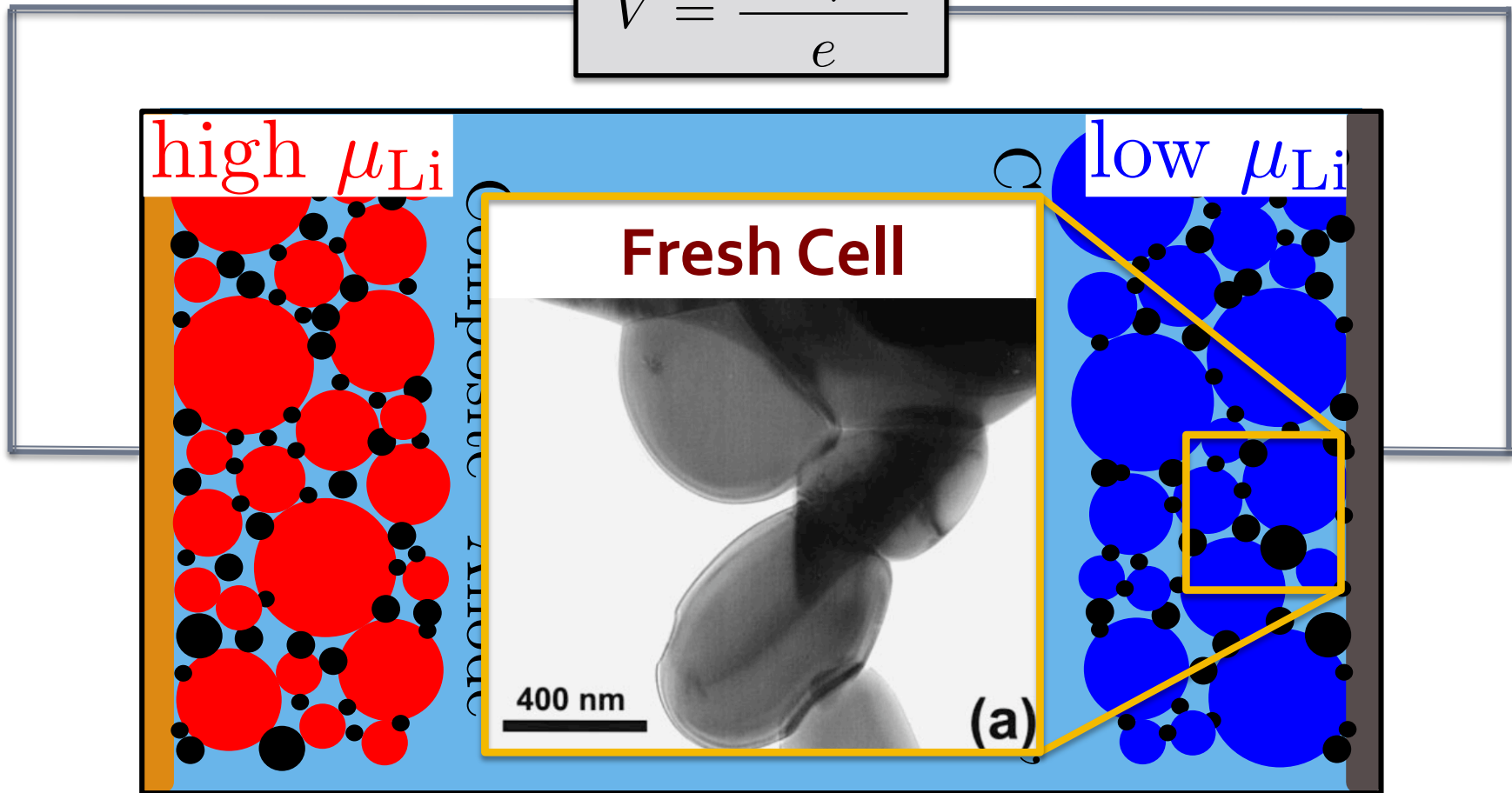
\*J.R. Wilson, et al., *J. Power Sources* (2010), doi:10.1016/j.jpowsour.2010.04.066

# Lithium-ion Batteries – Operating Principles



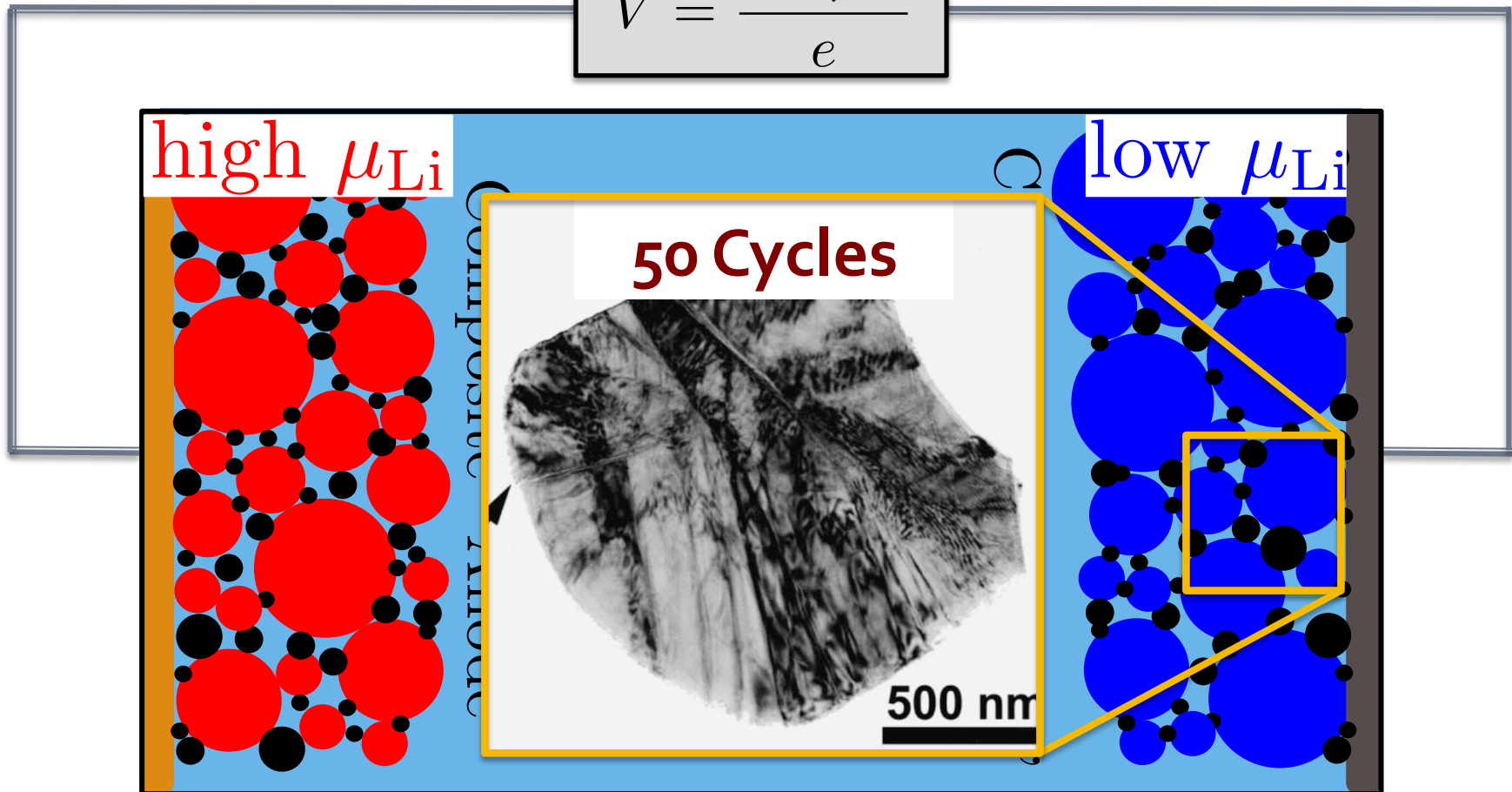
# Lithium-ion Batteries – Operating Principles

$$V = \frac{-\Delta\mu_{\text{Li}}}{e}$$



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H. Wang, Y.-I. Jang, B. Huang, D. Sadoway, and Y.-M. Chiang, *J. Electrochem. Soc.*, **146** (2) 473-480 (1999).

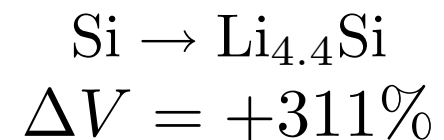
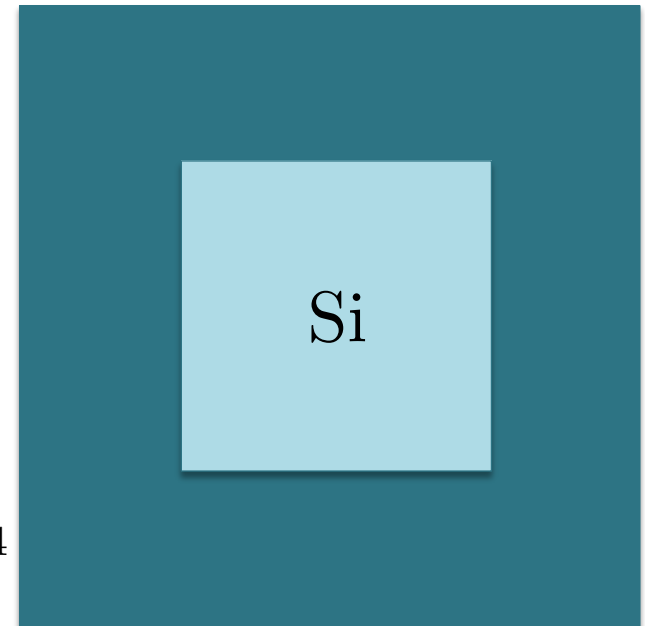
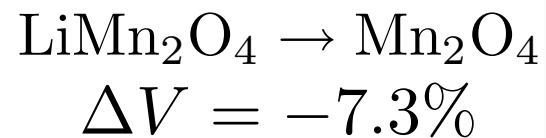
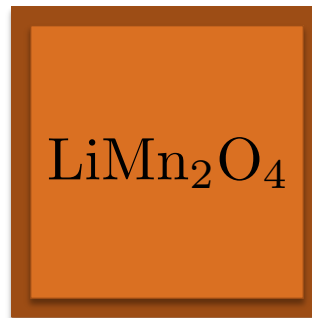
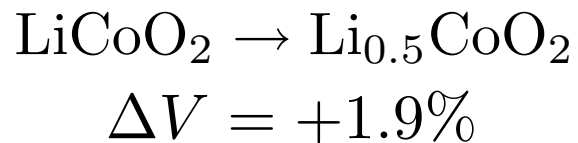
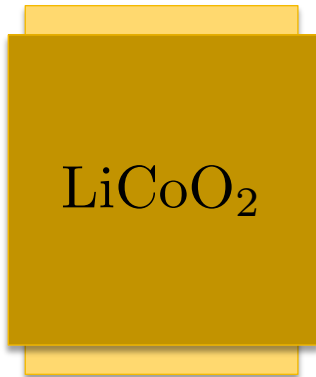
# Most Materials Change Shape with Varying Lithium Content

$\text{LiCoO}_2$

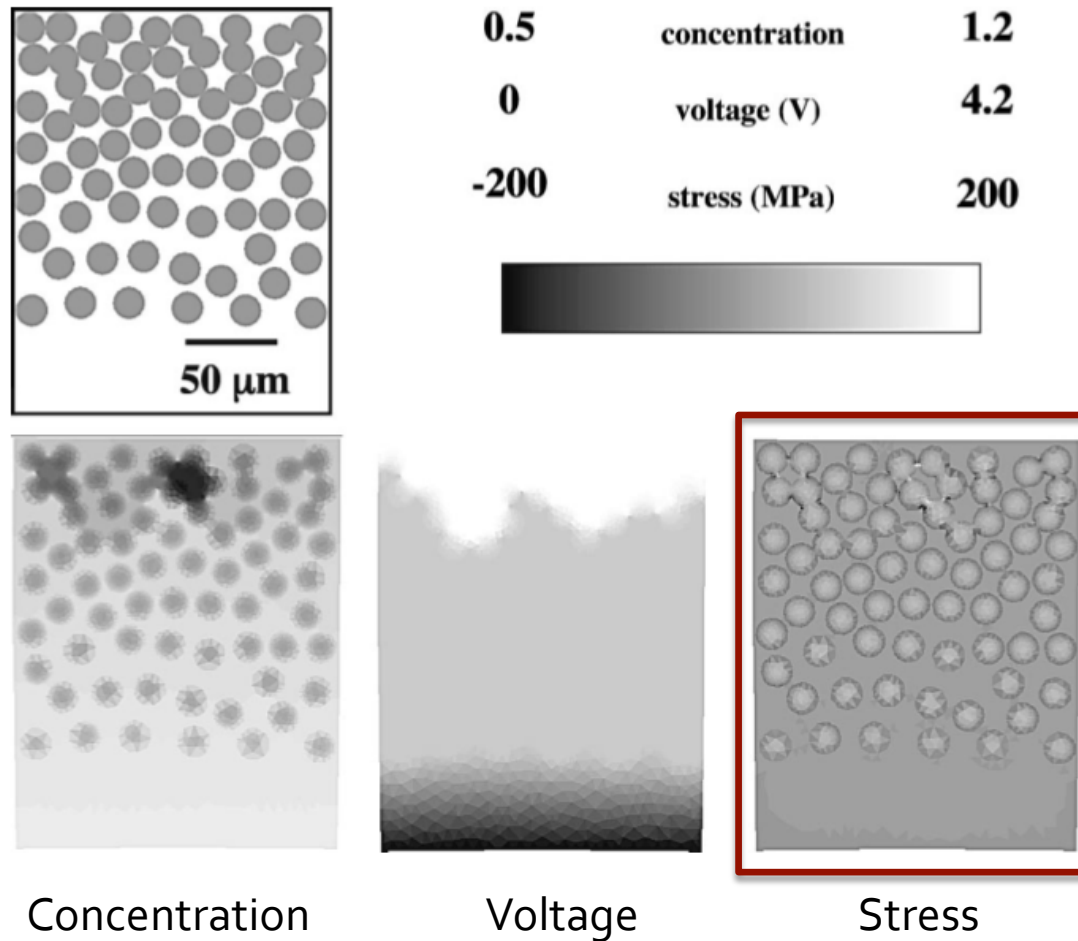
$\text{LiMn}_2\text{O}_4$

Si

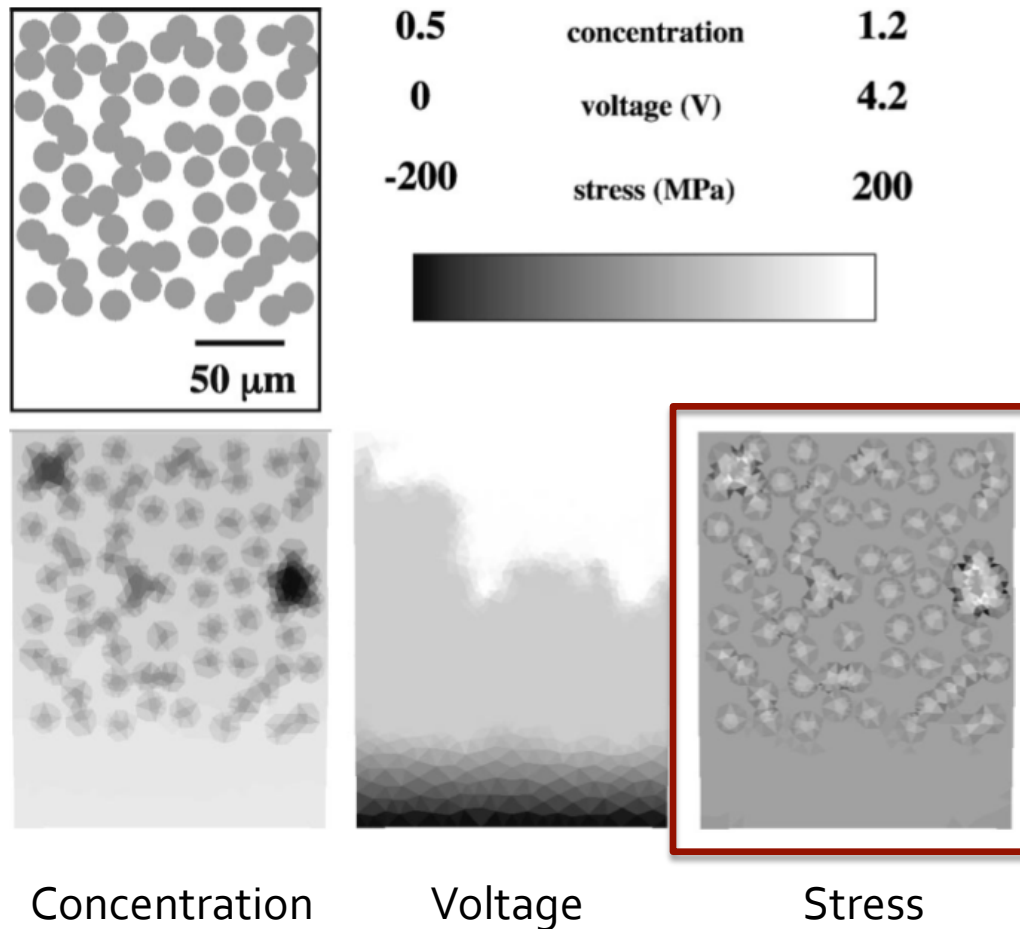
# Most Materials Change Shape with Varying Lithium Content



# Previous Models Have Calculated Diffusion-Induced Stresses

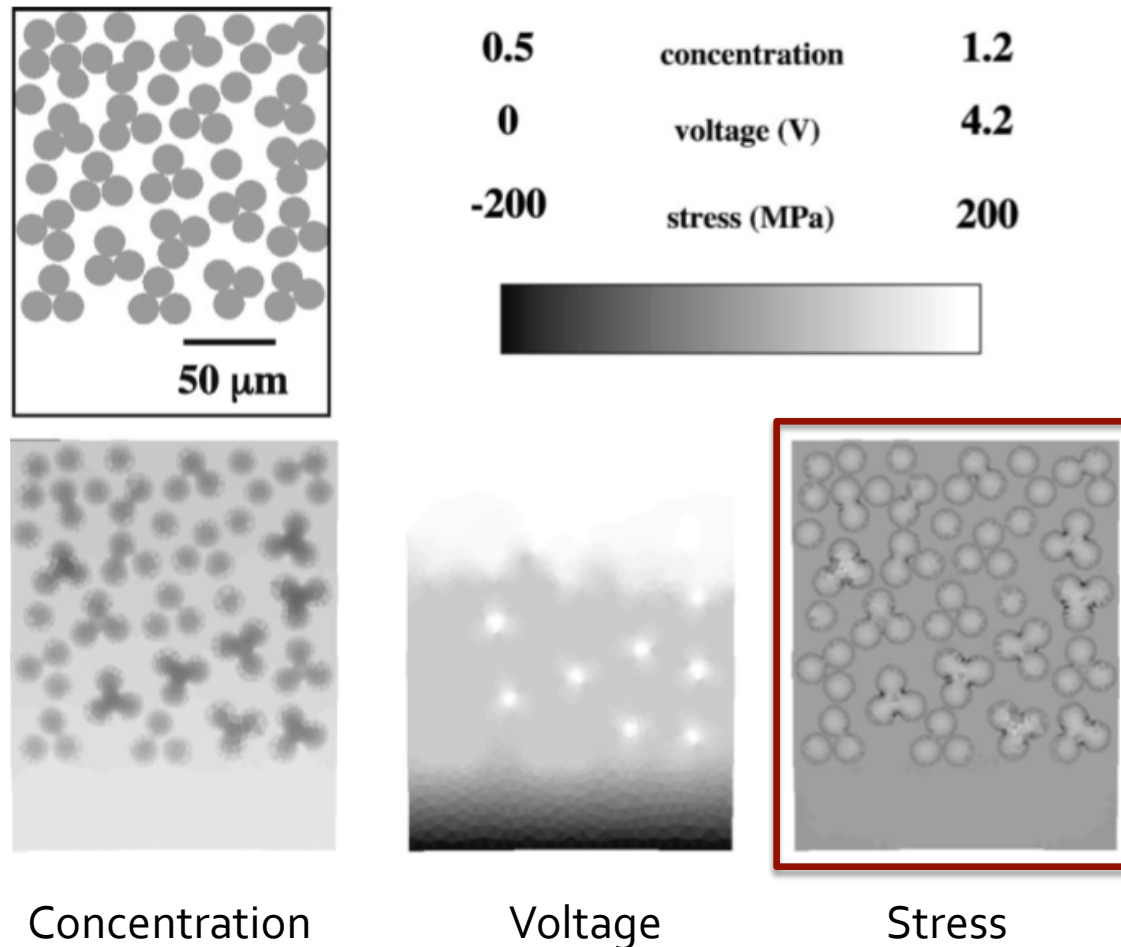


# Previous Models Have Calculated Diffusion-Induced Stresses

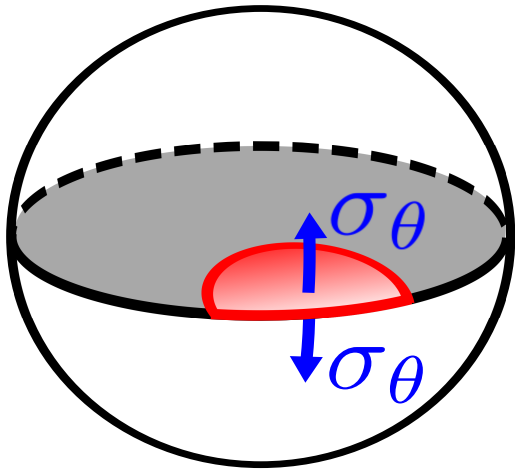




# Previous Models Have Calculated Diffusion-Induced Stresses

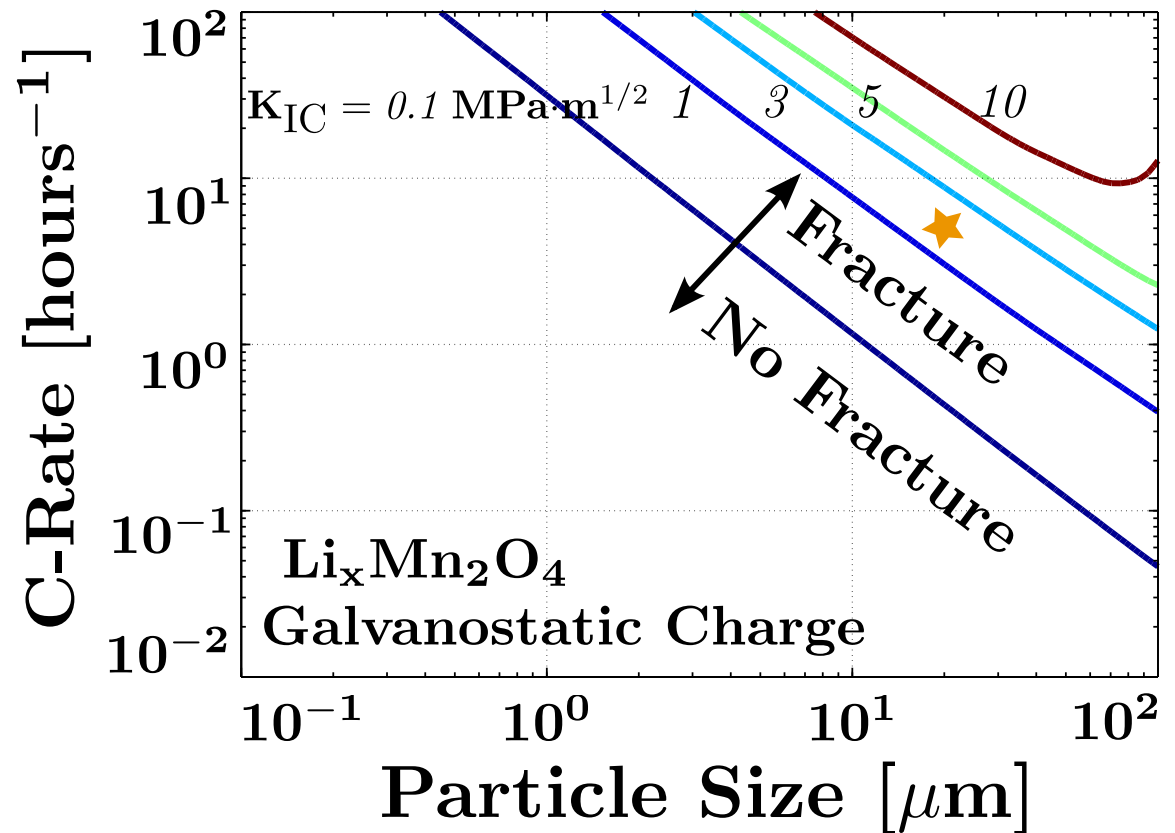


# Link to Fracture Mechanics: Electrochemical Shock Map

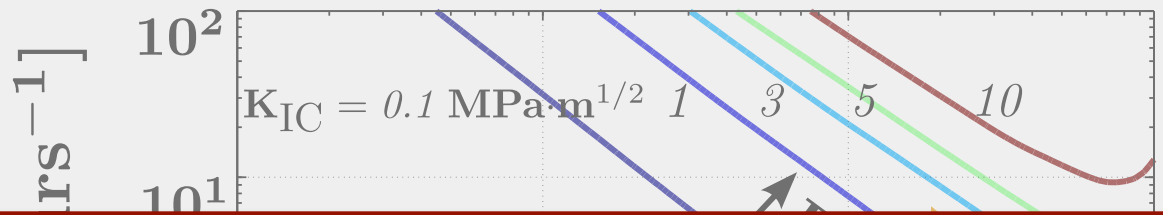
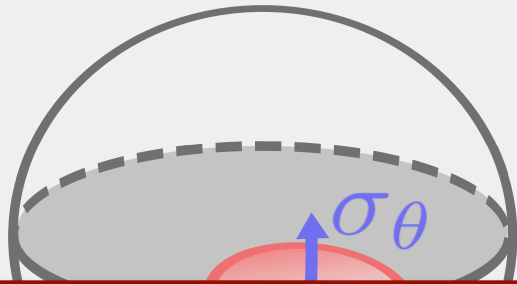


**Critical combinations of particle size and rate**

Need fracture toughness measurements!



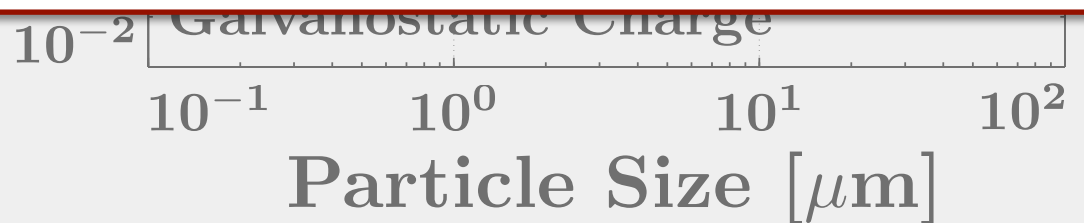
# Link to Fracture Mechanics: Electrochemical Shock Map



## What About Polycrystals?

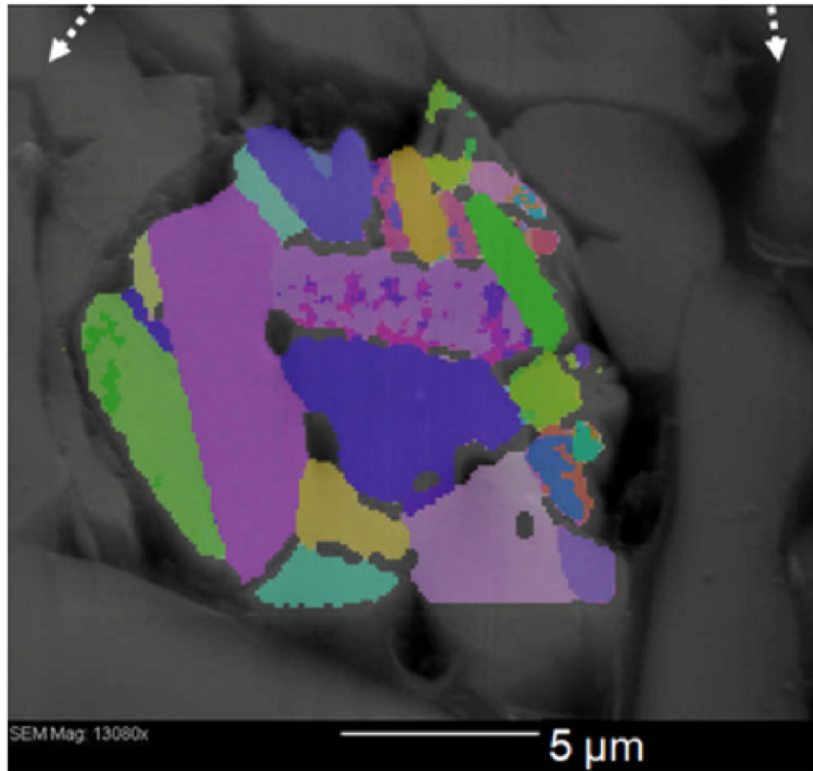
## Phase Transformations?

particle size and  
rate



Need fracture toughness  
measurements!

# Microstructure Matters for Electrochemical Shock



EBSD orientation maps  
for  $\text{LiCoO}_2$   
**polycrystalline** particles  
in composite (Lishen)  
electrodes

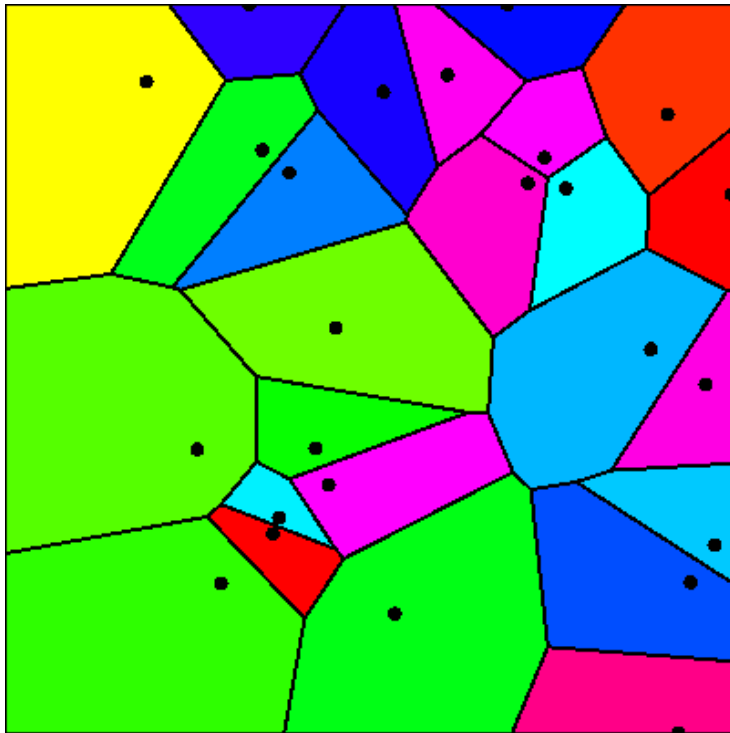
J.R. Wilson, et al., *J. Power Sources* (2010), doi:  
10.1016/j.jpowsour.2010.04.066

# Microstructure Matters for Electrochemical Shock



**Goal:** Develop Models for Electrochemical Shock that incorporate this microstructural complexity and address (anisotropic) phase transformations

# Microstructure Generation



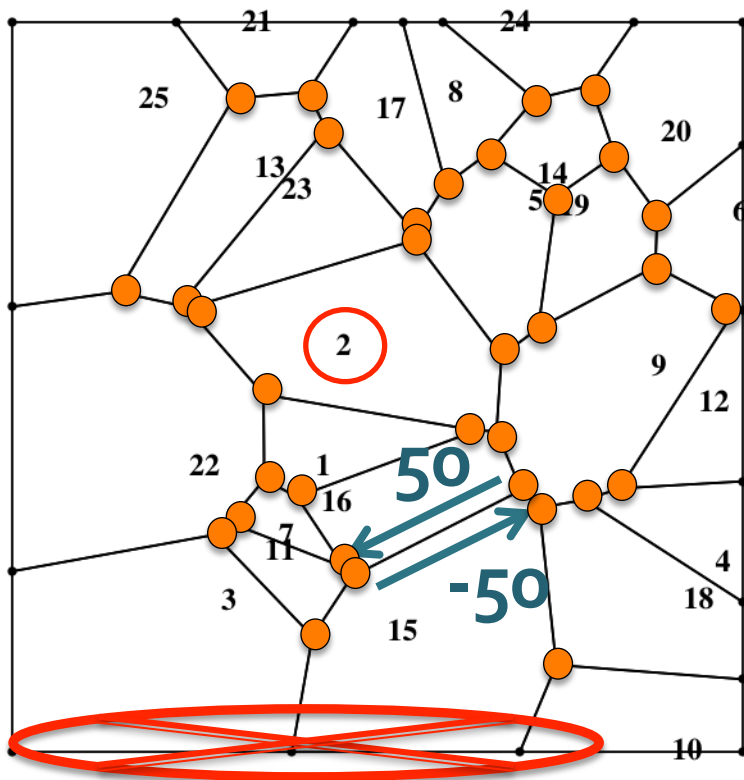
## 2D Voronoi Construction

- $2N$  Random numbers per grain  $(x_{ii}, y_i)$

## Random Grain Orientations

- Use OOF2's EulerABG Convention
- 3 Random numbers per grain for  $(\alpha_{ii}, \beta_{ii}, \gamma_i)$
- All done in *Mathematica*

# Microstructure Information



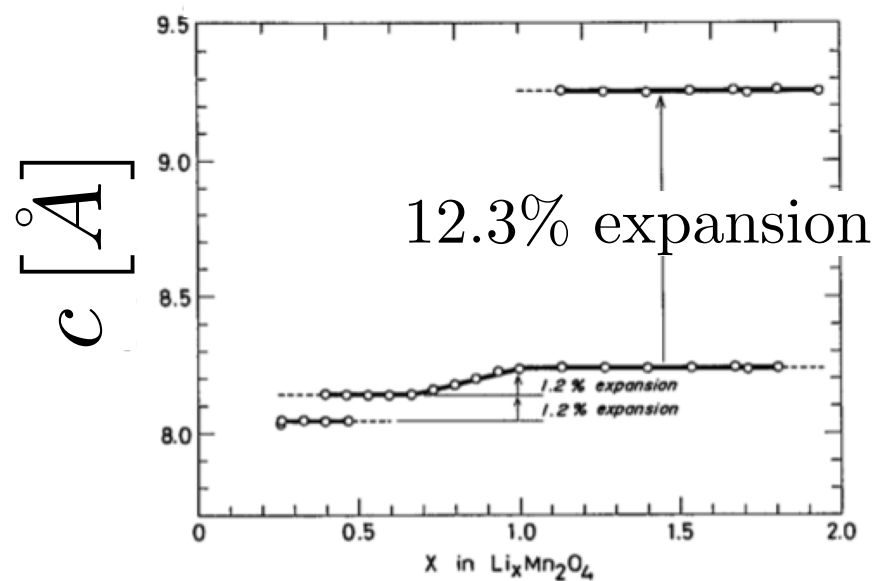
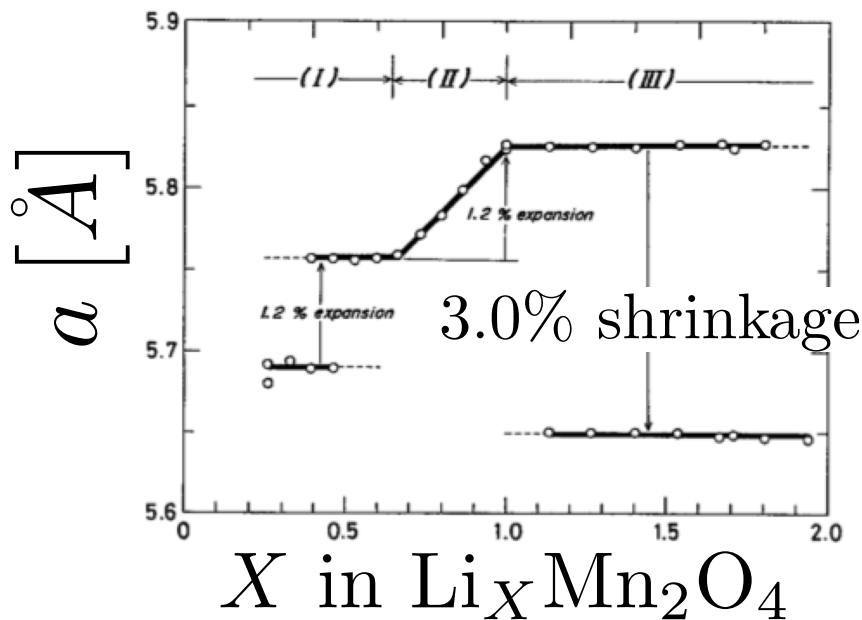
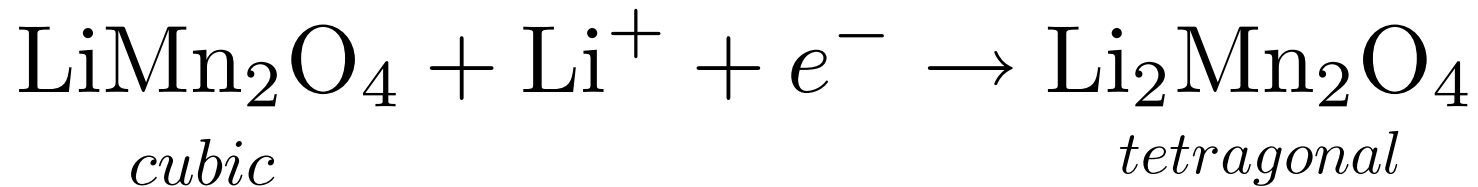
Each grain is numbered

Each boundary is numbered and we know which grains it separates

- $n \rightarrow -n$  for opposite direction along same edge
- Exclude Boundary Edges from Analysis

We know the location of each triple point

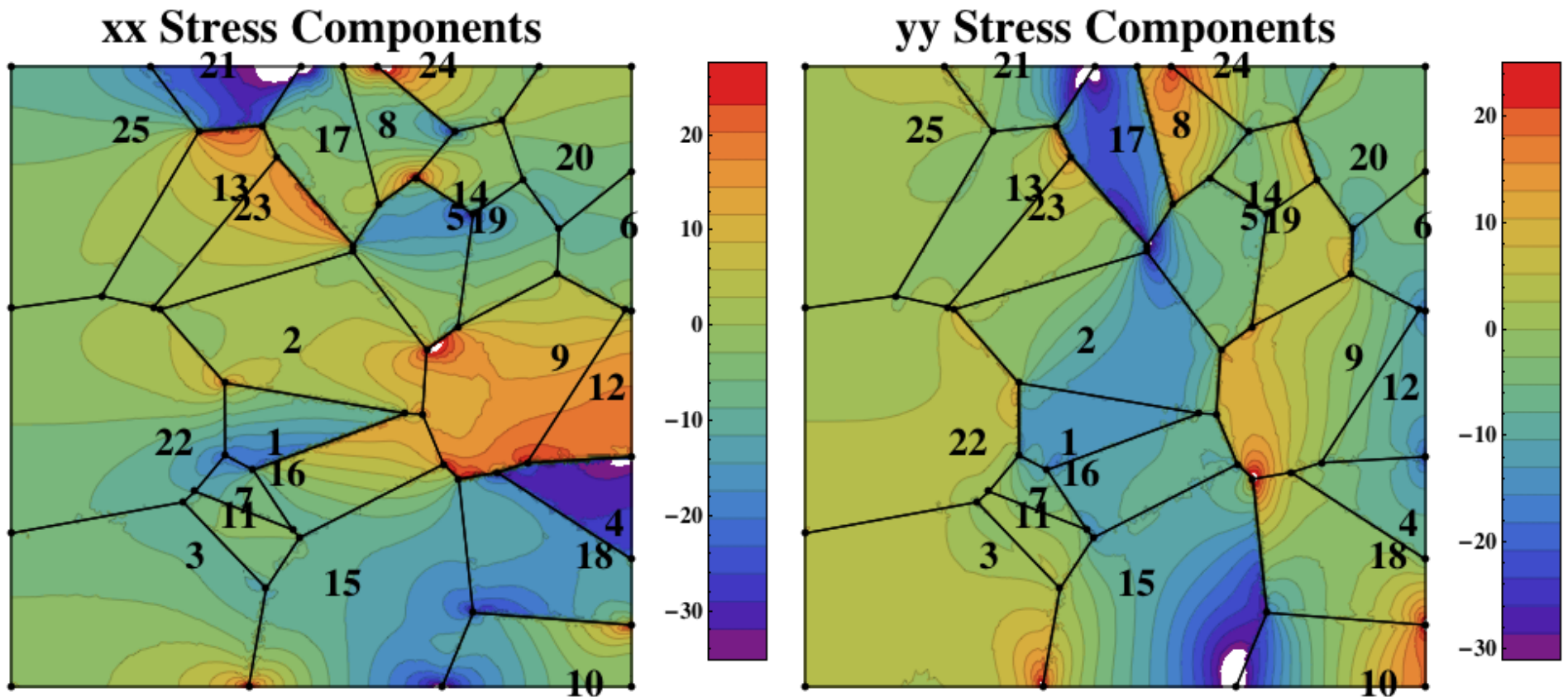
# LiMn<sub>2</sub>O<sub>4</sub>: A Model System



**Start with end point analysis... (Analogies to thermal shock)**



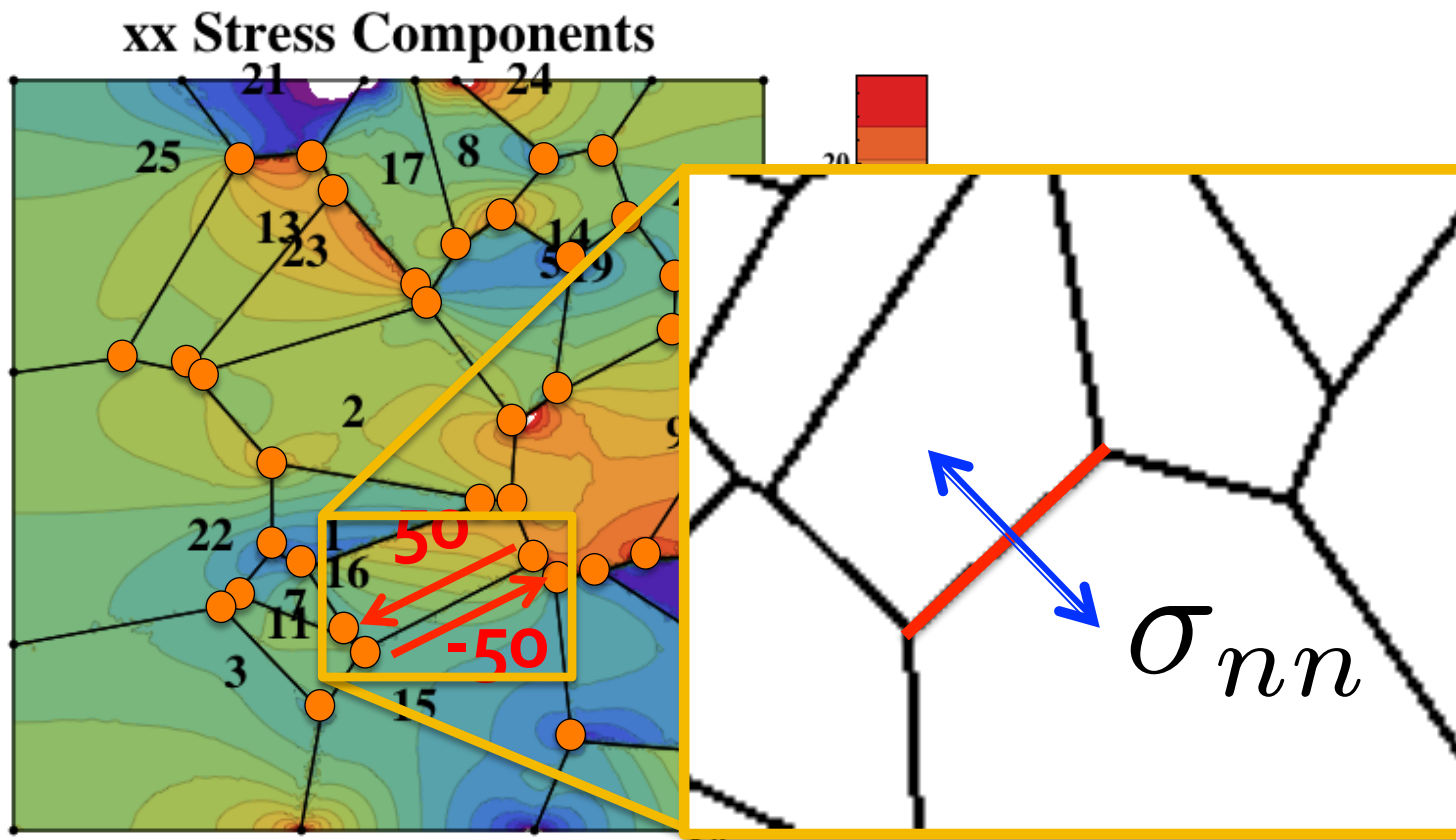
# Cartesian Stress Components



**Assumptions:** Plane Stress Condition; Zero-Displacement normal to external boundaries

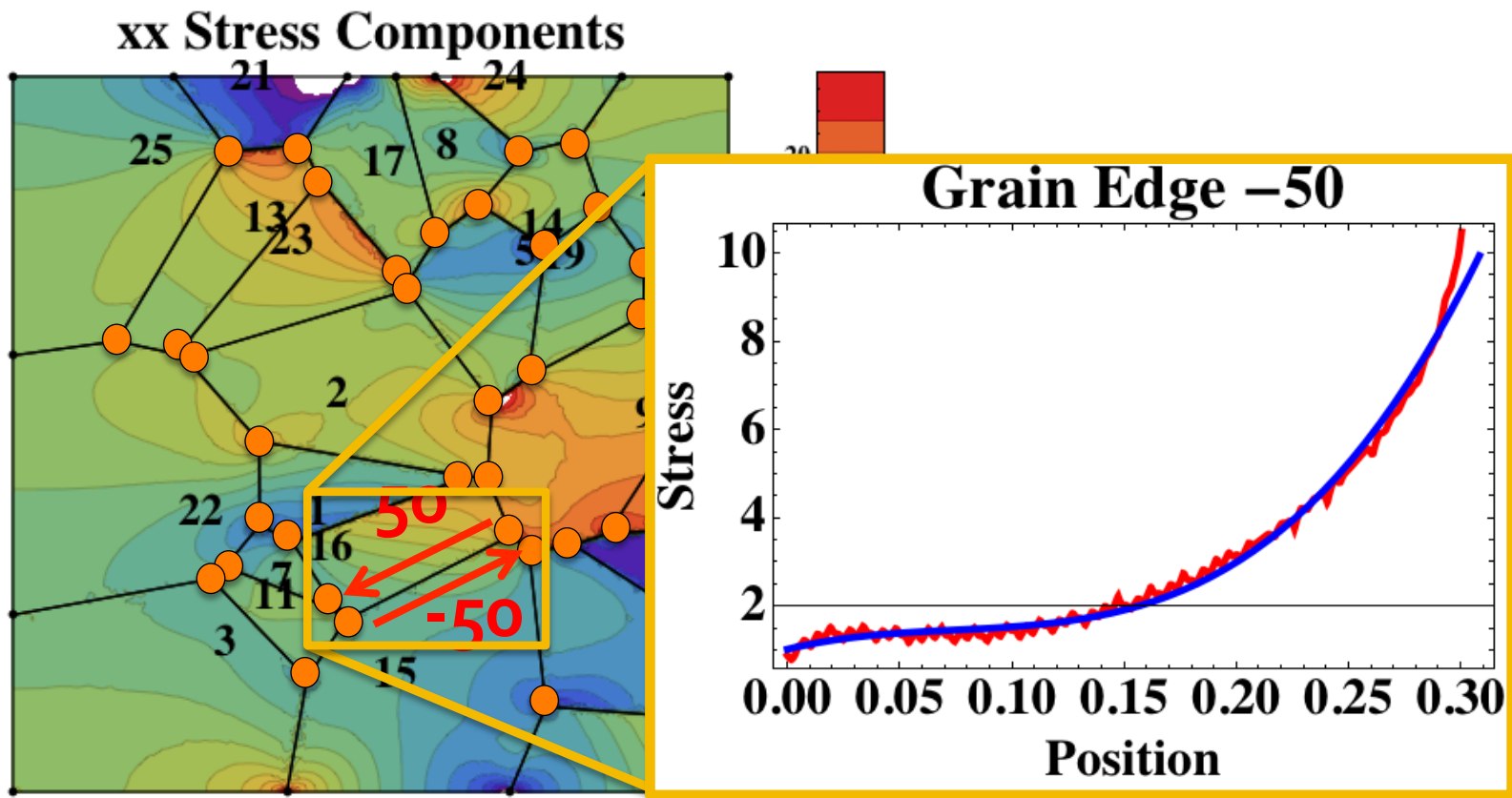
Note: Stresses here are referred to the the OOF/Lab frame coordinates

# Extracting Local Stress Information



Use tensor transformation to extract grain boundary normal stress

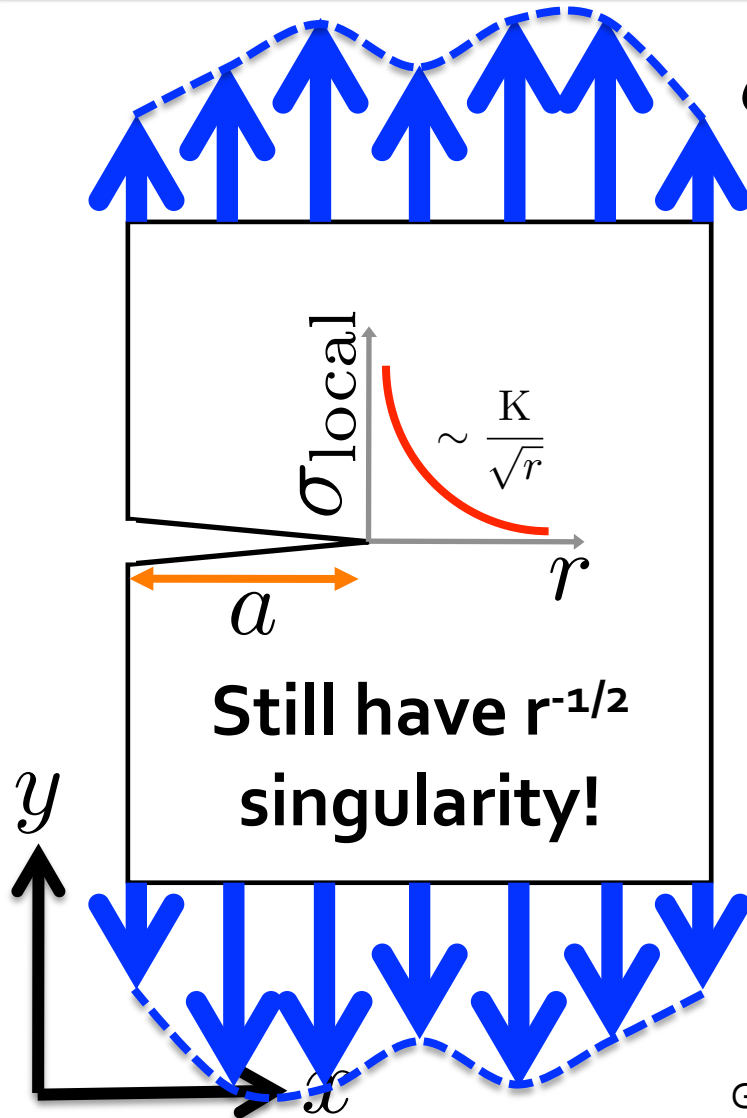
# Extracting Local Stress Information



Red line: Linear interpolation of raw data from OOF2  
Blue line: Calculated with cubic polynomial fit (fast!)

$$\sigma(x) = a + bx + cx^2 + dx^3$$

# Stress-Intensity Factor – Nonuniform Loading



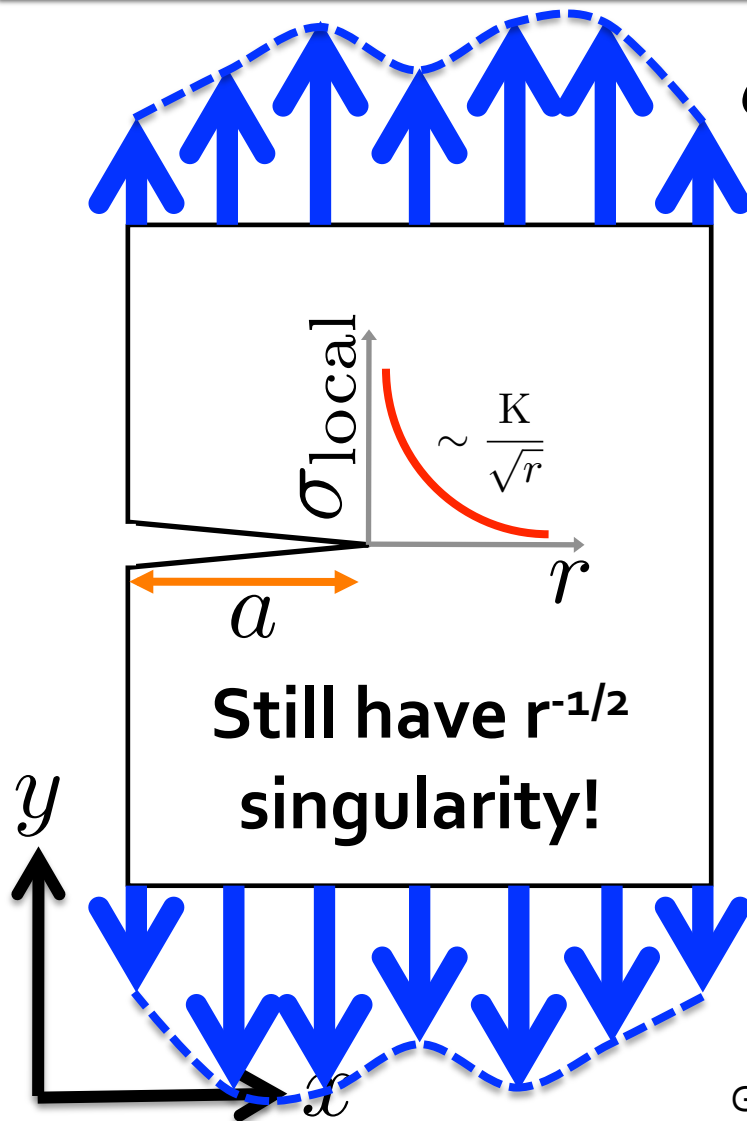
$\sigma_{nn}(x)$

$$K = \frac{2}{\sqrt{\pi a}} \int_0^a \sigma_{nn}(x') \sqrt{\frac{x'}{a-x'}} dx'$$

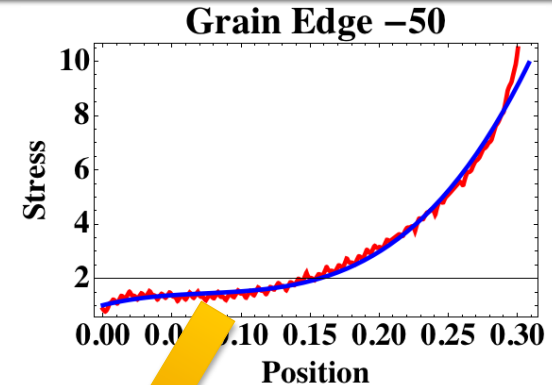
K: Stress-Intensity Factor

$$K > K_{IC}$$

# Stress-Intensity Factor – Nonuniform Loading



$$\sigma_{nn}(x)$$

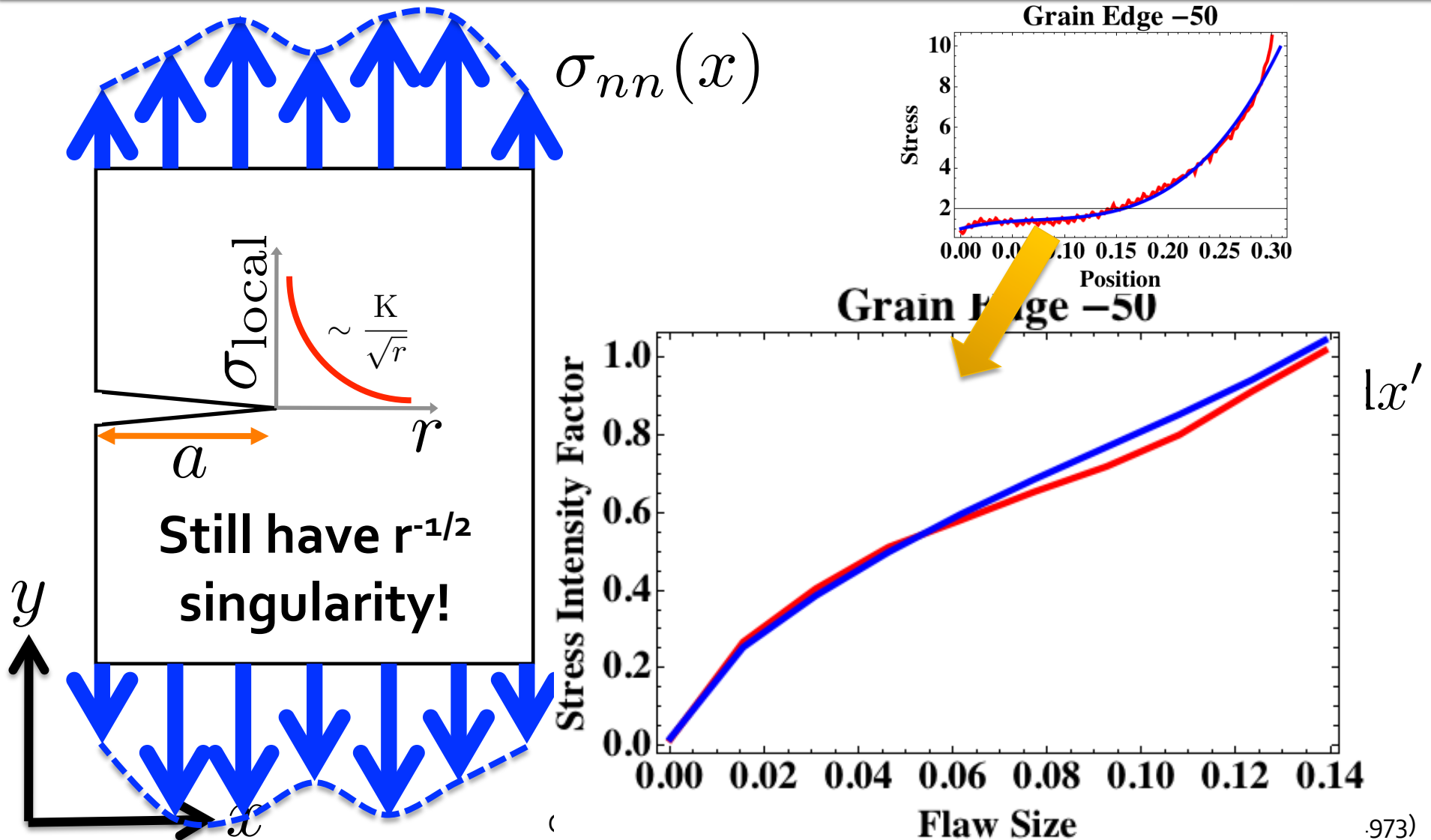


$$K = \frac{2}{\sqrt{\pi a}} \int_0^a \sigma_{nn}(x') \sqrt{\frac{x'}{a-x'}} dx'$$

K: Stress-Intensity Factor

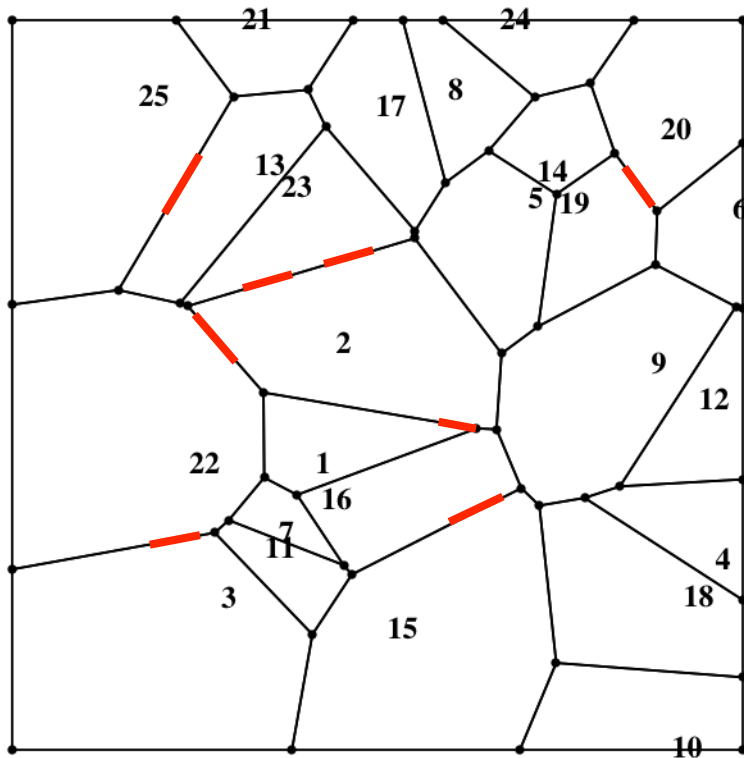
$$K > K_{IC}$$

# Stress-Intensity Factor – Nonuniform Loading



# Introducing Random Flaws

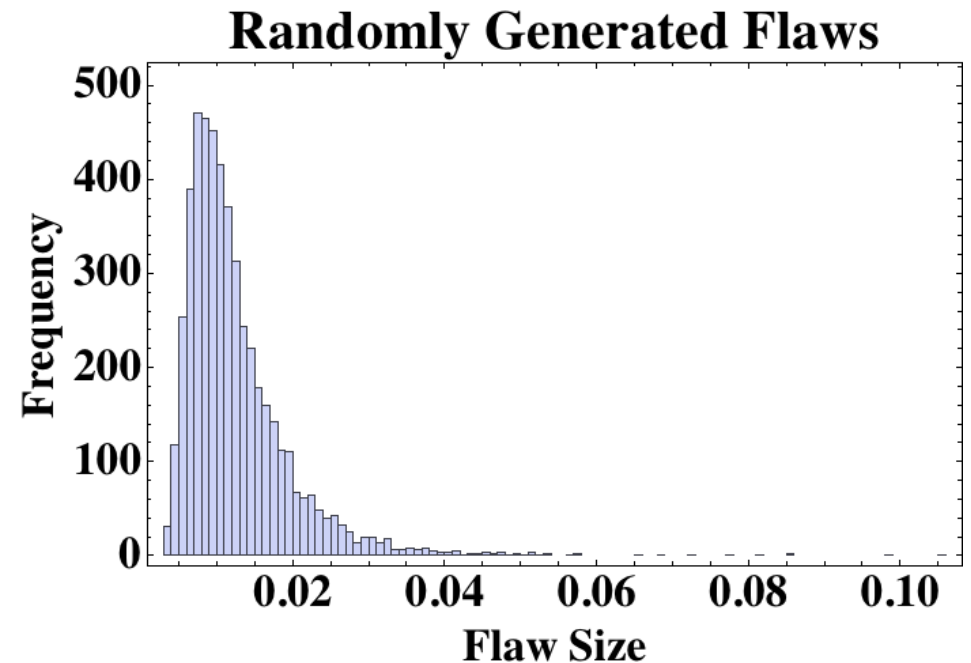
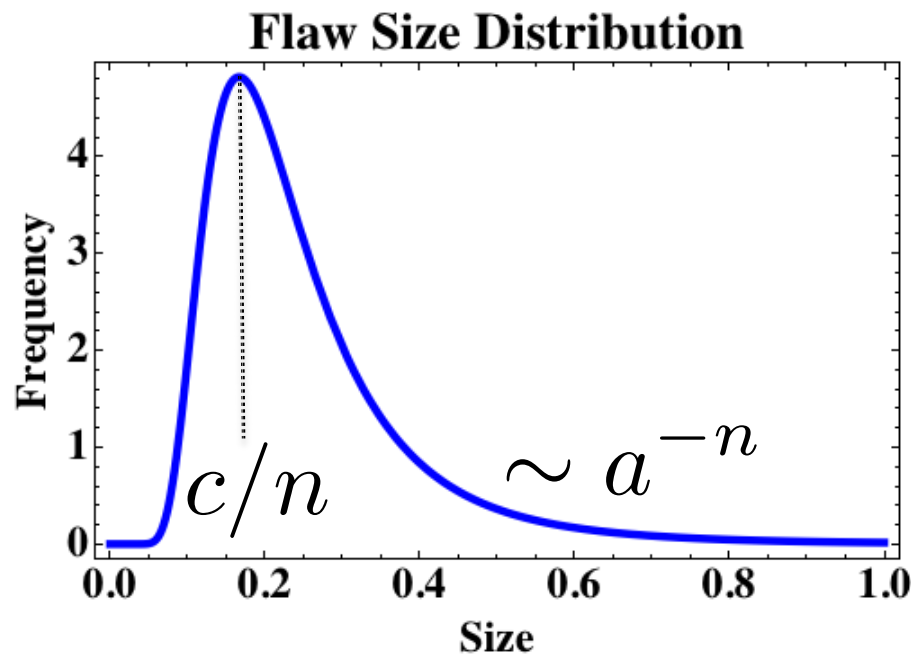
## Method:



- 1) Choose an edge  
Remember, they have been numbered...
- 2) Choose a random flaw size from a flaw size distribution  
Need flaw distribution information!
- 3) Choose a random position along the edge
- 4) Calculate  $K$  using polynomial model for stress distribution

# Flaw Size Distributions

- Flaws are *not* Weibull distributed



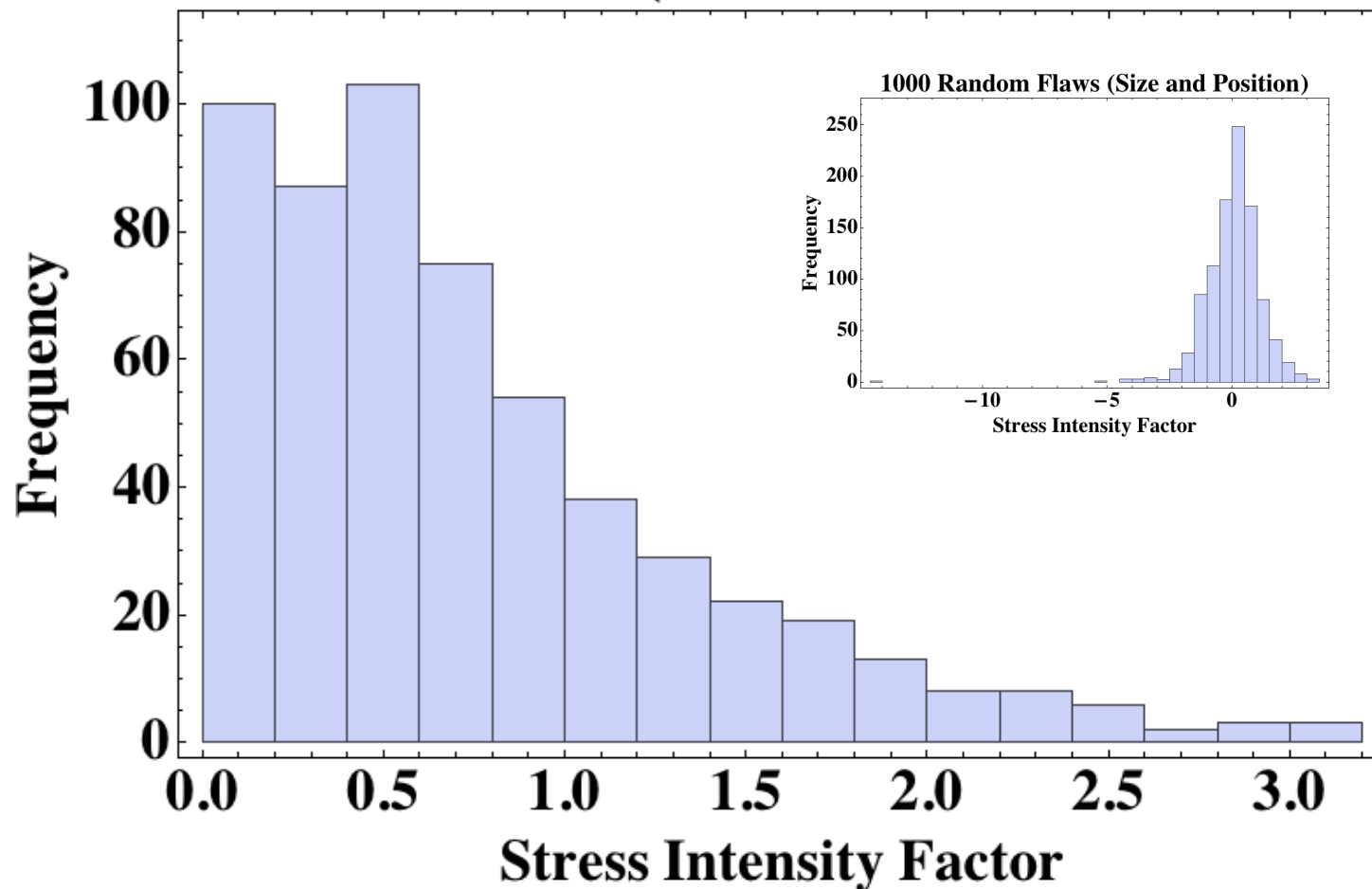
$$f(a) = \frac{c^{n-1}}{(n-2)!} a^{-n} e^{-c/a}$$

f: probability density  
a: flaw size  
c: scale parameter  
n: width parameter



# K Distribution from Random Flaws

## 570 Tensile Flaws (Random Size and Position)



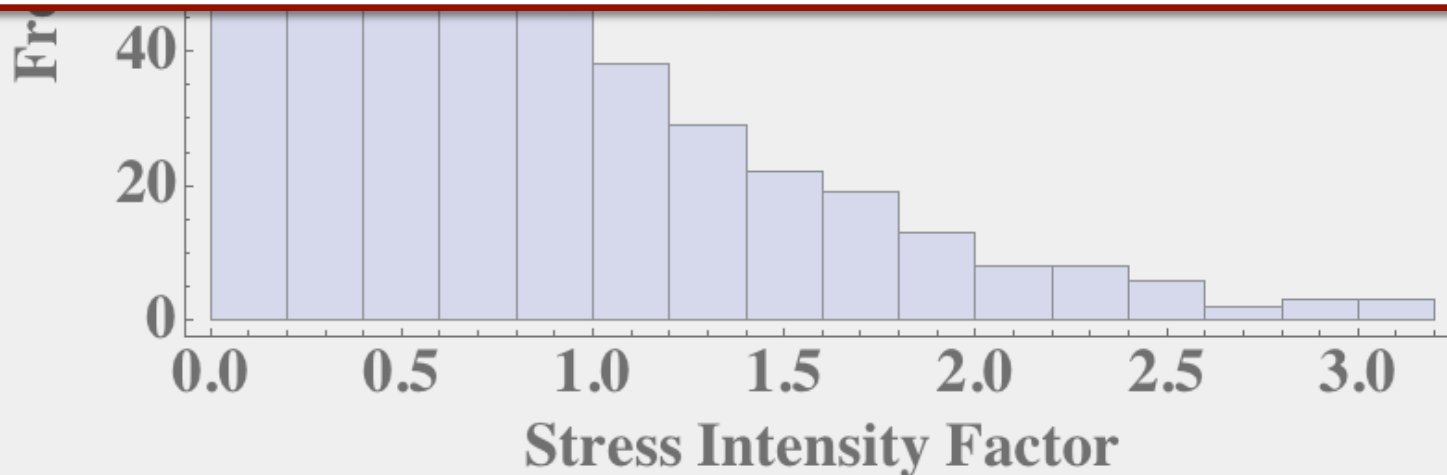
# K Distribution from Random Flaws

570 Tensile Flaws (Random Size and Position)

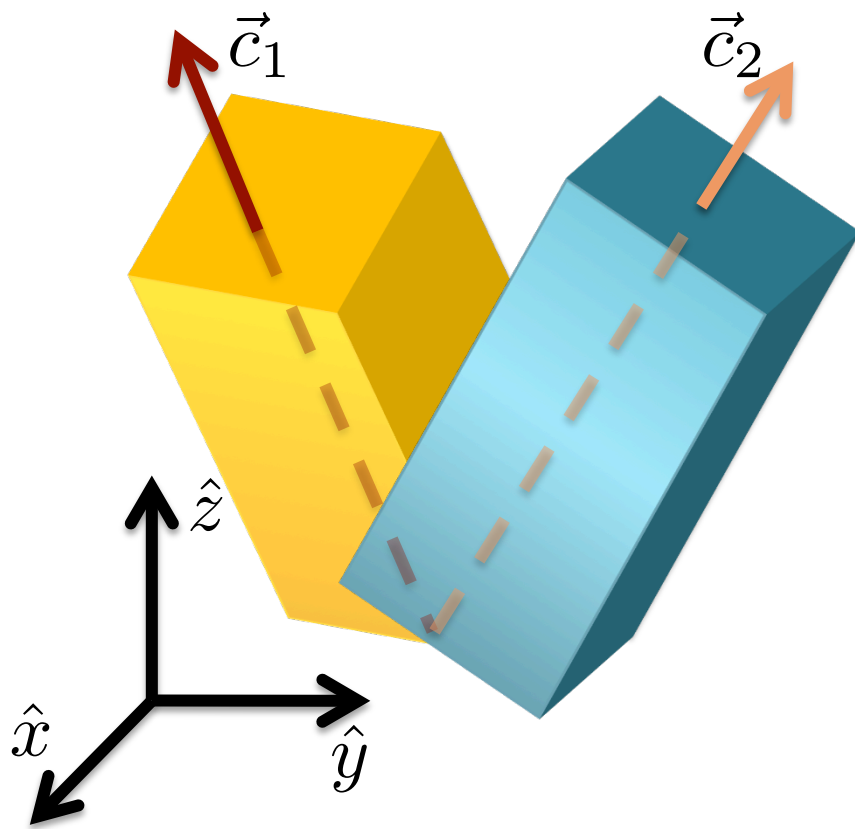


1000 Random Flaws (Size and Position)

**Is this distribution characteristic of the underlying microstructure?**



# Other Potentially Interesting Microstructure Variables



**Grain Orientation**

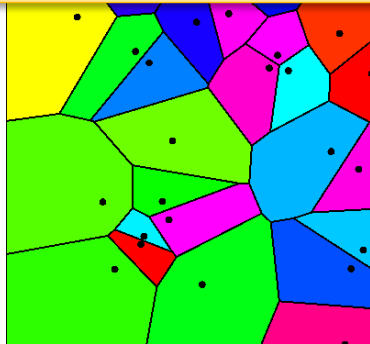
**Triple Points**

**Grain Size**

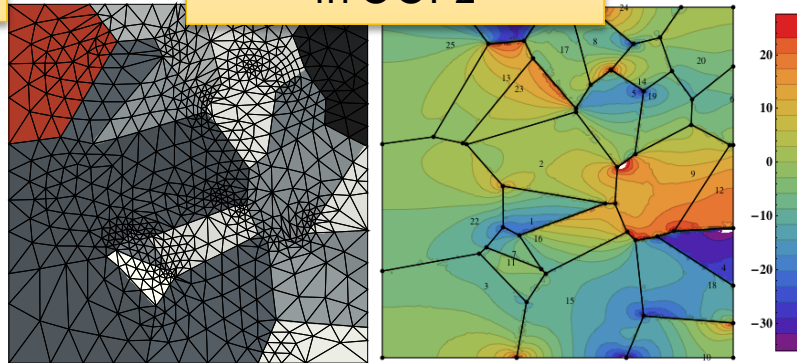
**Porosity**

# Summary

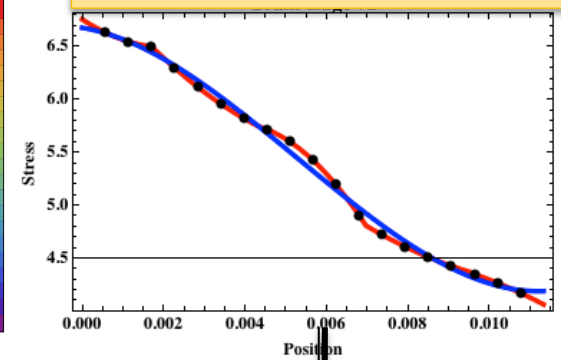
Generate Random Voronoi Microstructure in Mathematica



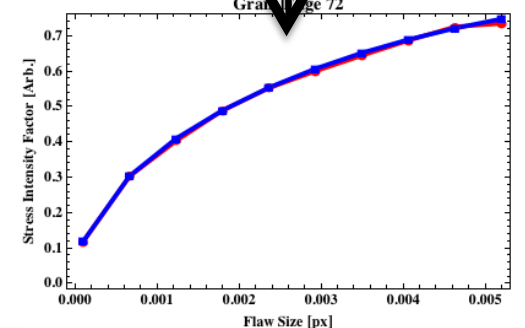
Finite Element Stress Calculations in OOF2



Extract Local Stresses Along Each Grain Boundary

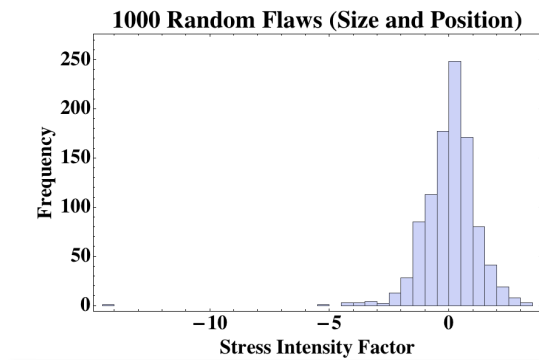


↓  
Grain Size 72

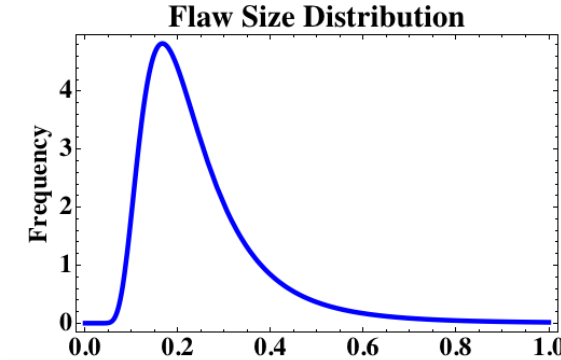


Calculate Stress Intensity Flaw-Size Relations for All Grain Boundaries

Populate the Microstructure with Random Flaws



Extract Failure Probabilities and Extreme Values Statistics



# Conclusions and Future Directions

Microstructure matters for electrochemical shock

– *opportunity for design*

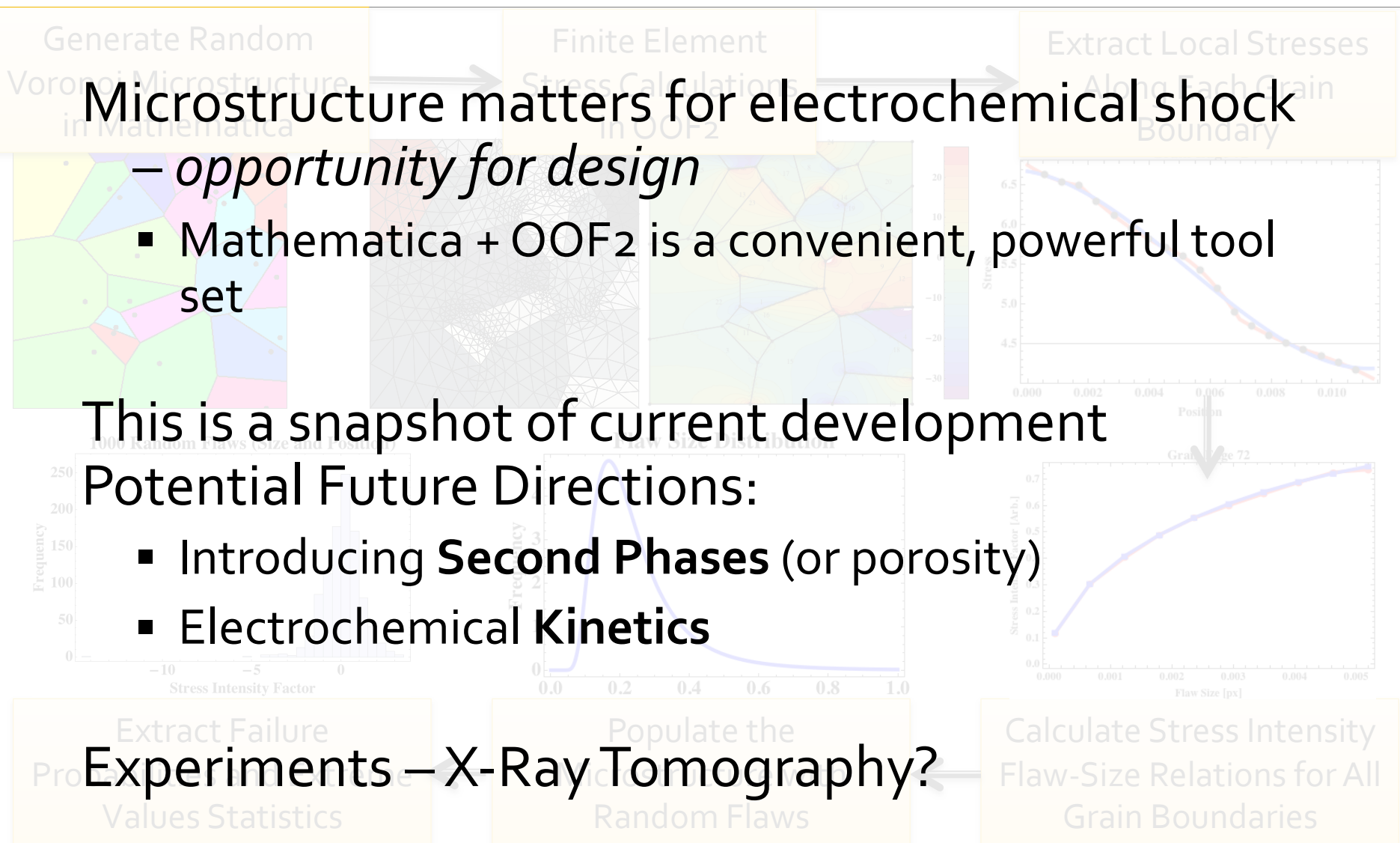
- Mathematica + OOF2 is a convenient, powerful tool set

This is a snapshot of current development

Potential Future Directions:

- Introducing **Second Phases** (or porosity)
- Electrochemical **Kinetics**

Experiments – X-Ray Tomography?



# Acknowledgements

- National Science Foundation Graduate Research Fellowship
- Dept. of Energy, Basic Energy Science, Award No. DE-SC0002633

Questions?